Design Manual For Structural Stainless Steel

(Third Edition)
PREFACE

Third Edition

This Third Edition of the Design Manual has been prepared by The Steel Construction Institute as a deliverable of the RFCS Project - Valorisation Project – Structural design of cold worked austenitic stainless steel (contract RFS2-CT-2005-00036). It is a complete revision of the Second Edition, extending the scope to include cold worked austenitic stainless steels and updating all the references to draft Eurocodes. The Third Edition refers to the relevant parts of EN 1990, EN 1991 and EN 1993. The structural fire design approach in Section 7 has been updated and new sections on the durability of stainless steel in soil and life cycle costing have been added.

Three new design examples have been included to demonstrate the appropriate use of cold worked stainless steel. They were completed by the following partners:

- Universitat Politècnica de Catalunya (UPC)
- The Swedish Institute of Steel Construction (SBI)
- Technical Research Centre of Finland (VTT)

A project steering committee, including representatives from each partner and sponsoring organisation, oversaw the work and contributed to the development of the Design Manual. The following organizations participated in the preparation of the Third Edition:

- The Steel Construction Institute (SCI) *(Project co-ordinator)*
- Centro Sviluppo Materiali (CSM)
- CUST, Blaise Pascal University
- Euro Inox
- RWTH Aachen, Institute of Steel Construction
- VTT Technical Research Centre of Finland
- The Swedish Institute of Steel Construction (SBI)
- Universitat Politècnica de Catalunya (UPC)

Preface to the Second Edition

This Design Manual has been prepared by The Steel Construction Institute as a deliverable of the ECSC funded project, Valorisation Project – Development of the use of stainless steel in construction (contract 7215-PP-056). It is a complete revision of the Design manual for structural stainless steel, which was prepared by The Steel Construction Institute between 1989 and 1992 and published by Euro Inox in 1994.

This new edition takes into account advances in understanding in the structural behaviour of stainless steel over the last 10 years. In particular, it includes the new design recommendations from the recently completed ECSC funded project, Development of the use of stainless steel in construction (contract 7210-SA/842), which has led to the scope of the Manual being extended to cover circular hollow sections and fire resistant design. Over the last ten years a great many new European standards have been issued covering
stainless steel material, fasteners, fabrication, erection, welding etc. The Manual has been updated to make reference to current standards and data in these standards.

A project steering committee, including representatives from each partner, sub-contractor and sponsoring organisation, oversaw the work and contributed to the development of the Manual.

The worked examples were completed by the following partners:

- Centre Technique Industriel de la Construction Métallique (CTICM)
- Luleå Institute of Technology
- RWTH Aachen
- VTT Technical Research Centre of Finland
- The Steel Construction Institute (SCI)

The following people were members of the steering committee and/or completed the design examples:

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- Research Fund for Coal and Steel (RFCS) (formerly, European Coal and Steel Community (ECSC))
- Euro Inox

The contribution made to this and the previous two editions by the European stainless steel producers and other organisations is also gratefully acknowledged.
FOREWORD

This Design Manual has been prepared for the guidance of engineers experienced in the
design of carbon steel structural steelwork though not necessarily in stainless steel
structures. It is not in any way intended to have a legal status or absolve the engineer of
responsibility to ensure that a safe and functional structure results.

The Manual is divided into two parts:

• Part I - Recommendations
• Part II - Design Examples

The Recommendations in Part I are formulated in terms of limit state philosophy and,
where appropriate, are in compliance with the following Parts of Eurocode 3 Design of
steel structures:

EN 1993-1-1 Design of steel structures: General rules and rules for buildings
EN 1993-1-2 Design of steel structures: Structural fire design
EN 1993-1-3 Design of steel structures: General rules: Supplementary rules for
cold-formed members and sheeting
EN 1993-1-4 Design of steel structures: General rules: Supplementary rules for
stainless steels
EN 1993-1-5 Design of steel structures: Plated structural elements
EN 1993-1-8 Design of steel structures: Design of joints
EN 1993-1-9 Design of steel structures: Fatigue
EN 1993-1-10 Design of steel structures: Material toughness and through-thickness
properties

This Design Manual gives recommended values for certain factors. These values may be
subject to modification at a national level by the National Annexes.

The Design Examples contained in Part II demonstrate the use of the recommendations.
A cross-reference system locates that section of the examples corresponding to a
particular recommendation.

The Recommendations and Design Examples are available online at Steelbiz, an SCI
technical information system (www.steelbiz.org), and from the Euro Inox web site
(www.euro-inox.org). A Commentary to the Recommendations, which includes a full set
of references, is also available online at these web sites. The purpose of the
Commentary is to allow the designer to assess the basis of the recommendations and to
facilitate the development of revisions as and when new data become available.
Opportunity is taken to present the results of various test programmes conducted
specifically to provide background data for the Design Manual. The Recommendations,
Design Examples and Commentary are also available on CD from Euro Inox.
An online design facility is available at www.steel-stainless.org/software for designing cold-formed stainless steel members subject to axial tension, bending or axial compression. The design facility calculates section properties and member resistances in accordance with the Recommendations in this Design Manual.

The design recommendations presented in this document are based upon the best knowledge available at the time of publication. However, no responsibility of any kind for injury, death, loss, damage or delay, however caused, resulting from the use of the recommendations can be accepted by the project partners or others associated with its preparation.
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## PART I – RECOMMENDATIONS

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PART 1 - RECOMMENDATIONS

1 INTRODUCTION

1.1 Scope
The recommendations given in this part of the Design Manual apply to the grades of stainless steel that are typically used in structural applications. The recommendations are intended primarily for the design of elements and secondary structural components of buildings, offshore installations and similar structures. They should not be applied to special structures such as those in nuclear installations or pressure vessels for which specific standards for stainless steel application already exist.

The recommendations concern aspects of material behaviour, the design of cold formed and welded members, and their connections. They are applicable to the austenitic and duplex grades of stainless steel that are typically used in structural or architectural applications. The recommendations have been formulated using limit state philosophy.

1.2 Symbols
In general, the symbols used in this Design Manual are the same as used in EN 1993-1-1: Eurocode 3, Design of steel structures: General rules and rules for buildings. Extensive use is made of subscripts, e.g. \( N_{b,z,Rd} \) is the design resistance (subscript Rd) of a column under axial load (\( N \)) to buckling (subscript b) about the minor axis (subscript z).

Dimensions and axes of sections are illustrated in Figure 1.1. Note that contrary to normal practice in many countries, the major axis of a section is normally y-y and the minor axis z-z, see Section 1.3.

Latin upper case letters

\begin{itemize}
  \item \( A \) Accidental action; Area
  \item \( C \) Fixed value; Factor
  \item \( E \) Modulus of elasticity; Effect of actions
  \item \( F \) Action; Force
  \item \( G \) Permanent action; Shear modulus
  \item \( I \) Second moment of area
  \item \( L \) Length; Span; System length
  \item \( M \) Bending moment
  \item \( N \) Axial force
  \item \( Q \) Variable action
  \item \( R \) Resistance
  \item \( V \) Shear force
  \item \( W \) Section modulus
\end{itemize}
**Greek upper case letters**

Δ Difference in ……. (precedes main symbol)

**Latin lower case letters**

a Distance between stiffeners; Throat thickness of a weld
b Width; Breadth
c Distance; Outstand
d Diameter; Depth
e Eccentricity; Shift of neutral axis; Edge distance; End distance
f Strength (of a material)
g Gap
h Height
i Radius of gyration; Integer
k Coefficient; Factor
l Buckling length
m Constant
n Number of …
p Pitch; Spacing
q Distributed force
r Radius; Root radius
s Staggered pitch
t Thickness
uu Major axis
vv Minor axis
w Curling deformation
xx, yy, zz Rectangular axes

**Greek lower case letters**

α (alpha) Ratio; Factor
β (beta) Ratio; Factor
γ (gamma) Partial factor
ε (epsilon) Strain; Coefficient = \( \frac{235 E}{210000 f_y} \)^{0.5}
λ (lambda) Slenderness ratio (a bar above indicates non dimensional)
ρ (rho) Reduction factor
σ (sigma) Normal stress
τ (tau) Shear stress
ϕ (phi) Ratio
χ (chi) Reduction factor (for buckling)
ψ (psi) Stress ratio; Reduction factor

**Subscripts**

a Average
b Bearing; Buckling; Bolt
c Cross section
cr Critical
d  Design
E  Euler; Internal force; Internal moment
eff Effective
e Effective (with further subscript)
el  Elastic
f  Flange
g  Gross
i,j,k  Indices (replace by numeral)
k  Characteristic
LT  Lateral-torsional
M  (Allowing for) bending moment
N  (Allowing for) axial force
net  Net
o  Initial
pl  Plastic
R  Resistance
r  Reduced value
S  Secant
s  Tensile stress (area); Stiffener
t  Tension; Tensile; Torsion
u  Major axis of cross-section; Ultimate
V  (Allowing for) shear force
v  Shear; Minor axis of cross-section
w  Web; Weld; Warping
x  Axis along member
y  Yield (proof value); Axis of cross-section (major axis except for unsymmetric sections)
z  Axis of cross-section (minor axis except for unsymmetric sections)
σ  Normal stress
τ  Shear stress.

1.3 Conventions for member axes

In general, the convention for member axes is:

xx  along the length of the member.

yy  cross-section axis perpendicular to web, or the larger leg in the case of angle sections.

zz  cross-section axis parallel to web, or the larger leg in the case of angle sections.

The yy axis will normally be the major axis of the section and the zz axis will normally be the minor axis. For angle sections, the major and minor axes (uu and vv) are inclined to the yy and zz axes, see Figure 1.1.

The convention used for subscripts which indicate axes for moments is: "Use the axis about which the moment acts".

For example, for an I-section a bending moment acting in the plane of the web is denoted $M_y$ because it acts about the cross-section axis perpendicular to the web.
1.4 Units

For calculations, the following units are recommended:

- forces and loads: kN, kN/m, kN/m²
- unit mass: kg/m³
- unit weight: kN/m³
- stresses and strengths: N/mm² (= MN/m² or MPa)
- bending moments: kNm.

Note that, in accordance with European practice, a “,” symbol is used to separate the integer part from the decimal part in a number.

Figure 1.1 Dimensions and axes of sections
2 BASIS OF DESIGN

2.1 General requirements
A structure should be designed and fabricated so that it can:

- remain fit for use during its intended life
- sustain the loads which may occur during construction, installation and usage
- localise damage due to accidental overloads
- have adequate durability in relation to maintenance costs.

The above requirements can be satisfied by using suitable materials, by appropriate design and detailing and by specifying quality control procedures for construction and maintenance.

Structures should be designed by considering all relevant limit states.

2.2 Limit state design
Limit states are limiting conditions which, when exceeded, make the structure unable to meet design performance criteria. Three classes of limit states are recognised: ultimate limit states, serviceability limit states and durability limit states. Ultimate limit states are those which, if exceeded, can lead to collapse of part or the whole of the structure, endangering the safety of people. Serviceability limit states correspond to states beyond which specified service criteria are no longer met. Durability limit states can be regarded as subsets of the ultimate and serviceability limit states depending on whether, for example, the corrosion affects the strength of the structure or its aesthetic appearance. Examples of these limit states are given below:

Ultimate Limit State
- Strength (including general yielding, rupture, buckling and transformation into a mechanism)
- Stability against over-turning and sway
- Fracture due to fatigue

Serviceability Limit State
- Deflection
- Vibration (e.g. wind induced)
- Repairable damage due to fatigue
- Creep

Durability Limit State
- Corrosion
- Metallurgical stability
**Ultimate limit states**

For ultimate limit states, relationships of the following form have to be satisfied:

\[ E_d \leq R_d \]  

(2.1)

where:

- \( E_d \) is the design value of the effect of actions such as an internal moment or vector in the member or element under consideration due to the factored applied loading (see Section 2.3) acting on the structure, and
- \( R_d \) is the corresponding design resistance, as given in the appropriate clause in these recommendations.

The design resistance, \( R_d \), is generally given as \( R_k/\gamma_M \) where \( R_k \) is a characteristic resistance and \( \gamma_M \) is a partial factor. The partial factor \( \gamma_M \) takes on various values. Table 2.1 gives the \( \gamma_M \) values to be used with this Design Manual which are taken from EN 1993-1-4 and EN 1993-1-8. Reference should also be made to the National Annex (NA) to EN 1993-1-4 and other relevant parts of EN 1993 for the country for which the structure is being designed because modified values for \( \gamma_M \) may be given that should be used instead of the values given in Table 2.1. (If a NA is not available, then \( \gamma_M \) factors should be agreed with the relevant national regulator.)

As an alternative to analysis, the design resistance may be assessed by testing of materials, components and structures (for guidance see Section 9).

**Table 2.1  Recommended values of \( \gamma_M \)**

<table>
<thead>
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<th>For resistance of:</th>
<th>Symbol</th>
<th>Value (EN 1993-1-4)</th>
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<td>Cross-sections to excessive yielding including buckling</td>
<td>( \gamma_{M0} )</td>
<td>1,10</td>
</tr>
<tr>
<td>Members to instability assessed by member checks</td>
<td>( \gamma_{M1} )</td>
<td>1,10</td>
</tr>
<tr>
<td>Cross-sections in tension to fracture</td>
<td>( \gamma_{M2} )</td>
<td>1,25</td>
</tr>
<tr>
<td>Bolts, welds, pins and plates in bearing</td>
<td>( \gamma_{M2} )</td>
<td>1,25</td>
</tr>
</tbody>
</table>

<table>
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<tr>
<th>For resistance of:</th>
<th>Symbol</th>
<th>Value (EN 1993-1-8)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Joints in hollow section lattice girder</td>
<td>( \gamma_{M5} )</td>
<td>1,00</td>
</tr>
<tr>
<td>Pins at the serviceability limit state</td>
<td>( \gamma_{M6,ser} )</td>
<td>1,00</td>
</tr>
</tbody>
</table>

**Serviceability limit states**

The corresponding relationship for serviceability limit states is:

\[ E_d \leq C_d \]  

(2.2)

where:

- \( E_d \) is the design value of the effects of actions specified in the serviceability criterion e.g. member deflection response to forces and
moments in the member due to the unfactored applied loading \((F_k, \text{ see Section 2.3.4})\), and

\[ C_d \]

is the limiting design value of the relevant serviceability criterion.

**Durability limit states**

These states require consideration of the corrosion phenomena addressed in Section 3.7.

### 2.3 Loading

#### 2.3.1 General

In the Eurocodes, loading is expressed terms of ‘actions’. An ‘action’ is defined as:

- A set of forces (loads) applied to the structure (direct action)
- A set of imposed deformations or accelerations caused by, for example temperature changes, moisture variation, uneven settlement or earthquakes (indirect action).

Characteristic values \((F_k)\) of individual actions are specified:

- in EN 1991 *Actions on structures* (taking into account possible additions and/or changes in the relevant National Annex) or other relevant loading code, or
- by the client, or the designer in consultation with the client, provided that the minimum provisions specified in the relevant loading codes or by a competent authority are observed.

The design values of individual actions \((F_d)\) are given by multiplying characteristic actions by partial factors for actions \((\gamma_f)\).

The design case is established by considering all realistic combinations of actions and identifying the critical case.

#### 2.3.2 Ultimate limit state - Onshore factored loads

The following types of action are recognised:

- “Permanent” actions \((G)\) - e.g. self-weight of structures, fittings, ancillaries and fixed equipment.
- “Variable” actions \((Q)\) - e.g. imposed loads, wind loads, snow loads, and thermal loads.
- “Accidental” actions \((A)\) - e.g. explosions, fire and vehicle impact.

EN 1990 *Basis of Structural Design* gives combinations of actions for use in design of buildings and recommended values for partial factors for actions \((\gamma_f)\). Reference should also be made to the National Annex to EN 1990 for the country for which the structure is being designed because it may give modified values for \(\gamma_f\) that should be used instead of the recommended values. The NA also gives recommended values for the combination factors \((\psi\text{ factors})\) and the unfavourable permanent actions \((\xi\text{ factors})\). (If a NA is not available, then \(\gamma_f\), \(\psi\) and \(\xi\) factors should be agreed with the relevant national regulator.)
Reference should be made to the National Annex of EN 1991 regarding numerical values for loads.

As given in EN 1990, for normal usage, i.e. in situations not involving accidents, the combination of actions may be expressed as:

\[
\sum_{j \geq 1} \gamma_{G,j} G_{k,j} + \gamma_{Q,1} Q_{k,1} + \sum_{i \geq 1} \gamma_{Q,i} \psi_{0,i} Q_{k,i}
\]  
(2.3)

or alternatively, the less favourable of the following expressions

\[
\sum_{j \geq 1} \gamma_{G,j} G_{k,j} + \gamma_{Q,1} \psi_{0,1} Q_{k,1} + \sum_{i \geq 1} \gamma_{Q,i} \psi_{0,i} Q_{k,i}
\]  
(2.4a)

\[
\sum_{j \geq 1} \xi_j \gamma_{G,j} G_{k,j} + \gamma_{Q,1}Q_{k,1} + \sum_{i \geq 1} \gamma_{Q,i} \psi_{0,i} Q_{k,i}
\]  
(2.4b)

where:

- \( G_{k,j} \) is the characteristic value of the permanent action
- \( Q_{k,1} \) is the characteristic value of leading variable action 1 (i.e. the most unfavourable variable action)
- \( Q_{k,i} \) are the characteristic values of the accompanying variable actions i
- \( j \) is the index for permanent action
- \( i \) is the index for variable action
- \( \gamma_{G,j} \) is the partial factor for the permanent action \( G_{k,j} \)
- \( \gamma_{Q,1} \) is the partial factor for the leading variable action 1
- \( \xi_j \) is a reduction factor for unfavourable permanent actions G
- \( \psi_{0,i} \) is a reduction factor for combination value of a variable action Q.

However, reference again should be made to the NA for the particular country for which the structure is being designed.

The following recommended values are given in EN 1990:

\[
\begin{align*}
\gamma_{G,j} & = 1.35 \text{ (for unfavourable effects)} \\
\gamma_{Q,1} & = 1.5 \\
\gamma_{Q,i} & = 1.5 \\
\xi & = 0.85
\end{align*}
\]

The value of \( \psi_{0,i} \) depends on the type of loading (see EN 1990).

Equations 2.4a and 2.4b were introduced because Equation 2.3 was unduly pessimistic for heavyweight structures. For steel structures, Equations 2.4a and 2.4b generally result in lighter loads than Equation 2.3.

### 2.3.3 Ultimate limit state - Offshore factored loads


The following factored load combinations from API RP2A for the in-place condition are suggested for use in this Design Manual in conjunction with the
loads specified in API RP2A for the design of topside stainless steel components. Note that the notation is as used in API RP2A.

**Operating conditions:**

\[ 1,3D_1 + 1,3D_2 + 1,5L_1 + 1,5L_2 + 1,2(W_o + 1,25D_n) \]  

(2.5)

**Extreme storm conditions:**

\[ 1,1D_1 + 1,1D_2 + 1,1L_1 + 1,35(W_e + 1,25D_n) \]  

(2.6)

When internal forces due to gravity loads oppose the internal forces due to wind, wave and current loads, the gravity loads should be reduced such that:

\[ 0,9D_1 + 0,9D_2 + 0,8L_1 + 1,35(W_e + 1,25D_n) \]  

(2.7)

where:

- \( D_1 \) is the dead load, including self-weight of structures, fittings, ancillaries and permanent equipment
- \( D_2 \) is the dead load, including weight of equipment and other objects which may change from one mode of operation to another
- \( L_1 \) is Live load 1 (includes weight of consumable supplies in pipes and tanks)
- \( L_2 \) is Live load 2 (short duration forces arising from operations such as lifting of drill string, lifting by cranes, machine operations, vessel mooring and helicopter loadings)
- \( W_o \) is the operator defined operating wind, wave and current load or effects
- \( W_e \) are the extreme wind, wave and current load or effects (100 year return period)
- \( D_n \) are the inertial forces.

**2.3.4 Serviceability limit state loads**

Serviceability limit states should be checked for the following combinations:

- characteristic
- frequent
- quasi-permanent load combinations.

EN 1990 gives combinations of actions for use in design of buildings. (Reference should also be made to the NA for the particular country for which the structure is being designed.) EN 1990 also requires that the acceptable deflection should be agreed with the client.

For the characteristic combination, normally used for irreversible limit states, the following load combination should be used:

\[ \sum_{j \geq 1} G_{k,j} + Q_{k,1} + \sum_{i > 1} \psi_{0,i} Q_{k,i} \]  

(2.8)

where all terms are defined in Section 2.3.2.
Note that EN 1990 gives the appropriate combinations of actions to use in the following situations:

- for calculating deflections under normal combinations of actions (Clause A.1.4.3(1))
- when long term deformations due to shrinkage, relaxation or creep need to be considered (Clause A.1.4.3(6))
- if the appearance of the structure or the comfort of the user or functioning of machinery are being considered (Clauses A.1.4.3(4) and (5)).
3 MATERIALS: PROPERTIES, SELECTION AND DURABILITY

3.1 Material grades

3.1.1 Introduction

There are many different types of stainless steel. Not all of these are suitable for structural applications, particularly where welding is contemplated. There are five basic groups of stainless steel, classified according to their metallurgical structure: these are the austenitic, ferritic, martensitic, duplex and precipitation-hardening groups. The austenitic stainless steels and the duplex stainless steels are generally the more useful groups for structural applications.

Austenitic stainless steels provide a good combination of corrosion resistance, forming and fabrication properties. Duplex stainless steels have high strength and wear resistance with very good resistance to stress corrosion cracking.

The most commonly used grades, typically referred to as the standard austenitic grades, are 1.4301 (widely known as 304) and 1.4401 (widely known as 316). They contain about 17-18% chromium and 8-11% nickel. Grade 1.4301 is suitable for rural, urban and light industrial sites whilst grade 1.4401 is a more highly alloyed grade and will perform well in marine and industrial sites.

The low carbon versions of these grades are 1.4307 (304L) and 1.4404 (316L). Grades 1.4301 and 1.4401 were formerly made with significantly higher carbon levels with implications for corrosion behaviour\(^1\). Either the ‘L’ grade, or a stabilised steel such as 1.4541 and 1.4571 would have been used where there was concern about corrosion performance in the as-welded condition.

Grade 1.4318 is a low carbon, high nitrogen stainless steel which work hardens very rapidly when cold worked. It has a long track record of satisfactory performance in the railcar industry and is equally suitable for automotive, aircraft and architectural applications. Grade 1.4318 has similar corrosion resistance to 1.4301 and is most suitable for applications requiring higher strength than 1.4301 where large volumes are required. It is procured directly from the mill; specifiers interested in using 1.4318 should check availability directly with the mill. Its price is likely to be slightly higher than 1.4301, depending on the amount required.

An increasing use of stainless steels for load bearing applications has led to a demand for ‘lean’ duplex grades in which the mechanical and corrosion properties of duplex grades are combined with a leanly alloyed chemical composition. In the forthcoming Parts 4 and 5 of EN 10088 (see Section 3.1.2), the newly developed duplex grade 1.4162 is included. Grade 1.4162 is suitable for many applications in the construction sector with a proof strength in

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\(^1\) Carbon present in the steel reacts with chromium and precipitates chromium carbides on grain boundaries under certain thermal cycles, e.g. in the weld heat affected zones (HAZ). The local loss of chromium from the boundary region into the carbide particles allows preferential intercrystalline corrosion attack and the steel is said to be sensitized, or to suffer from weld decay (see Section 3.7.2).
the range of 450 – 530 N/mm², a corrosion resistance between the austenitic grades 1.4301 and 1.4404 and a lean chemical composition.

Only the rolled versions, as opposed to the cast versions, are considered. Guidance on grade selection for particular applications is given in Section 3.6.

3.1.2 Relevant standards

Flat and long products

The relevant standard is EN 10088, *Stainless steels*. It comprises three parts:

- Part 1, *Lists of stainless steels*, gives the chemical compositions and reference data on some physical properties such as modulus of elasticity, $E$.

- Part 2, *Technical delivery conditions for sheet, plate and strip of corrosion resisting steels for general purposes*, gives the technical properties and chemical compositions for the materials used in forming structural sections.

- Part 3, *Technical delivery conditions for semi-finished products, bars, rods, wire, sections and bright products of corrosion resisting steels for general purposes*, gives the technical properties and chemical compositions for the materials used in long products.

Parts 4 (flat products) and 5 (long products) of EN 10088 are now in preparation to cover material for construction purposes. They are likely to be published in 2007.

The designation systems adopted in EN 10088 are the European steel number and a steel name.

For example, grade 304L has a steel number 1.4307, where:

1. 43 07

Denotes steel Denotes one group of stainless steels Individual grade identification

The steel name system provides some understanding of the steel composition. The name of the steel number 1.4307 is X2CrNi18-9, where:

X 2 CrNi 18-9

Denotes high alloy steel 100 x % of carbon Chemical symbols of main alloying elements % of main alloying elements

Each stainless steel name has a unique corresponding steel number. Appendix A gives a table showing the designations for equivalent grades of stainless steel in various national and European standards.

Table 3.1 gives minimum specified mechanical properties of common stainless steels to EN 10088-2. The chemical compositions of these grades are given in Table 3.2.
Both austenitic and duplex stainless steels can be assumed to be adequately tough and not susceptible to brittle fracture for service temperatures down to $-40^\circ C$.

Design values of the mechanical properties are addressed in Section 3.2.4.

### Table 3.1 Specified mechanical properties of common stainless steels to EN 10088-2

<table>
<thead>
<tr>
<th>Grade</th>
<th>Product form$^{(1)}$</th>
<th>Max thickness (mm)</th>
<th>Minimum 0.2% proof strength$^{(2)}$ (N/mm²)</th>
<th>Ultimate tensile strength (N/mm²)</th>
<th>Elongation after fracture (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>C</td>
<td>8</td>
<td>230</td>
<td>540 – 750</td>
<td>45$^{(3)}$</td>
</tr>
<tr>
<td>1.4301</td>
<td>H</td>
<td>13,5</td>
<td>210</td>
<td>520 – 720</td>
<td>45$^{(3)}$</td>
</tr>
<tr>
<td></td>
<td>P</td>
<td>75</td>
<td>210</td>
<td>520 – 720</td>
<td>45</td>
</tr>
<tr>
<td></td>
<td>C</td>
<td>8</td>
<td>220</td>
<td>520 – 700</td>
<td>45</td>
</tr>
<tr>
<td>1.4307</td>
<td>H</td>
<td>13,5</td>
<td>200</td>
<td>520 – 700</td>
<td>45</td>
</tr>
<tr>
<td></td>
<td>P</td>
<td>75</td>
<td>200</td>
<td>500 – 700</td>
<td>45</td>
</tr>
<tr>
<td></td>
<td>C</td>
<td>8</td>
<td>240</td>
<td>530 – 680</td>
<td>40</td>
</tr>
<tr>
<td>1.4401</td>
<td>H</td>
<td>13,5</td>
<td>220</td>
<td>530 – 680</td>
<td>40</td>
</tr>
<tr>
<td></td>
<td>P</td>
<td>75</td>
<td>220</td>
<td>520 – 670</td>
<td>45</td>
</tr>
<tr>
<td></td>
<td>C</td>
<td>8</td>
<td>240</td>
<td>530 – 680</td>
<td>40</td>
</tr>
<tr>
<td>1.4404</td>
<td>H</td>
<td>13,5</td>
<td>220</td>
<td>530 – 680</td>
<td>40</td>
</tr>
<tr>
<td></td>
<td>P</td>
<td>75</td>
<td>220</td>
<td>520 – 670</td>
<td>45</td>
</tr>
<tr>
<td></td>
<td>C</td>
<td>8</td>
<td>220</td>
<td>520 – 720</td>
<td>40</td>
</tr>
<tr>
<td>1.4541</td>
<td>H</td>
<td>13,5</td>
<td>200</td>
<td>520 – 720</td>
<td>40</td>
</tr>
<tr>
<td></td>
<td>P</td>
<td>75</td>
<td>200</td>
<td>500 – 700</td>
<td>40</td>
</tr>
<tr>
<td></td>
<td>C</td>
<td>8</td>
<td>240</td>
<td>540 – 690</td>
<td>40</td>
</tr>
<tr>
<td>1.4571</td>
<td>H</td>
<td>13,5</td>
<td>220</td>
<td>540 – 690</td>
<td>40</td>
</tr>
<tr>
<td></td>
<td>P</td>
<td>75</td>
<td>220</td>
<td>520 – 670</td>
<td>40</td>
</tr>
<tr>
<td></td>
<td>C</td>
<td>8</td>
<td>350</td>
<td>650 – 850</td>
<td>35</td>
</tr>
<tr>
<td>1.4318</td>
<td>H</td>
<td>13,5</td>
<td>330</td>
<td>650 – 850</td>
<td>35</td>
</tr>
<tr>
<td></td>
<td>P</td>
<td>75</td>
<td>330</td>
<td>630 – 830</td>
<td>45</td>
</tr>
<tr>
<td></td>
<td>C</td>
<td>8</td>
<td>450</td>
<td>650 – 850</td>
<td>20</td>
</tr>
<tr>
<td>1.4362</td>
<td>H</td>
<td>13,5</td>
<td>400</td>
<td>650 – 850</td>
<td>20</td>
</tr>
<tr>
<td></td>
<td>P</td>
<td>75</td>
<td>400</td>
<td>630 – 800</td>
<td>25</td>
</tr>
<tr>
<td></td>
<td>C</td>
<td>8</td>
<td>500</td>
<td>700 – 950</td>
<td>20</td>
</tr>
<tr>
<td>1.4462</td>
<td>H</td>
<td>13,5</td>
<td>460</td>
<td>700 – 950</td>
<td>25</td>
</tr>
<tr>
<td></td>
<td>P</td>
<td>75</td>
<td>460</td>
<td>640 – 840</td>
<td>25</td>
</tr>
</tbody>
</table>

**Notes:**
1. C = cold rolled strip, H = hot rolled strip, P = hot rolled plate
2. Transverse properties
3. For stretcher levelled material, the minimum value is 5% lower
Table 3.2  Chemical composition to EN 10088-2

<table>
<thead>
<tr>
<th>Grade</th>
<th>Content of alloying element (maximum or range permitted) weight %</th>
<th>C</th>
<th>Cr</th>
<th>Ni</th>
<th>Mo</th>
<th>Others</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.4301</td>
<td></td>
<td>0.07</td>
<td>17.5 – 19.5</td>
<td>8.0 – 10.5</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1.4307</td>
<td></td>
<td>0.03</td>
<td>17.5 – 19.5</td>
<td>8.0 – 10.5</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1.4401</td>
<td></td>
<td>0.07</td>
<td>16.5 – 18.5</td>
<td>10.0 – 13.0</td>
<td>2.0 – 2.5</td>
<td></td>
</tr>
<tr>
<td>1.4404</td>
<td></td>
<td>0.03</td>
<td>16.5 – 18.5</td>
<td>10.0 – 13.0</td>
<td>2.0 – 2.5</td>
<td></td>
</tr>
<tr>
<td>1.4541</td>
<td></td>
<td>0.08</td>
<td>17.0 – 19.0</td>
<td>9.0 – 12.0</td>
<td>Ti: 5xC – 0.7 (1)</td>
<td></td>
</tr>
<tr>
<td>1.4571</td>
<td></td>
<td>0.08</td>
<td>16.5 – 18.5</td>
<td>10.5 – 13.5</td>
<td>2.0 – 2.5</td>
<td>Ti: 5xC – 0.7 (1)</td>
</tr>
<tr>
<td>1.4318</td>
<td></td>
<td>0.03</td>
<td>16.5 – 18.5</td>
<td>6.0 – 8.0</td>
<td>N: 0.1 – 0.2</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Austenitic steels</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Duplex steels</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1.4362</td>
<td></td>
<td>0.03</td>
<td>22.0 – 24.0</td>
<td>3.5 – 5.5</td>
<td>0.1 – 0.6</td>
<td>N: 0.05 – 0.2</td>
</tr>
<tr>
<td>1.4462</td>
<td></td>
<td>0.03</td>
<td>21.0 – 23.0</td>
<td>4.5 – 6.5</td>
<td>2.5 – 3.5</td>
<td>N: 0.1 – 0.22</td>
</tr>
</tbody>
</table>

Note:
(1) Titanium is added to stabilise carbon and improve corrosion performance in the heat affected zones of welds. However, except for very heavy section construction, the use of titanium stabilised austenitic steels has been superseded largely by the ready availability of the low carbon grades, 1.4307 and 1.4404.

Bolts

Stainless steel bolts are covered by EN ISO 3506, Corrosion-resistant stainless steel fasteners. The specification gives chemical compositions and mechanical properties for fasteners in the austenitic, martensitic and ferritic groups. Alternative materials not specifically covered in the specification are permitted if they meet the physical and mechanical property requirements and have equivalent corrosion resistance.

In EN ISO 3506, bolt and nut materials are classified by a letter: “A” for austenitic, “F” for ferritic and “C” for martensitic. It is recommended that austenitic bolts are used, for which the properties are as given in Tables 3.3 and 3.4 (taken from EN ISO 3506). The letter is followed by a number (1, 2, 3 4 or 5) which reflects the corrosion resistance; 1 representing the least durable and 5 the most durable.

Steel grade A1 is specially designed for machining. Due to high sulfur content, the steels within this grade have lower resistance to corrosion than corresponding steels with normal sulfur content. Care should be exercised if Grade A1 bolts are being considered, see Section 3.6.1.

Steels of grade A2 have equivalent corrosion resistance to grade 1.4301. Steels of grade A3 are stabilised stainless steels with equivalent corrosion resistance to grade 1.4541. (A stabilised steel is one which contains an addition of a strong carbide-forming agent such as titanium, which reacts preferentially with carbon and prevents formation of chromium carbides.)

Steels of grade A4 contain molybdenum and have equivalent corrosion resistance to grade 1.4401. Steels of grade A5 are stabilised molybdenum-bearing stainless steels with properties of grade 1.4571 steel.
Austenitic bolts can be obtained in three ultimate strength levels (known as property classes), see Table 3.3. Note that values must be agreed for bolts larger than M39 for property class 50 and M24 for property classes 70 and 80 as the values depend on the alloy and manufacturing method.

Bolts manufactured to property class 50 will be non-magnetic, but those to property classes 70 and 80 may demonstrate some magnetic properties.

The condition of the alloy in property class 50 bolts is soft, resulting in the highest corrosion resistance. Property classes 70 and 80 are cold worked and this can affect corrosion resistance slightly. Property class 50 bolts having machined threads may be more prone to thread galling, see Section 10.5.

Consideration should be given to matching the strength and corrosion resistance of the bolts and parent material.

EN 14399 gives rules for the CE marking of bolts.

Table 3.3 Minimum specified mechanical properties of austenitic grade bolts and nuts to EN ISO 3506

<table>
<thead>
<tr>
<th>Grade(1)</th>
<th>Property class</th>
<th>Thread diameter range</th>
<th>Ultimate tensile strength(2) (N/mm²)</th>
<th>Stress at 0.2% permanent strain (N/mm²)</th>
<th>Proof load stress (N/mm²)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A1, A2, A3, A4 and A5</td>
<td>50</td>
<td>≤ M39</td>
<td>500</td>
<td>210</td>
<td>500</td>
</tr>
<tr>
<td></td>
<td>70</td>
<td>≤ M24(3)</td>
<td>700</td>
<td>450</td>
<td>700</td>
</tr>
<tr>
<td></td>
<td>80</td>
<td>≤ M24(3)</td>
<td>800</td>
<td>600</td>
<td>800</td>
</tr>
</tbody>
</table>

Notes:
(1) In addition to the various steel types covered in EN ISO 3506 under property class 50, 70 and 80, other steel types to EN 10088-3 may also be used.
(2) The tensile stress is calculated on the stress area.
(3) For fasteners with nominal thread diameters d>24 mm, the mechanical properties shall be agreed upon between user and manufacturer and marked with grade and property class according to this table.
Table 3.4  Chemical composition of bolts to EN ISO 3506

<table>
<thead>
<tr>
<th>Grade</th>
<th>Chemical composition (percentage weight) (1)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>C</td>
</tr>
<tr>
<td>A1</td>
<td>0,12</td>
</tr>
<tr>
<td>A2</td>
<td>0,1</td>
</tr>
<tr>
<td>A3</td>
<td>0,08</td>
</tr>
<tr>
<td>A4</td>
<td>0,08</td>
</tr>
<tr>
<td>A5</td>
<td>0,08</td>
</tr>
</tbody>
</table>

Note:
(1) Values are maxima unless indicated otherwise
(2) Molybdenum may be present at the discretion of the manufacturer

3.2  Mechanical behaviour and design values of properties

3.2.1  Basic stress-strain behaviour

The stress-strain behaviour of stainless steels differs from that of carbon steels in a number of respects. The most important difference is in the shape of the stress-strain curve. Whereas carbon steel typically exhibits linear elastic behaviour up to the yield stress and a plateau before strain hardening is encountered, stainless steel has a more rounded response with no well-defined yield stress (see Figure 3.1). Therefore, stainless steel “yield” strengths are generally quoted in terms of a proof strength defined for a particular offset permanent strain (conventionally the 0,2% strain), as indicated in the Figure 3.1.

Note that Figure 3.1 shows typical experimental stress-strain curves. The curves shown are representative of the range of material likely to be supplied and should not be used in design.

Stainless steels can absorb considerable impact without fracturing due to their excellent ductility (especially the austenitic grades) and their strain hardening characteristics.
Factors affecting stress-strain behaviour

There are factors that can change the form of the basic stress-strain curve for any given grade of stainless steel. These factors are to some extent interdependent and include:

**Cold working**

Strength levels of austenitic and duplex grades are enhanced by cold working (such as imparted during cold forming operations including roller levelling/flattening and also during fabrication). Associated with this enhancement is a reduction in ductility but this normally is of slight consequence due to the initial high values of ductility, especially for the austenitic stainless steels.

Table 3.5 gives the cold worked levels specified in EN 1993-1-4 which are taken from the European material standard for stainless steel, EN 10088. Cold worked steels may be specified either in terms of minimum 0,2% proof strength or ultimate tensile strength or hardness, but only one parameter can be specified.

As stainless steel is cold worked, it tends to exhibit non-symmetry of tensile and compressive behaviour and anisotropy (different stress-strain characteristics parallel and transverse to the rolling directions). The degree of asymmetry and anisotropy depends on the grade, level of cold working and manufacturing route. Figure 3.2 shows stress-strain curves for grade 1.4318 cold worked to C850; the compression strength in the longitudinal direction lies below the tensile strength in both the transverse and longitudinal direction (the values traditionally given in material standards such as EN 10088 and reported accordingly by suppliers). Care is therefore needed in the choice of design strength for cold worked material (see Section 3.2.4). Additional information about values related to other types or directions of loading should be sought from the supplier.
The price of cold worked stainless steel is slightly higher than the equivalent annealed material, depending on the grade, product form and level of cold working.

### Table 3.5  
**Cold worked strength levels in EN 10088-2**  
*(applicable to material of thickness \( \leq 6 \) mm)*

<table>
<thead>
<tr>
<th>Cold worked condition</th>
<th>Minimum 0,2% proof strength(^1) (^2)</th>
<th>Minimum tensile strength(^1) (^2)</th>
<th>Available steel grades in the cold worked condition</th>
</tr>
</thead>
<tbody>
<tr>
<td>CP350</td>
<td>350</td>
<td>700 (^3)</td>
<td>1.4301, 1.4541, 1.4401, 1.4571</td>
</tr>
<tr>
<td>CP500</td>
<td>500</td>
<td>850 (^3)</td>
<td>1.4301, 1.4541, 1.4401, 1.4571, 1.4318</td>
</tr>
<tr>
<td>CP700</td>
<td>700</td>
<td>1000 (^3)</td>
<td>1.4318, 1.4301</td>
</tr>
<tr>
<td>C700</td>
<td>350 (^3)</td>
<td>700</td>
<td>1.4301, 1.4541, 1.4401, 1.4571</td>
</tr>
<tr>
<td>C850</td>
<td>500 (^3)</td>
<td>850</td>
<td>1.4301, 1.4541, 1.4401, 1.4571, 1.4318</td>
</tr>
<tr>
<td>C1000</td>
<td>700 (^3)</td>
<td>1000</td>
<td>1.4318, 1.4301</td>
</tr>
</tbody>
</table>

**Note:**

1. Intermediate 0,2% proof strength or tensile strength values may be agreed.
2. Maximum product thickness for each strength level decreases with strength. Maximum product thickness and remaining elongation are also dependent on the work hardening behaviour of the steel and the cold working conditions - more exact information may be requested from the manufacturer.
3. Not specified, indicative minimum values.

---

During the fabrication of a section, a 0,2% proof strength enhancement by a factor of about 50% is typical in cold formed corners of cross sections. However, the effect is localised and the increase in member resistance is dependent on the location of the corners within the section; e.g. in a beam, little benefit would be obtained for corners close to the neutral axis. The strength enhancement easily compensates for any effect due to thinning of the material at cold worked corners. If advantage is to be made of localised increased strength arising from fabrication, this should be proved by testing (see Section 9).
Subsequent welding of the member will have a partial annealing effect with a consequential reduction in any enhanced strength properties arising from cold working - Section 6.4.4 gives guidance on the design of welded connections between members from cold worked material.

**Strain-rate sensitivity**

Strain-rate sensitivity is more pronounced in stainless steels than in carbon steels. That is, a proportionally greater strength can be realised at fast strain rates for stainless steel than for carbon steel.

**Heat treatment**

Annealing, or softening, reduces the strength enhancement and the anisotropy.

### 3.2.3 Typical values of properties

It should be apparent from Sections 3.2.1 and 3.2.2 above that more factors are involved when considering the mechanical properties of stainless steels than for carbon steels. Their metallurgy is more complex and the manufacturing process has a higher impact on their final properties. For any given grade it is to be expected that there will be differences in properties for materials made by different manufacturers. However, the mechanical properties, being dependent on chemical composition and thermo-mechanical treatment, are therefore largely under the control of the manufacturers and it is possible to negotiate desired properties with individual manufacturers.

From a structural point of view, the margin by which the actual 0.2% proof stress exceeds the minimum specified value is significant. Typical mean proof stresses lie between 20 and 35% above the specified minima. The proportions of enhancement observed for proof stresses are not shared by ultimate tensile strength values, which typically are only about 10% above specified minima.

### 3.2.4 Design values of properties

**Flat products**

Three options may be considered: minimum specified values, verified material test data or mill certificate data.

(i) Design using minimum specified values

*Annealed material*

Take the characteristic yield strength, $f_y$, and the characteristic ultimate tensile strength, $f_u$, as the minimum values specified in EN 10088-2 (given in Table 3.1).

*Cold worked material*

Increased nominal values of $f_y$ and $f_u$ may be adopted for material delivered in the cold worked conditions specified in EN 10088.

For material delivered to a specified 0.2% proof strength (e.g. CP350), the minimum 0.2% proof strength in Table 3.5 may be taken as the characteristic strength. To take into account asymmetry of the cold worked material in those cases where compression in the longitudinal direction is a relevant stress condition (i.e. column behaviour or bending), the characteristic value should be taken as $0.8 \times 0.2\%$ proof strength in
Table 3.5. A higher value may be used if supported by appropriate experimental data.

For material delivered to a specified tensile strength (e.g. C700), the minimum tensile strength in Table 3.5 may be taken as the characteristic strength; the minimum 0.2% proof strength should be obtained from the supplier.

Note 1: Rectangular hollow sections are available in material cold worked to intermediate strengths between CP350 and CP500 with the yield and ultimate tensile strength guaranteed by the producer (the yield strength being valid in tension and compression).

Note 2: The design rules in this Design Manual are applicable for material up to grade CP500 and C850. For higher cold worked strength levels, design should be by testing according to Section 9. An exception is members with Class 1, 2 and 3 cross-sections which are not subject to local or global instability, for which the cross-section resistance may be calculated according to Section 4.

(ii) Design using test data

This should only be considered as an option where tensile testing has been carried out on coupons cut from the plate or sheet from which the members are to be formed or fabricated. The designer should also be satisfied that the tests have been carried out to a recognised standard, e.g. EN 10002-1, and that the procedures adopted by the fabricator are such that the member will be actually made from the tested material and positioned correctly within the structure.

A value for the design strength can be derived from a statistical approach carried out in accordance with the recommendations in Annex D of EN 1990.

It is recommended that the characteristic ultimate tensile strength, $f_u$, should still be based on the specified minimum value given in EN 10088-2.

(iii) Design using mill certificate data

Measured values of the 0.2% proof stress are given on the mill (or release) certificate. A value for the design strength can be derived from a statistical approach carried out in accordance with the recommendations in Annex D of EN 1990.

It is recommended that the characteristic ultimate tensile strength, $f_u$, should still be based on the specified minimum value given in EN 10088-2.

A value of 200 000 N/mm$^2$ is given by EN 10088-1 for Young’s modulus for all the standard austenitic and duplex grades typically used in structural applications. For estimating deflections, the secant modulus is more appropriate, see Section 5.4.6. For these grades, a value of 0.3 can be taken for Poisson’s ratio and 76 900 N/mm$^2$ for the shear modulus, $G$.

**Bolts**

For calculating the resistance of a bolt under tension or shear or combined tension and shear, take the basic strength $f_{ub}$ as:
$f_{ub} = \sigma_{ub}$

where $\sigma_{ub}$ is the specified minimum ultimate tensile strength given in Table 3.3 for the appropriate property class.

When it is necessary to consider the long term resistance of a bolt, reference should be made to EN 1990 for the appropriate combination of actions at the Ultimate Limit State.

### 3.3 Physical properties

Table 3.6 gives the room temperature physical properties in the annealed condition of the range of EN 10088 grades covered in this Design Manual. Physical properties may vary slightly with product form and size but such variations are usually not of critical importance to the application.

<table>
<thead>
<tr>
<th>Grade</th>
<th>Density (kg/m³)</th>
<th>Thermal expansion $20 - 100^\circ$C ($10^{-6}$/°C)</th>
<th>Thermal conductivity (W/m°C)</th>
<th>Heat capacity (J/kg°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.4301</td>
<td>7900</td>
<td>16</td>
<td>15</td>
<td>500</td>
</tr>
<tr>
<td>1.4307</td>
<td>7900</td>
<td>16</td>
<td>15</td>
<td>500</td>
</tr>
<tr>
<td>1.4401</td>
<td>8000</td>
<td>16</td>
<td>15</td>
<td>500</td>
</tr>
<tr>
<td>1.4404</td>
<td>8000</td>
<td>16</td>
<td>15</td>
<td>500</td>
</tr>
<tr>
<td>1.4541</td>
<td>7900</td>
<td>16</td>
<td>15</td>
<td>500</td>
</tr>
<tr>
<td>1.4571</td>
<td>8000</td>
<td>16,5</td>
<td>15</td>
<td>500</td>
</tr>
<tr>
<td>1.4318</td>
<td>7900</td>
<td>16</td>
<td>15</td>
<td>500</td>
</tr>
<tr>
<td>1.4362</td>
<td>7800</td>
<td>13</td>
<td>15</td>
<td>500</td>
</tr>
<tr>
<td>1.4462</td>
<td>7800</td>
<td>13</td>
<td>15</td>
<td>500</td>
</tr>
</tbody>
</table>

From a structural point of view, the most important physical property is the coefficient of linear expansion which, for the austenitic grades, differs considerably from that for carbon steel ($12 \times 10^{-6}$/°C). Where carbon and stainless steel are used together, the effects of differential thermal expansion should be considered in design.

Duplex and ferritic grades are magnetic. Where the non-magnetic properties of the austenitic grades are important to the application, care must be exercised in selecting appropriate welding consumables to minimise the ferrite content in the weldment. Heavy cold working, particularly of the lean alloyed austenitic steel, can also increase magnetic permeability; subsequent annealing would restore the non-magnetic properties. For non-magnetic applications, it is recommended that further advice be obtained from a steel producer.

### 3.4 Effects of temperature

Austenitic grades are used for cryogenic applications. At the other end of the temperature scale, austenitic and duplex grades retain a higher proportion of their strength above about 550°C than carbon steel. However, the design of structures subject to long term exposure at cryogenic temperatures or to long...
term exposure at high temperatures is outside the scope of this Design Manual. Suffice it to say that other mechanical properties and types of corrosion than those considered in this Section 3 take on a greater significance. Other stainless steels than those selected here are in most cases better suited for high temperature applications and further advice should be sought.

Duplex steels should not be used for long periods at temperatures above about 300°C, due to the possibility of embrittlement.

Section 7 covers fire resistant design and gives mechanical and physical properties at high temperatures.

### 3.5 Life cycle costing

There is increasing awareness that life cycle (or whole life) costs, not just initial costs, should be considered when selecting materials. Life cycle costs take account of:

- initial costs,
- operating costs,
- residual value.

Stainless steel is sometimes considered to be an expensive material. However, experience has shown that using a corrosion resistant material in order to avoid future maintenance, downtime and replacement costs can save costs which far outweigh higher initial material costs.

The initial cost of a structural stainless steel product is considerably higher than that of an equivalent carbon steel product, depending on the grade of stainless steel. However, savings will arise from the omission of surface coatings at regular (repeated) intervals in time.

The excellent corrosion resistance of stainless steel can offer many benefits including:

- reduced inspection frequency and costs,
- reduced maintenance costs,
- long service life.

Stainless steel has a high residual value (i.e. value at the end of a structure’s life), though this is rarely a deciding factor for a structure with a long projected life (for instance over 50 years).

Life cycle costing uses the standard accountancy principle of discounted cash flow to reduce all those costs to present day values. The discount rate encompasses inflation, bank interest rates, taxes and, possibly, a risk factor. This allows a realistic comparison to be made of the options available and the potential long term benefits of using stainless steel to be assessed against other material selections.
3.6 Selection of materials

3.6.1 Grades

In the great majority of structural applications utilising stainless steel, it is the metal’s corrosion resistance, which is being exploited, whether this be for reasons of aesthetics, minimal maintenance or long-term durability. Corrosion resistance must therefore be the primary factor in choosing a suitable grade.

Stainless steels derive their corrosion resistance from the presence of a passive surface film which, given adequate access to oxygen or suitable oxidising agents, tends to be self-healing when damaged. This oxide film is primarily a consequence of the chromium content of the steel, though the addition of nickel and other alloying elements can substantially enhance the protection offered by the film. In particular, a small percentage of molybdenum is used to improve the pitting resistance of the steel (see Section 3.7.2).

It is when the surface oxide film is damaged, possibly by electro-chemical attack or by mechanical damage, that corrosion might initiate.

Careful design should ensure trouble-free performance, but designers should be aware that even stainless steels may be subject to various forms of corrosion under certain circumstances. Notwithstanding the existence of these degradation effects, it is perfectly possible to employ stainless steels extremely effectively, provided that a few elementary principles are kept in mind. It is only when these materials are used without consideration for the principles behind their corrosion properties that problems might be encountered.

The selection of the correct grade of stainless steel must take into account the environment of the application, the fabrication route, surface finish and the maintenance of the structure. It might be noted that the maintenance requirement is minimal: merely washing down the stainless steel, even naturally by rain, will markedly assist in extending the service life.

The first step is to characterise the service environment, including reasonably anticipated deviations from the design conditions. In categorising atmospheric environments, special attention should be given to highly localised conditions such as proximity to chimneys venting corrosive fumes. Possible future developments or change of use should also be considered. The surface condition and the temperature of the steel, and the anticipated stress, could also be important parameters (see Section 3.7.2).

Candidate grades can then be chosen to give overall satisfactory corrosion resistance in the environment. The selection of a candidate steel should consider which possible forms of corrosion might be significant in the operating environment. To do this requires some appreciation of the nature of corrosion found in stainless steels. Section 3.7 outlines the broad principles underlying the corrosion of stainless steels, and indicates conditions where use of stainless steels should be free of undue risk and complication. It is also intended to illustrate general points of good practice, as well as the circumstances where stainless steels might have to be used with caution. In these latter conditions specialist advice should be sought, for in many cases the steels can still be successfully used.

Consideration should then be given to mechanical properties, ease of fabrication, availability of product forms, surface finish and costs.
Assessing the suitability of grades is best approached by referring to experience of stainless steels in similar applications and environments. Table 3.7 gives guidance for selecting suitable grades for atmospheric environments. National regulations should also be checked, since in some cases they may be more onerous. In the case of immersed stainless steel, see Section 3.7.3. When stainless steel comes into contact with chemicals, expert advice should always be sought.

Caution should be exercised when considering the use of free-machining stainless steels for fasteners. The addition of sulfur in the composition of these steels in the austenitic class renders them more liable to corrosion, especially in industrial and marine environments. In particular, this applies to fasteners in EN ISO 3506 grade A1 materials, see Table 3.3.

**Table 3.7 Suggested grades for atmospheric applications**

<table>
<thead>
<tr>
<th>Steel grade</th>
<th>Location</th>
<th>Rural</th>
<th>Urban</th>
<th>Industrial</th>
<th>Marine</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>L M H</td>
<td>L M H</td>
<td>L M H</td>
<td>L M H</td>
</tr>
<tr>
<td>Basic chromium-nickel austenitic steels (e.g. 1.4301, 1.4307, 1.4541, 1.4318)</td>
<td></td>
<td>✓ ✓ ✓</td>
<td>✓ ✓ ✓</td>
<td>✓ ✓ ✓</td>
<td>X ✓ X</td>
</tr>
<tr>
<td>Molybdenum-chromium-nickel austenitic steels (e.g. 1.4401, 1.4404, 1.4571) and duplex 1.4362</td>
<td>0 0 0</td>
<td>0 ✓ ✓</td>
<td>✓ ✓ ✓</td>
<td>✓ ✓ ✓</td>
<td>✓ ✓ ✓</td>
</tr>
<tr>
<td>Duplex steel grade 1.4462</td>
<td>0 0 0</td>
<td>0 0 0</td>
<td>0 ✓ ✓</td>
<td>0 ✓ ✓</td>
<td>0 ✓ ✓</td>
</tr>
</tbody>
</table>

L Least corrosive conditions within that category, e.g. tempered by low humidity, low temperatures.

M Fairly typical of that category.

H Corrosion likely to be higher than typical for that category, e.g. increased by persistent high humidity, high ambient temperatures, and particularly aggressive air pollutants.

O Potentially over-specified from a corrosion point of view.

✓ Probably the best choice for corrosion resistance and cost.

X Likely to suffer excessive corrosion.

✓✓ Worthy of consideration if precautions are taken (i.e. specifying a relatively smooth surface and if regular washing is carried out).

NOTE: National regulations may contain more onerous requirements.

### 3.6.2 Availability of product forms

**General types of product form**

Sheet, plate and bar products are all widely available in the grades of stainless steel considered in this Design Manual. Tubular products are available in austenitic grades and also the duplex grade 1.4462 (2205). Tubular products in the duplex grade 1.4362 (2304) are not widely available as this is a relatively new grade to the construction industry, although it has been used for some years for offshore blast walls.

There is a range of rolled sections (angles, channels, tees, rectangular hollow sections and I-sections) in standard austenitic grades such as 1.4301 and 1.4401 but none for duplex grades. Generally, sections may be produced by cold forming (rolling or bending), or fabricated by welding.
Material in the cold worked condition is available in various product forms including plate, sheet, coil, strip, bars and hollow sections:

- plate, sheet, coil, strip (in thicknesses typically ≤ 6.0 mm)
- round bar (diameters from 5 mm to 60 mm)
- square and rectangular hollow sections (cross-section dimensions up to 400 mm, thicknesses from 1.2 to 6 mm).

The grades of stainless steel which are commercially available in the cold worked condition are given in Table 3.5.

**Cold forming**

It is important that early discussion with potential fabricators takes place to ascertain cold forming limits as stainless steels require higher forming loads than carbon steels. The length of brake-pressed cold formed sections is necessarily limited by the size of machine or by power capability in the case of thicker or stronger materials. Duplex grades require approximately twice the forming loads used for the austenitic materials and consequently the possible range of duplex sections is more limited. Furthermore, because of the lower ductility in the duplex material, more generous bending radii should be used. Further information may be found in Section 10.3.2.

**Surface finish**

In certain applications, surface finish and appearance are important. Manufacturers offer a range of standard finishes, from mill finish through dull finishes to bright polish. They may also offer proprietary textured finishes. It should be noted that although the various finishes are standardised, variability in processing introduces differences in appearance between manufacturers and even from a single producer. Bright finishes are frequently used in architectural applications and it should be noted that bright finishes will exaggerate any out-of-flatness of the material, particularly on panel surfaces. Rigidised, embossed, textured, patterned or profiled sheets with a rigid supporting frame will alleviate this tendency.

**Bolts**

Bolts to EN ISO 3506 property class 70 are the most widely available. Certain size and length restrictions apply to bolts in property classes 70 and 80, see Table 3.3. It is possible to have “specials” made to order and indeed, this sometimes produces an economical solution.

Bolts can be produced by a number of techniques, e.g. machining, cold forming and forging. Machined threads should not be used in very aggressive environments (e.g. marine), due to potential problems with crevice corrosion. Rolled threads are also to be preferred because they are generally stronger than machined threads and provide greater resistance to thread galling.

### 3.7 Durability

#### 3.7.1 Introduction

Stainless steels are generally very corrosion resistant and will perform satisfactorily in most environments. The limit of corrosion resistance of a given stainless steel depends on its constituent elements, which means that each grade has a slightly different response when exposed to a corrosive environment.
Care is therefore needed to select the most appropriate grade of stainless steel for a given application. Generally, the higher the level of corrosion resistance required, the greater the cost of the material. For example, grade 1.4401 steel costs more than grade 1.4301 because of the addition of molybdenum.

Material in the cold worked condition has a similar corrosion resistance to that in the annealed condition.

The most common reasons for a metal to fail to live up to expectations regarding corrosion resistance are:

(a) incorrect assessment of the environment or exposure to unexpected conditions, e.g. unsuspected contamination by chloride ions

(b) the way in which the stainless steel has been worked or treated may introduce a state not envisaged in the initial assessment.

Although stainless steel may be subject to discolouration and staining (often due to carbon steel contamination), it is extremely durable in buildings. In aggressive industrial and marine environments, tests have shown no indication of reduction in component capacity even where a small amount of weight loss occurred. However, the user may still regard unsightly rust staining on external surfaces as a failure. As well as careful material grade selection, good detailing and workmanship can significantly reduce the likelihood of staining and corrosion; practical guidance is given in Section 10. Experience indicates that any serious corrosion problem is most likely to show up in the first two or three years of service.

In certain aggressive environments, some grades of stainless steel will be susceptible to localised attack. Six mechanisms are described below although the last three are very rarely encountered in buildings onshore.

It should be emphasised that the presence of moisture (including that due to condensation) is necessary for corrosion to occur.

3.7.2 Types of corrosion and performance of steel grades

**Pitting corrosion**

As the name implies, pitting takes the form of localised pits. It occurs as a result of local breakdown of the passive layer, normally by chloride ions although the other halides and other anions can have a similar effect. In a developing pit, corrosion products may create a very corrosive solution, often leading to high corrosion rates. In most structural applications, the extent of pitting is likely to be superficial and the reduction in section of a component is negligible. However, corrosion products can stain architectural features. A less tolerant view of pitting should be adopted for services such as ducts, piping and containment structures.

Since the chloride ion is by far the most common cause of pitting, coastal and marine environments are rather aggressive. The probability of a certain medium causing pitting depends on, besides the chloride content, factors such as the temperature, acidity or alkalinity and the content of oxidising agents. The pitting resistance of a stainless steel is dependent on its chemical composition. Chromium, molybdenum and nitrogen all enhance the resistance to pitting.

An approximate measure of pitting resistance is given by the Pitting Index or Pitting Resistance Equivalent (PRE) defined as:
PRE = % wt Cr + 3,3(% wt Mo) + 30(% wt N) for austenitic grades

PRE = % wt Cr + 3,3(% wt Mo) + 16(% wt N) for duplex grades

The PRE of a stainless steel is a useful guide to its ranking with other stainless steels, but has no absolute significance.

Grade 1.4301 has the lowest PRE of the grades covered in this Design Manual and hence is the most unsuitable grade for architectural applications in marine environments except, perhaps, for internal structural components effectively shielded from sea spray and mist. Grade 1.4301 may also show unacceptable levels of pitting in severe industrial atmospheres and therefore grade 1.4401 or a duplex grade is to be preferred.

**Crevice corrosion**

Crevice corrosion occurs in the same environments as pitting corrosion. Corrosion initiates more easily in a crevice than on a free surface because the diffusion of oxidants necessary for maintaining the passive film is restricted. The severity of a crevice is very dependent on its geometry: the narrower and deeper the crevice, the more severe the corrosion conditions. It is only likely to be a problem in stagnant solutions where a build up of chlorides can occur.

Crevices may result from a metal to metal joint, a gasket, biofouling, deposits and surface damage such as deep scratches. Every effort should be made to eliminate crevices, but it is often not possible to eliminate them entirely.

As in pitting corrosion, the alloying elements chromium, molybdenum and nitrogen enhance the resistance to attack and thus the resistance to crevice corrosion increases from grade 1.4301 through 1.4401 to 1.4462.

**Bimetallic (galvanic) corrosion**

When two dissimilar metals are in electrical contact and are also bridged by an electrolyte (i.e. an electrically conducting liquid such as sea water or impure fresh water), a current flows from the anodic metal to the cathodic or nobler metal through the electrolyte. As a result the less noble metal corrodes.

This form of corrosion is particularly relevant when considering joining stainless steel and carbon or low alloy steels. It is important to select welding consumables that are at least as noble as the parent material. In corrosive environments where water may be present such as heavy industrial environments, marine atmospheres, and where immersion in brackish or sea water may occur, martensitic and ferritic bolts (see Section 3.1.2) should be avoided for joining austenitic stainless steels.

Bimetallic corrosion need not be a problem with stainless steels, though sometimes its prevention can require precautions which at first sight might seem surprising. The prevention of bimetallic corrosion, in principle, is to prevent current flow by:

- insulating dissimilar metals, i.e. breaking the metallic path (see Section 6.1.1).
- preventing electrolyte bridging, i.e. breaking the electrolytic path by paint or other coating. Where protection is sought by this means and it is impracticable to coat both metals, then it is preferable to coat the more
noble one (i.e. stainless steel in the case of a stainless/carbon steel connection).

The risk of a deep corrosion attack is greatest if the area of the more noble metal (i.e. stainless steel) is large compared with the area of the less noble metal (i.e. carbon steel). Special attention should be paid to the use of paints or other coatings on the carbon steel. If there are any small pores or pinholes in the coating, the small area of bare carbon steel will provide a very large cathode/anode area ratio, and severe pitting of the carbon steel may occur. This is, of course, likely to be most severe under immersed conditions. For this reason it is preferable to paint the stainless steel; any pores will lead to small area ratios.

Adverse area ratios are likely to occur with fasteners and at joints. Carbon steel bolts in stainless steel members should be avoided because the ratio of the area of the stainless steel to the carbon steel is large and the bolts will be subject to aggressive attack. Conversely, the rate of attack of a carbon steel member by a stainless steel bolt is much slower. It is usually helpful to draw on previous experience in similar sites because dissimilar metals can often be safely coupled under conditions of occasional condensation or dampness with no adverse effects, especially when the conductivity of the electrolyte is low.

The prediction of these effects is difficult because the corrosion rate is determined by a number of complex issues. The use of electrical potential tables ignores the presence of surface oxide films and the effects of area ratios and different solution (electrolyte) chemistry. Therefore, uninformed use of these tables may produce erroneous results. They should be used with care and only for initial assessment.

Stainless steels usually form the cathode in a bimetallic couple and therefore do not suffer corrosion. Contact between austenitic stainless steels and zinc or aluminium may result in some additional corrosion of the latter two metals. This is unlikely to be significant structurally, but the resulting white/grey powder may be deemed unsightly. The couple with copper should generally be avoided except under benign conditions.

The general behaviour of metals in bimetallic contact in rural, urban, industrial and coastal environments is fully documented in BS PD 6484 Commentary on corrosion at bimetallic contacts and its alleviation.

**Stress corrosion cracking**

The development of stress corrosion cracking (SCC) requires the simultaneous presence of tensile stresses and specific environmental factors unlikely to be encountered in normal building atmospheres. The stresses do not need to be very high in relation to the proof stress of the material and may be due to loading, residual effects from manufacturing processes such as welding or bending. Duplex stainless steels usually have superior resistance to stress corrosion cracking than the austenitic stainless steels covered in this Design Manual. Higher alloy austenitic stainless steels such as grades 1.4539, 1.4529, 1.4547 and 1.4565 (not covered in this Design Manual) have been developed for applications where SCC is a corrosion hazard.

Caution should be exercised when stainless steel members containing high residual stresses (e.g. due to cold working) are used in chloride rich environments (e.g. indoor swimming pools, marine, offshore). EN 1993-1-4
advises that for load-bearing members in atmospheres containing chlorides that cannot be cleaned regularly (e.g. in suspended ceilings above swimming pools), only grades 1.4529, 1.4547, 1.4565 should be used, unless the concentration of chloride ions in the pool water is (unusually) \( \leq 250 \text{ mg/l} \), in which case grade 1.4539 is also suitable. Alternative grades which have been shown to have equivalent resistance to stress corrosion cracking in these atmospheres may also be used.

**General (uniform) corrosion**

Under normal conditions typically encountered in structural applications, stainless steels do not suffer from the general loss of section that is characteristic of rusting in non-alloyed irons and steels.

Stainless steel is resistant to many chemicals; indeed it is sometimes used for their containment. However, reference should be made to tables in manufacturers’ literature, or the advice of a competent corrosion engineer should be sought, if the stainless steel is to come into contact with chemicals.

**Intergranular corrosion (sensitisation) and weld decay**

When austenitic stainless steels are subject to prolonged heating in the range 450\(^\circ\)C to 850\(^\circ\)C, the carbon in the steel diffuses to the grain boundaries and precipitates chromium carbide. This removes chromium from the solid solution and leaves a lower chromium content adjacent to the grain boundaries. Steel in this condition is termed *sensitized*. The grain boundaries become prone to preferential attack on subsequent exposure to a corrosive environment. This phenomenon is known as *weld decay* when it occurs in the heat affected zone of a weldment.

There are three ways to avoid intergranular corrosion:

- use steel having a low carbon content
- use steel stabilised with titanium or niobium, because these elements combine preferentially with carbon to form stable particles, thereby reducing the risk of forming chromium carbide
- use heat treatment, however this method is rarely used in practice.

Grades of stainless steel with a low carbon content (0.03% maximum) up to 20 mm thick should not suffer from intergranular corrosion after arc welding.

### 3.7.3 Corrosion in selected environments

**Air**

Atmospheric environments vary, as do their effect on stainless steels. Rural atmospheres, uncontaminated by industrial fumes or coastal salt, are very mild in terms of corrosivity, even in areas of high humidity. Industrial and marine atmospheres are considerably more severe. Table 3.7 should be referred to for guidance on selecting suitable types of stainless steel.

The most common causes of atmospheric corrosion are metallic iron particles, arising from fabrication operations either in the workshop or at site, and chlorides originating from the sea, industrial processes or from calcium chloride used to make cement. Some deposited particles, although inert, are able to absorb weak acid solutions of sulfur dioxide from the atmosphere which may locally break down the passive film.
General appearance of exposed stainless steel is affected by surface finish (the smoother the better) and whether or not regular washing down is carried out (either intentionally or by rain).

**Sea water**

Sea water, including brackish water, contains high levels of chloride and hence is very corrosive, particularly when the water current is low (under about 1.5 m/s). At low current flows, severe pitting of grades 1.4301 and 1.4401 can occur. Also, these grades can suffer attack at crevices, whether these result from design details or from fouling organisms such as barnacles.

Salt spray may cause as much attack as complete immersion because the chloride concentration is raised by the evaporation of water or because of salt crystal deposits.

The possibility of severe bimetallic corrosion must be considered if stainless steel is used with other metals in the presence of sea water.

**Other waters**

Austenitic stainless steels usually perform satisfactorily in distilled, tap and boiler waters. Where acidity is high, grade 1.4401 is to be preferred, otherwise 1.4301 will usually suffice. Grade 1.4401 is also suggested as being more suitable where there are minor amounts of chloride present to avoid possible pitting and crevice corrosion problems. River water needs special consideration; biological and microbiological activity can cause pitting in austenitic stainless steels within a comparatively short time.

The possibility of erosion-corrosion should be considered for waters containing abrasive particles.

**Chemical environments**

The range of application of stainless steel in chemical environments is wide and it is not appropriate here to cover this subject in detail. It should be noted, however, that in many applications steels other than those considered in this Design Manual may be more suitable. The advice of a specialist corrosion engineer should be sought.

Charts published by manufacturers showing results of corrosion tests in various chemicals require careful interpretation. Although giving a guide to the resistance of a particular grade, service conditions (temperatures, pressures, concentrations, etc.) vary and will generally differ from the test conditions. Also, the effect of impurities and the degree of aeration can have a marked effect on results.

**Soils**

External corrosion of buried stainless steel is dependent on soil chemistry and resistivity. Soils differ in their corrosiveness depending on moisture level, pH, aeration, presence of chemical contamination, microbiological activity and surface drainage. Stainless steels generally perform well in a variety of soils and especially well in soils with high resistivity, although some pitting has occurred in low resistivity, moist soils. The presence of aggressive chemical species such as chloride ions as well as types of bacteria and stray current (caused by local direct current electric transportation systems such as railways or tram systems) can cause localized corrosion. The development of stray
current can be suppressed with a proper electrical insulation of the pipe (coatings or wrappings) and/or cathodic protection.

For grade selection purposes, it is recommended to consider the corrosion resistance of buried stainless steel firstly in relation to the presence of chloride ions and secondly according to the soil resistivity and pH, assuming poorly drained soils in all cases. Table 3.8 recommends suitable grades for different soil conditions.

**Table 3.8 Stainless steel grades for use in different soil conditions**

<table>
<thead>
<tr>
<th>Typical location</th>
<th>Soil condition</th>
<th>Grade of stainless steel</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inland</td>
<td>Cl &lt; 500 ppm</td>
<td>1.4301</td>
</tr>
<tr>
<td></td>
<td>Resistivity &gt;1000 ohm.cm</td>
<td>1.4404</td>
</tr>
<tr>
<td></td>
<td>pH &gt; 4.5</td>
<td></td>
</tr>
<tr>
<td>Marine – non-tidal zone</td>
<td>Cl &lt; 1500 ppm</td>
<td>1.4404</td>
</tr>
<tr>
<td></td>
<td>Resistivity &gt;1000 ohm.cm</td>
<td></td>
</tr>
<tr>
<td></td>
<td>pH &gt; 4.5</td>
<td></td>
</tr>
<tr>
<td>Marine – tidal zone</td>
<td>Cl &lt; 6000 ppm</td>
<td>1.4410</td>
</tr>
<tr>
<td></td>
<td>Resistivity &gt;500 ohm.cm</td>
<td>1.4547</td>
</tr>
<tr>
<td></td>
<td>pH &gt; 4.5</td>
<td></td>
</tr>
</tbody>
</table>

**Note:**
1.4410 is a duplex grade and 1.4547 is a super-austenitic grade. These grades are not generally used in construction applications and fall outside the scope of this Design Manual.

**Design for corrosion control**

The most important step in preventing corrosion problems is selecting an appropriate grade of stainless steel with suitable fabrication procedures for the given environment. However, after specifying a particular steel, much can be achieved in realising the full potential of the steel’s resistance by careful attention to detailing. Anti-corrosion actions should ideally be considered at the planning stage and during detailed design.

Table 3.9 gives a check list for consideration. Not all points would give the best detail from a structural strength point of view and neither are the points intended to be applied to all environments. In particular, in environments of low corrosivity or where regular maintenance is carried out, many would not be required. Figure 3.3 illustrates poor and good design features for durability.
Table 3.9  *Design for corrosion control*

<table>
<thead>
<tr>
<th>Avoid dirt entrapment</th>
</tr>
</thead>
<tbody>
<tr>
<td>• orientate angle and channel profiles to minimise the likelihood of dirt retention</td>
</tr>
<tr>
<td>• provide drainage holes, ensuring they are of sufficient size to prevent blockage</td>
</tr>
<tr>
<td>• avoid horizontal surfaces</td>
</tr>
<tr>
<td>• specify a small slope on gusset stiffeners which nominally lie in a horizontal plane</td>
</tr>
<tr>
<td>• use tubular and bar sections (seal tubes with dry gas or air where there is a risk of harmful condensates forming)</td>
</tr>
<tr>
<td>• specify smooth finishes.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Avoid crevices</th>
</tr>
</thead>
<tbody>
<tr>
<td>• use welded rather than bolted connections</td>
</tr>
<tr>
<td>• use closing welds or mastic fillers</td>
</tr>
<tr>
<td>• Preferably, dress/profile welds</td>
</tr>
<tr>
<td>• prevent biofouling.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Reduce the likelihood of stress corrosion cracking in those specific environments where it may occur (see Section 3.7.2):</th>
</tr>
</thead>
<tbody>
<tr>
<td>• minimise fabrication stresses by careful choice of welding sequence</td>
</tr>
<tr>
<td>• shot peen (but avoid the use of iron/steel shot).</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Reduce likelihood of pitting (see Section 10):</th>
</tr>
</thead>
<tbody>
<tr>
<td>• remove weld spatter</td>
</tr>
<tr>
<td>• pickle stainless steel to remove unwanted welding products. Strongly oxidising chloride-containing reagents such as ferric chloride should be avoided; rather a pickling bath or a pickling paste, both containing a mixture of nitric acid and hydrofluoric acid, should be used. Welds should always be cleaned up to restore corrosion resistance.</td>
</tr>
<tr>
<td>• avoid pick-up of carbon steel particles (e.g. use workshop area and tools dedicated to stainless steel)</td>
</tr>
<tr>
<td>• follow a suitable maintenance programme.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Reduce likelihood of bimetallic corrosion (see Section 3.7.2):</th>
</tr>
</thead>
<tbody>
<tr>
<td>• provide electrical insulation</td>
</tr>
<tr>
<td>• use paints appropriately</td>
</tr>
<tr>
<td>• minimise periods of wetness</td>
</tr>
<tr>
<td>• use metals that are close to each other in electrical potential.</td>
</tr>
</tbody>
</table>
Figure 3.3 Poor and good design features for durability
4 PROPERTIES OF SECTIONS

4.1 General
The recommendations in Sections 4 and 5 apply to cross-sections with elements complying with the dimensional limits of Section 4.2.

The width-to-thickness ratios of elements that are partly or wholly in compression determine whether they are subject to local buckling, with a consequential reduction in the resistance of the cross-section. Elements and cross-sections are classified as Class 1, 2, 3 or 4 depending on the susceptibility to local buckling and their rotation capacity (Class 1 and 2), see Section 4.3.

The reduced resistance of Class 4 cross-sections may be allowed for in design by the use of effective widths of elements, see Section 4.4.1.

Mid-line dimensions may only be used for calculating section properties of cold-formed members and sheeting. For other sections, the overall dimensions should be used. EN 1993-1-3 and EN 1993-1-5 permit mid-line dimensions to be used in calculating resistances. EN 1993-1-1 also allows the use of mid-line dimensions in calculating resistances in certain cases (see 6.2.1(9) but also 6.2.5(2) of EN 1993-1-1).

4.2 Maximum width-to-thickness ratios
Table 4.1 gives maximum width-to-thickness ratios for stainless steel elements.

4.3 Classification of cross-sections
4.3.1 General
In principle, stainless steel cross-sections may be classified in the same way as those of carbon steel. Four classes of cross-section are defined as follows:

Class 1 cross-sections are those which can form a plastic hinge with the rotation capacity required from plastic analysis.

Class 2 cross-sections are those which can develop their plastic moment resistance, but have limited rotation capacity.

Class 3 cross-sections are those in which the calculated stress in the extreme compression fibre of the steel member can reach its yield strength, but local buckling is liable to prevent development of the plastic moment resistance.

Class 4 cross-sections are those in which local buckling will occur before the attainment of yield stress in one or more parts of the cross-section.
Table 4.1  Maximum width-to-thickness ratios

<table>
<thead>
<tr>
<th>a) Flat element or intermediately stiffened element connected to a web along one edge with the other edge unsupported:</th>
<th>b/t ≤ 50</th>
</tr>
</thead>
<tbody>
<tr>
<td>b) Flat element or intermediately stiffened element connected to a web along one edge and provided with a small simple lip along the other edge</td>
<td>b/t ≤ 60  c/t ≤ 50</td>
</tr>
<tr>
<td>c) Flat element or intermediately stiffened element connected along both edges to webs or flanges:</td>
<td>b/t ≤ 400  h/t ≤ 400</td>
</tr>
</tbody>
</table>

Note: Flat elements supported as in a) above with b/t ratios greater than approximately 30 and flat elements supported otherwise with b/t ratios greater than approximately 75 are likely to develop visual distortion at serviceability design loads.

The classification of a cross-section depends on the highest (least favourable) class of its constituent parts that are partially or wholly in compression. It should be noted that the cross-section classification can vary according to the proportion of moment or axial load present and thus can vary along the length of a member.

4.3.2 Classification limits for parts of cross-sections

Sections are classified as Class 1, 2, or 3 depending on the limits set out in Table 4.2. Those sections which do not meet the criteria for Class 3 sections are classified as Class 4.
### Table 4.2  Maximum width-to-thickness ratios for compression parts

#### Internal compression parts

![Diagram of compression parts]

<table>
<thead>
<tr>
<th>Class</th>
<th>Part subject to bending</th>
<th>Part subject to compression</th>
<th>Part subject to bending and compression</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>(c / t \leq 56,0 \varepsilon)</td>
<td>(c / t \leq 25,7 \varepsilon)</td>
<td>when (\alpha &gt; 0,5): (c / t \leq 308 \varepsilon / (13 \alpha - 1)) when (\alpha \leq 0,5): (c / t \leq 28 \varepsilon / \alpha)</td>
</tr>
<tr>
<td>2</td>
<td>(c / t \leq 58,2 \varepsilon)</td>
<td>(c / t \leq 26,7 \varepsilon)</td>
<td>when (\alpha &gt; 0,5): (c / t \leq 320 \varepsilon / (13 \alpha - 1)) when (\alpha \leq 0,5): (c / t \leq 29,1 \varepsilon / \alpha)</td>
</tr>
<tr>
<td>3</td>
<td>(c / t \leq 74,8 \varepsilon)</td>
<td>(c / t \leq 30,7 \varepsilon)</td>
<td>(c / t \leq 15,3 \varepsilon \sqrt{k_\alpha}) for (k_\alpha) see 4.4.1</td>
</tr>
</tbody>
</table>

\[
\varepsilon = \left[ \frac{235}{f_y} \cdot \frac{E}{210 \, 000} \right]^{0.5}
\]

<table>
<thead>
<tr>
<th>Grade</th>
<th>1.4301</th>
<th>1.4401</th>
<th>1.4462</th>
</tr>
</thead>
<tbody>
<tr>
<td>(f_y) (N/mm²)</td>
<td>210</td>
<td>220</td>
<td>460</td>
</tr>
<tr>
<td>(\varepsilon)</td>
<td>1.03</td>
<td>1.01</td>
<td>0.698</td>
</tr>
</tbody>
</table>

**Notes:**

For hollow sections, \(c\) may conservatively be taken as \((b-2t)\) or \((h-2t)\)

\[E = 200 \, 000 \text{ N/mm}^2\]

\[
\alpha = \frac{1}{2} \left(1 + \frac{N_{Ed}}{f_y c \sum t_w} \right)\text{ for sections which are symmetrical about the major axis}\]
Table 4.2 (continued) Maximum width-to-thickness ratios for compression parts

<table>
<thead>
<tr>
<th>Class</th>
<th>Type of section</th>
<th>Part subject to compression</th>
<th>Part subject to bending and compression</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Tip in compression</td>
<td>Tip in tension</td>
</tr>
<tr>
<td>1</td>
<td>Cold formed</td>
<td>$c/t \leq 10,0\varepsilon$</td>
<td>$c/t \leq \frac{10\varepsilon}{\alpha}$</td>
</tr>
<tr>
<td></td>
<td>Welded</td>
<td>$c/t \leq 9,0\varepsilon$</td>
<td>$c/t \leq \frac{9\varepsilon}{\alpha}$</td>
</tr>
<tr>
<td>2</td>
<td>Cold formed</td>
<td>$c/t \leq 10,4\varepsilon$</td>
<td>$c/t \leq \frac{10,4\varepsilon}{\alpha}$</td>
</tr>
<tr>
<td></td>
<td>Welded</td>
<td>$c/t \leq 9,4\varepsilon$</td>
<td>$c/t \leq \frac{9,4\varepsilon}{\alpha}$</td>
</tr>
<tr>
<td>3</td>
<td>Cold formed</td>
<td>$c/t \leq 11,9\varepsilon$</td>
<td>$c/t \leq 18,1\varepsilon \sqrt{k_\sigma}$ For $k_\sigma$ see 4.4.1.</td>
</tr>
<tr>
<td></td>
<td>Welded</td>
<td>$c/t \leq 11,0\varepsilon$</td>
<td>$c/t \leq 16,7\varepsilon \sqrt{k_\sigma}$ For $k_\sigma$ see 4.4.1.</td>
</tr>
</tbody>
</table>

Angles

Refer also to Outstand flanges

Does not apply to angles in continuous contact with other components

Class | Section in compression |
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>$h/t \leq 11,9 \varepsilon$ ; $(b + h)/2t \leq 9,1 \varepsilon$</td>
</tr>
</tbody>
</table>
Table 4.2 (continued) *Maximum width-to-thickness ratios for compression parts*

<table>
<thead>
<tr>
<th>Class</th>
<th>Section in bending</th>
<th>Section in compression</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>(d/t \leq 50\varepsilon^2)</td>
<td>(d/t \leq 50\varepsilon^2)</td>
</tr>
<tr>
<td>2</td>
<td>(d/t \leq 70\varepsilon^2)</td>
<td>(d/t \leq 70\varepsilon^2)</td>
</tr>
<tr>
<td>3</td>
<td>(d/t \leq 280\varepsilon^2)</td>
<td>(d/t \leq 90\varepsilon^2)</td>
</tr>
</tbody>
</table>

Note for 2: \(d/t > 280\varepsilon^2\) see EN 1993-1-6

Note for 3: \(d/t > 90\varepsilon^2\) see EN 1993-1-6

\[
\varepsilon = \left[ 235 \frac{E}{f_y} \right]^{0.5}
\]

<table>
<thead>
<tr>
<th>Grade</th>
<th>(1.4301)</th>
<th>(1.4401)</th>
<th>(1.4462)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(f_y) (N/mm²)</td>
<td>210</td>
<td>220</td>
<td>460</td>
</tr>
<tr>
<td>(\varepsilon)</td>
<td>1.03</td>
<td>1.01</td>
<td>0.698</td>
</tr>
</tbody>
</table>

Note: \(E = 200\ 000\ N/mm^2\)

4.4 Effective widths

4.4.1 Effective widths of elements in Class 4 cross-sections

The properties of Class 4 cross-sections may be established by calculation using the effective widths of the component parts in full or partial compression. Alternatively, testing may be utilised, see Section 9.

The effective area of a Class 4 cross-section in full or partial compression, \(A_{\text{eff}}\), is the gross area of the cross-section minus the sum of the ineffective areas of each slender element making up the cross-section. The effective area of each Class 4 element is the effective breadth \(b_{\text{eff}}\) calculated below multiplied by the element thickness. When the cross-section is subject to bending, an effective moment of inertia \(I_{\text{eff}}\) and effective section modulus \(W_{\text{eff}}\) also need to be calculated.

The effective widths of elements in full or partial compression may be obtained from Table 4.3 for internal elements, and from Table 4.4 for outstand elements.

The effective widths of flange elements in compression may be based on the stress ratio \(\psi\) determined for the gross cross-section (\(\psi\) is defined in Tables 4.3 and 4.4). The effective width of a web element should be based on the stress...
ratio $\psi$ determined for a cross-section comprising the effective area of the compression flange but the gross area of the web and tension flange.

The reduction factor $\rho$ may be calculated as follows:

Cold formed or welded internal elements:

$$\rho = \frac{0.772}{\lambda_p} - \frac{0.125}{\lambda_p^2} \quad \text{but } \leq 1 \quad (4.1a)$$

Cold formed outstand elements:

$$\rho = \frac{1}{\lambda_p} - \frac{0.231}{\lambda_p^2} \quad \text{but } \leq 1 \quad (4.1b)$$

Welded outstand elements:

$$\rho = \frac{1}{\lambda_p} - \frac{0.242}{\lambda_p^2} \quad \text{but } \leq 1 \quad (4.1c)$$

where $\lambda_p$ is the element slenderness defined as:

$$\lambda_p = \frac{\bar{b}/t}{28.4\epsilon\sqrt{k_\sigma}} \quad (4.2)$$

in which:

- $\epsilon$ is the material factor defined in Table 4.2.

Generally, the neutral axis of the effective section will shift by a dimension $e$ compared to the neutral axis of the gross section, see Figures 4.1 and 4.2. This should be taken into account when calculating the properties of the effective cross-section.

When the cross-section is subject to axial compression, the recommendations of Section 5.5.2 take account of the additional moment $\Delta M_{Ed}$ given by:

$$\Delta M_{Ed} = N_{Ed} e_N$$
where $e_N$ is the shift of the neutral axis when the cross-section is subject to uniform compression, see Figure 4.2.

### Table 4.3  *Internal compression elements*  

<table>
<thead>
<tr>
<th>Stress distribution (compression positive)</th>
<th>Effective width $b_{eff}$</th>
</tr>
</thead>
<tbody>
<tr>
<td><img src="image" alt="Diagram" /></td>
<td>$\psi = 1$:</td>
</tr>
<tr>
<td></td>
<td>$b_{eff} = \rho \bar{b}$</td>
</tr>
<tr>
<td></td>
<td>$b_{e1} = 0.5 b_{eff}$ \hspace{1cm} $b_{e2} = 0.5 b_{eff}$</td>
</tr>
<tr>
<td><img src="image" alt="Diagram" /></td>
<td>$1 &gt; \psi \geq 0$:</td>
</tr>
<tr>
<td></td>
<td>$b_{eff} = \rho \bar{b}$</td>
</tr>
<tr>
<td></td>
<td>$b_{e1} = \frac{2 b_{eff}}{5 - \psi}$ \hspace{1cm} $b_{e2} = b_{eff} - b_{e1}$</td>
</tr>
<tr>
<td><img src="image" alt="Diagram" /></td>
<td>$\psi &lt; 0$:</td>
</tr>
<tr>
<td></td>
<td>$b_{eff} = \rho b_c = \rho \bar{b} / (1 - \psi)$</td>
</tr>
<tr>
<td></td>
<td>$b_{e1} = 0.4 b_{eff}$ \hspace{1cm} $b_{e2} = 0.6 b_{eff}$</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>$\psi = \sigma_2 / \sigma_1$</th>
<th>1</th>
<th>$1 &gt; \psi &gt; 0$</th>
<th>0</th>
<th>$0 &gt; \psi &gt; -1$</th>
<th>-1</th>
<th>$-1 &gt; \psi &gt; -3$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Buckling factor $k_o$</td>
<td>4.0</td>
<td>8.2 / (1.05 + $\psi$)</td>
<td>7.81</td>
<td>$7.81 - 6.29 \psi + 9.78 \psi^2$</td>
<td>23.9</td>
<td>5.98 (1 - $\psi$)$^2$</td>
</tr>
</tbody>
</table>
### Table 4.4  Outstand compression elements

<table>
<thead>
<tr>
<th>Stress distribution (compression positive)</th>
<th>Effective width $b_{\text{eff}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td><img src="image1.png" alt="Diag1" /></td>
<td>$1 &gt; \psi \geq 0$: $b_{\text{eff}} = \rho c$</td>
</tr>
<tr>
<td><img src="image2.png" alt="Diag2" /></td>
<td>$\psi &lt; 0$: $b_{\text{eff}} = \rho b_c = \rho c / (1-\psi)$</td>
</tr>
<tr>
<td>$\psi = \sigma_2/\sigma_1$</td>
<td>$1$</td>
</tr>
<tr>
<td></td>
<td>$0$</td>
</tr>
<tr>
<td></td>
<td>$-1$</td>
</tr>
<tr>
<td></td>
<td>$+1\geq \psi \geq -3$</td>
</tr>
<tr>
<td>Buckling factor $k_o$</td>
<td>$0.43$</td>
</tr>
<tr>
<td></td>
<td>$0.57$</td>
</tr>
<tr>
<td></td>
<td>$0.85$</td>
</tr>
<tr>
<td></td>
<td>$0.57 - 0.21\psi + 0.07\psi^2$</td>
</tr>
<tr>
<td><img src="image3.png" alt="Diag3" /></td>
<td>$1 &gt; \psi &gt; 0$: $b_{\text{eff}} = \rho c$</td>
</tr>
<tr>
<td><img src="image4.png" alt="Diag4" /></td>
<td>$\psi &lt; 0$: $b_{\text{eff}} = \rho b_c = \rho c / (1-\psi)$</td>
</tr>
<tr>
<td>$\psi = \sigma_2/\sigma_1$</td>
<td>$1$</td>
</tr>
<tr>
<td></td>
<td>$1 &gt; \psi &gt; 0$</td>
</tr>
<tr>
<td></td>
<td>$0$</td>
</tr>
<tr>
<td></td>
<td>$0 &gt; \psi &gt; -1$</td>
</tr>
<tr>
<td></td>
<td>$-1$</td>
</tr>
<tr>
<td>Buckling factor $k_o$</td>
<td>$0.43$</td>
</tr>
<tr>
<td></td>
<td>$0.578 / (\psi + 0.34)$</td>
</tr>
<tr>
<td></td>
<td>$1.70$</td>
</tr>
<tr>
<td></td>
<td>$1.7 - 5\psi + 17.1\psi^2$</td>
</tr>
<tr>
<td></td>
<td>$23.8$</td>
</tr>
</tbody>
</table>
4.4.2 Effects of shear lag
Shear lag in flanges may be neglected if $b_0 < L_e/50$, where $b_0$ is taken as the flange outstand or half the width of an internal element and $L_e$ is the length between points of zero bending moment. Where this limit for $b_0$ is exceeded, the effects of shear lag in flanges should be considered; the guidance for carbon steel in EN 1993-1-5 is applicable. Note that EN 1993-1-5 requires that shear lag be taken into account at both the ultimate and the serviceability limit states.

4.4.3 Flange curling
The effect on the load bearing resistance of curling (i.e. inward curvature towards the neutral plane) of a very wide flange in a profile subjected to flexure, or of a flange in an arched profile subjected to flexure in which the concave side is in compression, should be taken into account unless such curling is less than 5% of the depth of the profile cross-section. If the curling is larger,
then the reduction in load bearing resistance, for instance due to a decrease in the length of the lever arm for parts of the wide flanges, and the possible effect of the bending of the webs should be taken into account.

Width-to-thickness ratios of flanges in typical stainless steel beams are unlikely to be susceptible to flange curling. Where required, the guidance for carbon steel in EN 1993-1-3 is applicable.

4.5 Stiffened elements
4.5.1 Edge stiffeners
The guidance for carbon steel in EN 1993-1-3 is applicable.

4.5.2 Intermediate stiffeners
The guidance for carbon steel in EN 1993-1-3 is applicable.

4.5.3 Trapezoidal sheeting profiles with intermediate flange stiffeners
The effective cross-section of a flange with intermediate stiffeners and subject to uniform compression should be assumed to consist of the reduced effective areas \( A_{s,red} \) including two strips of width \( 0.5b_{eff} \) or \( 15t \) adjacent to the stiffener, see Figure 4.3 and 4.4.

Figure 4.3  Compression flange with one, two or multiple stiffeners
Figure 4.4  *Intermediate stiffener*

For one central flange stiffener, the elastic critical buckling stress $\sigma_{cr,s}$ (used for determining $\lambda_d$) should be obtained from:

$$\sigma_{cr,s} = \frac{4.2k_wE}{A_s} \sqrt{\frac{I_s t^3}{4b_p^2(2b_p + 3b_s)}}$$  \hspace{1cm} (4.3)

where:

- $b_p$ is the notional flat width of the plane element shown in Figure 4.3, 4.4 and 4.5
- $b_s$ is the stiffener width, measured around the perimeter of the stiffener, see Figure 4.3, 4.4 and 4.5
- $A_s$ is the cross-sectional area of the stiffener cross-section according to Figure 4.3, 4.4 and 4.5
- $I_s$ is the second moment of area of the stiffener cross-section according to Figure 4.3, 4.4 and 4.5
- $k_w$ is a coefficient that allows for partial rotational restraint of the stiffened flange by the webs or other adjacent elements, see below. For the calculation of the effective cross-section in axial compression the value $k_w = 1.0$.

For two symmetrically placed flange stiffeners, the elastic critical buckling stress $\sigma_{cr,s}$ should be obtained from:

$$\sigma_{cr,s} = \frac{4.2k_wE}{A_s} \sqrt{\frac{I_s t^3}{8b_1^2(3b_e - 4b_1)}}$$ \hspace{1cm} (4.4)

in which:

$$b_e = 2b_{p,1} + b_{p,2} + 2b_s$$  \hspace{1cm} (4.5)

$$b_1 = b_{p,1} + 0.5b_r$$ \hspace{1cm} (4.6)

where:

- $b_{p,1}$ is the notional flat width of an outer plane element, as shown in Figure 4.4,
- $b_{p,2}$ is the notional flat width of the central plane element, as shown in Figure 4.4
- $b_r$ is the overall width of a stiffener, see Figure 4.3.
The value of $k_w$ may be calculated from the compression flange buckling wavelength $l_b$ as follows:

if $\frac{l_b}{s_w} \geq 2$, \[ k_w = k_{wo} \]

if $\frac{l_b}{s_w} < 2$, \[ k_w = k_{wo} - (k_{wo} - 1) \left[ \frac{2l_b}{s_w} - \left( \frac{l_b}{s_w} \right)^2 \right] \]

where:

$s_w$ is the slant height of the web, see Figure 4.5.

$\frac{l_b}{s_w} \geq 2 \quad (4.7)$

$\frac{l_b}{s_w} < 2 \quad (4.8)$

**Figure 4.5** Notional widths of plane elements $b_p$ allowing for corner radii

Alternatively, the rotational restraint coefficient $k_w$ may conservatively be taken as equal to 1.0 corresponding to a pin-jointed condition.

The values of $l_b$ and $k_{wo}$ may be determined from:
a) for a compression flange with one intermediate stiffener:

\[ l_b = 3.07 \sqrt[3]{\frac{I_b b_p^2 (2b_p + 3b_s)}{t^3}} \]  \hspace{1cm} (4.9)

\[ k_{wo} = \frac{s_w + 2b_d}{s_w + 0.5b_d} \] \hspace{1cm} (4.10)

with \( b_d = 2b_p + b_s \) \hspace{1cm} (4.11)

b) for a compression flange with two or three intermediate stiffeners:

\[ l_b = 3.65 \sqrt[3]{\frac{I_b b_p^2 (3b_c - 4b_l)}{t^3}} \] \hspace{1cm} (4.12)

\[ k_{wo} = \frac{(2b_c + s_w)(3b_c - 4b_l)}{b_l (4b_c - 6b_l) + s_w (3b_c - 4b_l)} \] \hspace{1cm} (4.13)

The reduced effective area of the stiffener \( A_{s,red} \) allowing for distortional buckling should be taken as:

\[ A_{s,red} = \chi_d A_s \frac{f_y}{\gamma_{MO}} \] but \( A_{s,red} \leq A_s \] \hspace{1cm} (4.14)

where:

\( \sigma_{\text{com,ser}} \) is the maximum compressive stress in the stiffener (calculated on the basis of the effective cross-section) under serviceability limit state loading.

If the webs are unstiffened, the reduction factor \( \chi_d \) should be obtained from the following:

if \( \bar{\lambda}_d \leq 0.65 \), \( \chi_d = 1.0 \) \hspace{1cm} (4.15)

if \( 0.65 < \bar{\lambda}_d < 1.38 \), \( \chi_d = 1.47 - 0.723 \bar{\lambda}_d \) \hspace{1cm} (4.16)

if \( \bar{\lambda}_d \geq 1.38 \), \( \chi_d = \frac{0.66}{\bar{\lambda}_d} \) \hspace{1cm} (4.17)

where \( \bar{\lambda}_d = \sqrt{f_y / \sigma_{cr,s}} \).

If the webs are also stiffened, reference should be made to EN 1993-1-3.

In determining effective section properties, the reduced effective area \( A_{s,red} \) should be represented by using a reduced thickness \( t_{red} = t A_{red} / A_s \) for all the elements included in \( A_s \).

### 4.6 Calculation of section properties

#### 4.6.1 General

The calculation of section properties should be carried out in accordance with normal good practice taking into account any reduction in the gross area due to
local buckling or holes as necessary. Thinning of material at cold formed corners can be neglected, because of the strength increase afforded by work hardening.

4.6.2 Influence of rounded corners

The influence of rounded corners on cross-section resistance may be neglected if the internal radius \( r \leq 5t \) and \( r \leq 0.10b_p \) and the cross-section may be assumed to consist of plane elements with sharp corners. For cross-section stiffness properties the influence of rounded corners should always be taken into account.

The influence of rounded corners on section properties may be taken into account with sufficient accuracy by reducing the properties calculated for an otherwise similar cross-section with sharp corners, see Figure 4.6, using the following approximations:

\[
A_g = A_{g,sh} (1 - \delta) \tag{4.18}
\]
\[
I_g = I_{g,sh} (1 - 2\delta) \tag{4.19}
\]
\[
I_w = I_{w,sh} (1 - 4\delta) \tag{4.20}
\]

in which:

\[
\delta = 0.43 \sum_{j=1}^{n} r_j \frac{\phi_j}{90} \sum_{i=1}^{m} b_{p,i} \tag{4.21}
\]

where:

- \( A_g \) is the area of the gross cross-section
- \( A_{g,sh} \) is the value of \( A_g \) for a cross-section with sharp corners
- \( b_{p,j} \) is the notional flat width of the plane element \( i \) for a cross-section with sharp corners
- \( I_g \) is the second moment of area of the gross cross-section
- \( I_{g,sh} \) is the value of \( I_g \) for a cross-section with sharp corners
- \( I_w \) is the warping constant of the gross cross-section
- \( I_{w,sh} \) is the value of \( I_w \) for a cross-section with sharp corners
- \( \phi_j \) is the angle between two plane elements
- \( m \) is the number of plane elements
- \( n \) is the number of curved elements
- \( r_j \) is the internal radius of curved element \( j \).

The reductions given above may also be applied in calculating the effective section properties \( A_{eff}, I_{y,eff}, I_{z,eff} \) and \( I_{w,eff} \), provided that the notional flat widths of the plane elements are measured to the points of intersection of their midlines.
4.6.3 Gross cross section

When calculating gross cross section properties, holes for fasteners need not be deducted but allowance should be made for larger openings.

4.6.4 Net section

The net area of a section or element of a section should be taken as its gross area less appropriate deductions for all openings, including holes for fasteners. In the deductions for fasteners, the nominal hole diameter should be used.

Provided that the fastener holes are not staggered, the total area to be deducted for fastener holes should be the maximum sum of the sectional areas of the holes in any cross-section perpendicular to the member axis (see failure plane (2) in Figure 4.7).

When the fastener holes are staggered, the total area to be deducted should be the greater of:

- the deduction for non-staggered holes
- \[ t \left( n d_0 - \sum \frac{s^2}{4p} \right) \]

where:

- \( s \) is the staggered pitch, the spacing of the centres of two consecutive holes in the chain measured parallel to the member axis
- \( p \) is the spacing of the centres of the same two holes measured perpendicular to the member axis
- \( t \) is the thickness
- \( n \) is the number of holes extending in any diagonal or zig-zag line progressively across the member or part of the member, see Figure 4.7
- \( d_0 \) is the diameter of the hole.

For sections such as angles with holes in both legs, the gauge should be measured along the centre of the thickness of the material, see Figure 4.8.

For angles connected by one leg, see Section 6.2.
4.7 Resistances of cross-sections

4.7.1 General

This Section relates to the resistance of cross-sections only; a check on possible buckling modes is also required to establish member resistance. Buckling of members is addressed in Section 5. The $\gamma_M$ factors used in this Section are given in Table 2.1.

The work-hardening associated with cold forming operations during fabrication (see Section 3.2.2) will generally increase the cross-sectional resistance but sufficient data are not yet available for stainless steel to enable design recommendations to be made. It is suggested that when the benefits of work-hardening are to be utilised, the cross-sectional resistance should be established by tests (see Section 9).

Under exceptional circumstances, it may be permissible to utilise the strain hardening material property of stainless steel in design, see Section 4.7.7.

4.7.2 Cross-sections subject to tension

The resistance of cross-sections subject to uniform tensile stresses only, $N_{t,Rd}$, may be taken as the smaller of:

a) the design plastic resistance of the gross cross-section

$$N_{pl,Rd} = \frac{A_g f_y}{\gamma_{M0}} \quad (4.22)$$

b) the design ultimate resistance of the net cross-section at holes for fasteners
\[ N_{u,Rd} = \frac{k_r \ A_{\text{net}} \ f_u}{\gamma M_2} \]  \hspace{1cm} (4.23)

where:

- \( A_g \) is the gross area
- \( A_{\text{net}} \) is the net cross-sectional area (see Section 4.6.4)
- \( f_y \) is the characteristic yield strength (generally taken as the minimum specified 0.2% proof strength, see Table 3.1)
- \( f_u \) is the characteristic ultimate tensile strength (generally taken as the minimum specified value, see Table 3.1)
- \( k_r = [1 + 3r(d_0/u - 0.3)] \) but \( k_r \leq 1.0 \)  \hspace{1cm} (4.24)
- \( r = [\text{number of bolts at the cross-section}] / [\text{total number of bolts in the connection}] \)
- \( d_0 \) is the nominal bolt hole diameter
- \( u = 2e_2 \) but \( u \leq p_2 \).

### 4.7.3 Cross-sections subject to compression

The resistance of a cross-section subject to compression, \( N_{c,Rd} \), with a resultant acting through the centroid of the gross section (for Class 1, 2 and 3 cross-sections) or the effective section (Class 4 cross-sections) may be taken as:

\[ N\_{c,Rd} = A_g f_y / \gamma M_0 \]  \hspace{1cm} (4.25)

\[ N\_{c,Rd} = A_{\text{eff}} f_y / \gamma M_0 \]  \hspace{1cm} (4.26)

**Note:** Class 4 sections which are not doubly symmetric should be assessed in accordance with 4.7.6 to account for the additional bending moment \( \Delta M_{Ed} \) due to the eccentricity of the centroidal axial of the effective sections, see Section 4.4.1.

### 4.7.4 Cross-sections subject to bending moment

In the absence of shear and axial forces, the design moment resistance of a cross-section subject to a uniaxial moment, \( M_{c,Rd} \), should be taken as:

\[ M\_{c,Rd} = W_{pl} f_y / \gamma M_0 \]  \hspace{1cm} (4.27)

\[ M\_{c,Rd} = W_{el,min} f_y / \gamma M_0 \]  \hspace{1cm} (4.28)

\[ M\_{c,Rd} = W_{eff,min} f_y / \gamma M_0 \]  \hspace{1cm} (4.29)

where:

- \( W_{pl} \) is the plastic section modulus
- \( W_{el,min} \) is the elastic section modulus corresponding to the fibre with the maximum elastic stress (but see Section 4.1 for cold formed cross-sections)
- \( W_{eff,min} \) is the elastic modulus of effective section corresponding to the fibre with the maximum elastic stress (but see Section 4.1 for cold formed cross-sections).
For cross-sections where bending is applied about both axes, see Section 4.7.6.

### 4.7.5 Cross-sections subject to shear

The plastic shear resistance of a cross-section, $V_{pl,Rd}$ may generally be taken as:

$$V_{pl,Rd} = A_v (f_y / \sqrt{3}) / \gamma_{M0}$$  \hspace{1cm} (4.30)

where:

- $A_v$ is the shear area, which may be taken as follows:
  - a) rolled I and H sections, load parallel to web
    $$A = 2bt_f + (t_w + 2r) t_f$$ but not less than $\eta h_w t_w$
  - b) rolled channel sections, load parallel to web
    $$A = 2bt_f + (t_w + r) t_f$$
  - c) rolled T-section, load parallel to web
    $$A = 0.9(A - bt_f)$$
  - d) welded I, H and box sections, load parallel to web
    $$\sum h_w t_w$$
  - e) welded I, H, channel and box section, load parallel to flanges
    $$A = \sum (h_w t_w)$$
  - f) rolled rectangular hollow sections of uniform thickness
    - i. load parallel to depth
      $$Ah / (b + h)$$
    - ii. load parallel to width
      $$Ab / (b + h)$$
  - g) circular hollow sections and tubes of uniform thickness
    $$2A / \pi$$

where:

- $A$ is the cross-sectional area
- $b$ is the overall breadth
- $h$ is the overall depth
- $h_w$ is the depth of the web
- $r$ is the root radius
- $t_f$ is the flange thickness
- $t_w$ is the web thickness (if the web thickness is not constant, $t_w$ should be taken as the minimum thickness).
- $\eta$ see EN 1993-1-5. (EN 1993-1-4 recommends $\eta = 1.20$.)

Note: The same value of $\eta$ should be used for calculating the shear buckling resistance as is used for calculating the plastic shear resistance.

The resistance to shear buckling should be also checked, see Section 5.4.3.

### 4.7.6 Cross-sections subject to combination of loads

When an axial force is present, allowance should be made for its effect on the plastic moment resistance. For Class 1 and 2 cross sections, the following criterion should be satisfied:
\[ M_{\text{Ed}} \leq M_{N,Rd} \]  \hspace{1cm} (4.31)

where:

\( M_{N,Rd} \) is the design plastic moment resistance reduced due to the axial force \( N_{\text{Ed}} \).

For doubly symmetrical I- and H-sections or other flange sections, allowance need not be made for the effect of the axial force on the plastic resistance moment about the y-y axis when both the following criteria are satisfied:

\[ N_{\text{Ed}} \leq 0.25 N_{\text{pl,Rd}} \quad \text{and} \quad N_{\text{Ed}} \leq 0.5 h_w t_w f_y / \gamma_{M0} \]  \hspace{1cm} (4.32a)

\[ N_{\text{Ed}} \leq 0.5 h_w t_w f_y / \gamma_{M0} \]  \hspace{1cm} (4.32b)

In the absence of shear force, for Class 3 and Class 4 cross-sections the maximum longitudinal stress should satisfy the criterion:

\[ \sigma_{x,\text{Ed}} \leq f_y / \gamma_{M0} \]  \hspace{1cm} (4.33)

where:

\( \sigma_{x,\text{Ed}} \) is the design value of the local longitudinal stress due to moment and axial force, taking account of fastener holes where relevant.

For Class 4 cross-sections, the following criterion should also be met:

\[ \frac{N_{\text{Ed}}}{A_{\text{eff}} f_y / \gamma_{M0}} + \frac{M_{y,\text{Ed}} + N_{\text{Ed}} e_{Ny}}{W_{\text{eff,y,min}} f_y / \gamma_{M0}} + \frac{M_{z,\text{Ed}} + N_{\text{Ed}} e_{Nz}}{W_{\text{eff,z,min}} f_y / \gamma_{M0}} \leq 1 \]  \hspace{1cm} (4.34)

where:

\( A_{\text{eff}} \) is the effective area of the cross-section when subjected to uniform compression

\( W_{\text{eff,min}} \) is the effective section modulus of the cross-section when subjected only to moment about the relevant axis

\( e_N \) is the shift of the relevant centroidal axis when the cross-section is subjected to compression only.

Note that for angles, the y and z axes in the above should be taken as the u and v axes respectively.

When \( V_{\text{Ed}} \) exceeds 50% of \( V_{\text{pl,Rd}} \), the design resistance of the cross-section to combinations of moment and axial force should be calculated using a reduced yield strength \((1 - \rho) f_y\) for the shear area, where \( \rho = (2V_{\text{Ed}}/ V_{\text{pl,Rd}} -1)^2 \).

### 4.7.7 Utilisation of strain hardening behaviour

In certain circumstances, such as beams under short term accidental loads, it is permissible to recognise the benefits of the strain hardening properties of stainless steel more fully in design.

This may be achieved by utilising an enhanced proof stress, \( \sigma_0 \), in place of the 0.2% proof stress \( f_y \) in all calculations. It is recommended that in the absence of a more detailed appraisal, perhaps involving non-linear finite element analysis, the following restrictions should be observed:
• The cross-section should be of Class 1 or Class 2 as calculated by using $\sigma_0$ in place of $f_y$ when calculating $\epsilon$ in Table 4.2.
• The cross-section is subject to major axis bending only.
• The member concerned is not subject to instability caused by any form of buckling (flexural, torsional, lateral-torsional or distortional - see Section 5), again using $\sigma_0$ in all calculations.
• Connections to adjacent members and the members themselves are sufficiently strong to realise the enhanced resistance of the member.

Particular attention should be given to assessing connection strength requirements.

For Class 3 and 4 cross-sections, enhanced strengths may be used provided these values are verified by testing in accordance with Section 9.
5 MEMBER DESIGN

5.1 Introduction
The design checks required for stainless steel members are similar to those required for carbon steel members. It is recommended that the forces and moments in the members are derived from an elastic global analysis.

In addition to the cross-sectional resistance, see Section 4, consideration should be given to overall buckling of members, as addressed in this section.

A possible design approach for checking against buckling in stainless steel members is to use the tangent modulus corresponding to the buckling stress instead of the initial modulus as used in carbon steel rules. Assuming similar levels of geometric and residual stress imperfections in carbon steel and stainless steel members, this generally leads to satisfactory results when it is based on validated carbon steel rules. This approach is therefore available to the designer. However, it requires iterative solution techniques and therefore has been avoided in this Design Manual except in some cases when it has been used to derive effective design curves for use with the initial modulus. Instead, emphasis has been given to calibrating against available experimental data.

The following subsections are intended for use with singly, doubly or point-symmetric uniform sections. The resistance of members not possessing any axis of symmetry should be verified by appropriate tests.

5.2 Tension members
Members subject to tension only do not suffer any instability due to buckling. Their design may therefore be based only on the cross-section resistance, see Section 4.7.2, and the resistance of their connections, see Section 6.

For an angle connected by one leg or other unsymmetrically connected members:

\[ N_{t,Rd} = N_{pl,Rd} \leq N_{u,Rd} \]  \hspace{1cm} (5.1)

where the terms are defined in Section 4.7.2 and \( N_{u,Rd} \) is determined from Section 6.2.3, Equations 6.6, 6.7 or 6.8.

5.3 Compression members
5.3.1 General
Members in compression are susceptible to a number of possible buckling modes including:

- Plate buckling (Class 4 sections only)
- Flexural buckling
- Torsional buckling
- Torsional-flexural buckling.
**Doubly symmetric cross-sections (CHS, RHS, I sections etc.)**

Doubly symmetric cross-sections need not be checked for torsional-flexural buckling, since the shear centre coincides with the centroid of the cross-section. However, torsional buckling may be critical.

Circular and square hollow sections will not fail by torsional buckling.

For the range of rectangular hollow section sizes typically used in construction, torsional buckling will not be critical. Torsional buckling in rectangular hollow sections need only be considered for rectangular hollow sections with unusually high $h/b$ ratios.

**Singly symmetric cross-sections (equal-leg angles, channels etc.)**

It is necessary to check sections such as single channels and equal-leg angles for torsional-flexural buckling as the shear centre does not coincide with the centroid of the cross-section.

**Point symmetric cross-sections (Z-sections, cruciform sections etc.)**

Torsional buckling may be the critical buckling mode for these sections.

5.3.2 **Plate buckling**

Plate buckling within Class 4 sections is taken into account by the use of an effective cross-section area. Note that the additional moment caused by the shift in neutral axis of the effective section from that of the gross section in asymmetric Class 4 cross-sections should be considered in accordance with Section 5.5.

5.3.3 **Flexural buckling**

The resistance to flexural buckling should be determined from:

\[ N_{b,y,Rd} = \chi A f_y / \gamma M_1 \]  

for Class 1, 2 and 3 cross-sections \hspace{1cm} (5.2a)

\[ N_{b,y,Rd} = \chi A_{eff} f_y / \gamma M_1 \]  

for Class 4 cross-sections \hspace{1cm} (5.2b)

where:

- $A_{eff}$ is the effective area of Class 4 cross-section
- $A$ is the gross area
- $\chi$ is the reduction factor accounting for buckling, given by:

\[ \chi = \frac{1}{\varphi + \left[ \varphi \alpha - \lambda \right]^{0.5}} \leq 1 \]  

(5.3)

in which:

\[ \varphi = 0.5 \left( 1 + \alpha (\lambda - \lambda_0) + \lambda^2 \right) \]  

(5.4)

\[ \bar{\lambda} = \sqrt{\frac{A f_y}{N_{cr}}} \frac{L_{cr}}{i} \frac{1}{\pi} \sqrt{\frac{f_y}{E}} \]  

for Class 1, 2 and 3 cross-sections \hspace{1cm} (5.5a)

\[ \bar{\lambda} = \sqrt{\frac{A_{eff} f_y}{N_{cr}}} \frac{L_{cr}}{i} \frac{1}{\pi} \sqrt{\frac{f_y A_{eff}}{E}} \]  

for Class 4 cross-sections \hspace{1cm} (5.5b)
where:
\[ \alpha \] is the imperfection factor defined in Table 5.1
\[ N_{cr} \] is the elastic critical force for the relevant buckling mode based on the gross cross sectional properties
\[ \lambda_0 \] is the limiting non-dimensional slenderness defined in Table 5.1
\[ L_{cr} \] is the buckling length in the buckling plane considered, determined taking into account the boundary conditions
\[ i \] is the radius of gyration about the relevant axis, determined using the properties of the gross cross section.

The buckling curves are shown in Figure 5.1. The values for \( \alpha \) and \( \lambda_0 \) in Table 5.1 do not apply to hollow sections which are annealed after fabrication. For non-dimensional slenderness \( \lambda \leq \lambda_0 \) or for \( \frac{N_{Ed}}{N_{cr}} \leq \lambda_0^2 \) the buckling effects may be ignored and only cross sectional checks apply.

![Buckling curves for flexural, torsional and torsional-flexural buckling](image)

**Figure 5.1**  *Buckling curves for flexural, torsional and torsional-flexural buckling*

The determination of the buckling length should be based upon structural mechanics principles, taking boundary conditions into account.
Table 5.1  Values of $\alpha$ and $\lambda_0$ for flexural, torsional and torsional-flexural buckling

<table>
<thead>
<tr>
<th>Buckling mode</th>
<th>Type of member</th>
<th>$\alpha$</th>
<th>$\lambda_0$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Flexural</td>
<td>Cold formed open sections</td>
<td>0.49</td>
<td>0.40</td>
</tr>
<tr>
<td></td>
<td>Hollow sections (welded and seamless)</td>
<td>0.49</td>
<td>0.40</td>
</tr>
<tr>
<td></td>
<td>Welded open sections (major axis)</td>
<td>0.49</td>
<td>0.20</td>
</tr>
<tr>
<td></td>
<td>Welded open sections (minor axis)</td>
<td>0.76</td>
<td>0.20</td>
</tr>
<tr>
<td>Torsional and torsional-flexural</td>
<td>All members</td>
<td>0.34</td>
<td>0.20</td>
</tr>
</tbody>
</table>

5.3.4  Torsional and torsional-flexural buckling

The resistance to these buckling modes should be determined according to Section 5.3.3 but substituting $\lambda$ by $\lambda_T$, as given by Equations 5.6 and 5.7, and taking $\alpha = 0.34$ and $\lambda_0 = 0.2$.

\[
\lambda_T = \sqrt{\frac{Af_y}{N_{cr}}} \quad \text{for Class 1, 2 and 3 cross-sections} \tag{5.6a}
\]

\[
\lambda_T = \sqrt{\frac{A_{eff} f_y}{N_{cr}}} \quad \text{for Class 4 cross-sections} \tag{5.6b}
\]
in which:

$N_{cr} = N_{cr,T}$ and $N_{cr} < N_{cr,T}$

where:

$N_{cr,T}$ is the elastic critical torsional buckling force

\[
N_{cr,T} = \frac{1}{l_o^2} \left( GI_t + \frac{\pi^2 E I_o}{l_f^2} \right) \tag{5.7a}
\]

$N_{cr,TF}$ is the elastic critical torsional-flexural buckling force.

For cross-sections that are symmetrical about the y-y axis (e.g. $z_o = 0$)

\[
N_{cr,TF} = \frac{N_{cr,y}}{2 \beta} \left[ 1 + \frac{N_{cr,T}}{N_{cr,y}} - \sqrt{\left( 1 - \frac{N_{cr,T}}{N_{cr,y}} \right)^2 + 4 \left( \frac{y_o}{l_o} \right)^2 \frac{N_{cr,T}}{N_{cr,y}}} \right] \tag{5.7b}
\]
in which:

\[
l_o^2 = l_y^2 + l_z^2 + y_o^2 + z_o^2
\]

$l_y$ and $l_z$ are the radii of gyration of the gross cross-section about the y and z axes respectively

$y_o$ and $z_o$ are the shear centre co-ordinates with respect to the centroid of the gross cross-section

$G$ is the shear modulus

$l_T$ is the buckling length of the member for torsional buckling (see EN 1993-1-3)
$I_T$ is the torsional constant of the gross cross-section

$I_W$ is the warping constant of the gross cross-section

$$\beta = 1 - \left( \frac{y_o}{i_o} \right)^2$$

$N_{cr,y}$ and $N_{cr,z}$ are the elastic critical axial force for flexural buckling about the y-y and z-z axes respectively.

For a doubly symmetric cross-section, the shear centre coincides with the centroid, therefore $y_o = 0$ and $z_o = 0$ and

$$N_{cr,TF} = N_{cr,T} \text{ provided } N_{cr,T} < N_{cr,y} \text{ and } N_{cr,T} < N_{cr,z} .$$

Note that for angles, the y and z axes in the above should be taken as the u and v axes respectively.

5.4 Flexural members

5.4.1 General

A member is in simple bending under loads acting normal to the longitudinal axis if it is connected in such a way as to eliminate twisting or tensile or compressive end loading.

The following criteria should be considered for establishing the moment resistance of a beam:

- Yielding of the cross-section (see Section 4.7)
- Plate buckling (Class 4 section only – see Section 4.7)
- Lateral-torsional buckling (see Section 5.4.2)
- Shear buckling (see Section 5.4.3)
- Local strength at points of loading or reaction (see Section 5.4.4).

Note that for flexural members, the effects of shear lag and flange curling may have to be accounted for in design, see Sections 4.4.2 and 4.4.3.

Biaxial bending should be treated as described in Section 5.5.2.

5.4.2 Lateral-torsional buckling

The possibility of lateral-torsional buckling may be discounted for the following classes of member:

- beams subject to bending only about the minor axis
- beams laterally restrained throughout their length by adequate bracing
- beams where the lateral non-dimensional slenderness parameter $\lambda_{LT}$ (see below) $\leq 0.4$ or for $\frac{M_{Ed}}{M_{cr}} \leq 0.16$.

For all other classes of member, the resistance to lateral torsional buckling should be determined from:
\( M_{b, Rd} = \chi_{LT} W_y f_y / \gamma_M \) \hspace{1cm} (5.8)

where:

- \( W_y = W_{pl,y} \) for Class 1 or 2 cross-sections
- \( W_y = W_{el,y} \) for Class 3 cross-sections
- \( W_y = W_{eff,y} \) for Class 4 cross-sections

\( \chi_{LT} \) is a reduction factor accounting for lateral torsional buckling, given by:

\[
\chi_{LT} = \frac{1}{\varphi_{LT} + \left( \varphi_{LT}^2 - \lambda_{LT}^2 \right)^{0.5}} \leq 1
\] \hspace{1cm} (5.9)

in which:

\[
\varphi_{LT} = 0.5 \left( 1 + \alpha_{LT} \left( \lambda_{LT} - 0.4 \right) + \lambda_{LT}^2 \right)
\] \hspace{1cm} (5.10)

\[
\lambda_{LT} = \frac{W_y f_y}{M_{cr}}
\] \hspace{1cm} (5.11)

\( \alpha_{LT} \) is the imperfection factor

- \( = 0.34 \) for cold formed sections and hollow sections (welded and seamless)
- \( = 0.76 \) for welded open sections and other sections for which no test data is available.

\( M_{cr} \) is the elastic critical moment for lateral torsional buckling (Appendix B).

Note that for angles, the \( y \) and \( z \) axes in the above should be taken as the \( u \) and \( v \) axes respectively.

The buckling curves for lateral torsional buckling are shown in Figure 5.2.
5.4.3 Shear resistance

The shear resistance is limited by either the plastic shear resistance (see Section 4.7.5) or the shear buckling resistance.

The shear buckling resistance only requires checking when $h_w / t \geq 52 \varepsilon / \eta$ for an unstiffened web or $h_w / t \geq 23 \varepsilon \sqrt{k_t / \eta}$ for a stiffened web.

The shear buckling resistance for a beam should be obtained from:

$$V_{b,Rd} = V_{bw,Rd} + V_{bf,Rd} \leq \frac{\eta f_{yw} h_w t}{\sqrt{3} \gamma_{M1}} \tag{5.12a}$$

in which the contribution from the web is given by:

$$V_{bw,Rd} = \frac{X_w f_{yw} h_w t}{\sqrt{3} \gamma_{M1}} \tag{5.12b}$$

where:

- $h_w$ is the clear web depth between flanges (Figure 5.3)
- $\varepsilon$ is defined in Table 4.2
- $k_t$ is the shear buckling coefficient
- $V_{bw,Rd}$ is the contribution to the shear buckling resistance from the web
- $V_{bf,Rd}$ is the contribution to the shear buckling resistance from the flanges
- $f_{yw}$ is the characteristic yield strength of web
- $\eta$ see EN 1993-1-5 (EN 1993-1-4 recommends $\eta = 1.20.$)

Figure 5.2 Buckling curves for lateral-torsional buckling
Note: The same value of $\eta$ should be used for calculating the plastic shear resistance as is used for calculating the shear buckling resistance.

\[ \chi_w = \eta \text{ for } \lambda_w \leq \frac{0.60}{\eta} \] (5.13a)

\[ \chi_w = 0.11 + \frac{0.64}{\lambda_w} - \frac{0.05}{\lambda_w^2} \text{ for } \lambda_w > \frac{0.60}{\eta} \] (5.13b)

For webs with transverse stiffeners at the supports only, the non-dimensional slenderness parameter $\lambda_w$ should be taken as:

\[ \lambda_w = \left( \frac{h_w}{86.4t_w} \right) \] (5.14)

For webs with transverse stiffeners at the supports and intermediate transverse and/or longitudinal stiffeners, $\lambda_w$ should be taken as:

\[ \lambda_w = \left( \frac{h_w}{37.4t_w} \sqrt{k_r} \right) \] (5.15)

in which $k_r$ is the minimum shear buckling coefficient for the web panel. For webs with rigid transverse stiffeners and without longitudinal stiffeners or with more than two longitudinal stiffeners, $k_r$ can be obtained as follows:

\[ k_r = 5.34 + 4.00(h_w / a)^2 + k_{rst} \text{ when } a / h_w \geq 1 \] (5.16a)

\[ k_r = 4.00 + 5.34(h_w / a)^2 + k_{rst} \text{ when } a / h_w < 1 \] (5.16b)

where:

\[ k_{rst} = 9(h_w / a)^2 \sqrt[3]{\frac{I_{sl}}{t^3 h_w}} \] but not less than $\frac{2t}{3 \sqrt{3} h_w}$

where:

\[ I_{sl} \]

Figure 5.3 Notation for geometrical dimensions
\[ a \] is the distance between centrelines of transverse stiffeners, see Figure 5.3.

\[ I_{sl} \] is the second moment of area of the longitudinal stiffener about the z-axis.

Equation 5.16 also applies to plates with one or two longitudinal stiffeners, if the aspect ratio \( a/h_w \geq 3 \). For plates with one or two longitudinal stiffeners and an aspect ratio \( a/h_w < 3 \), reference should be made to EN 1993-1-5 Annex A3.

For simplicity, the contribution from the flanges \( \chi_f \) may be neglected. However, if the flange resistance is not completely utilized in withstanding the bending moment \((M_{Ed} < M_{f,Rd})\) then the contribution from the flanges may be obtained as follows:

\[
V_{bf,Rd} = \frac{b_f t_f^2 f_{yt}}{c \gamma M1} \left[ 1 - \left( \frac{M_{Ed}}{M_{f,Rd}} \right)^2 \right] \tag{5.17}
\]

where:

- \( b_f \) and \( t_f \) are taken for the flange which provides the least axial resistance, \( b_f \) being taken as not larger than \( 15 \varepsilon t_f \) on each side of the web
- \( M_{f,Rd} \) is the moment of resistance of the cross section consisting of the area of the effective flanges only
- \( M_{f,Rd} = \frac{M_{f,k}}{\gamma M0} \)

\[
c = a \left( 0,17 + \frac{3,5b_f t_f^2 f_{yt}}{t_w h_w^2 f_{yw}} \right) \quad \text{and} \quad \frac{c}{a} \leq 0,65
\]

- \( f_{yt} \) is the characteristic yield strength of the flange.

If an axial force \( N_{Ed} \) is also applied, the value of \( M_{f,Rd} \) should be reduced by a factor:

\[
1 - \frac{N_{Ed}}{(A_{f1} + A_{f2}) f_{yt}} \quad \left( A_{f1} + A_{f2} \right) f_{yt} \tag{5.18}
\]

where \( A_{f1} \) and \( A_{f2} \) are the areas of the top and bottom flanges, respectively.

The verification should be performed as follows:

\[
\eta_3 = \frac{V_{Ed}}{V_{b,Rd}} \leq 1,0 \tag{5.19}
\]

where:

- \( V_{Ed} \) is the design shear force including shear from torque.
Member verification for biaxial bending and axial compression should be performed as follows:

\[
\eta = \frac{N_{Ed}}{f_y A_{eff} / \gamma_{M0}} + \frac{M_{y,Ed} e_{y,N}}{f_y W_{y,eff} / \gamma_{M0}} + \frac{M_{z,Ed} e_{z,N}}{f_y W_{z,eff} / \gamma_{M0}} \leq 1,0
\]  

(5.20)

where:

- \( A_{eff} \) is the effective cross-section area (Section 4.4.1)
- \( e_{y,N} \) is the shift in the position of the neutral axis with respect to the y axis (Section 4.4.1)
- \( e_{z,N} \) is the shift in the position of the neutral axis with respect to the z axis (Section 4.4.1)
- \( M_{y,Ed} \) is the design bending moment with respect to the y axis
- \( M_{z,Ed} \) is the design bending moment with respect to the z axis
- \( N_{Ed} \) is the design axial force
- \( W_{y,eff} \) is the effective section modulus with respect to the y axis (Section 4.4.1)
- \( W_{z,eff} \) is the effective section modulus with respect to the z axis (Section 4.4.1).

Action effects \( M_{Ed} \) and \( N_{Ed} \) should include global second order effects where relevant. The plate buckling verification of the panel should be carried out for the stress resultants at a distance 0.4a or 0.5b, whichever is the smallest, from the panel end where the stresses are the greater.

Provided that \( \overline{\eta}_3 \) (see below) does not exceed 0.5, the design resistance to bending moment and axial force need not be reduced to allow for the shear force. If \( \overline{\eta}_3 \) is more than 0.5 the combined effects of bending and shear in the web of an I or box girder should satisfy:

\[
\overline{\eta}_1 + \left(1 - \frac{M_{f,Rd}}{M_{pl,Rd}}\right) (2\overline{\eta}_3 - 1)^2 \leq 1,0 \quad \text{for} \quad \overline{\eta}_1 \geq \frac{M_{f,Rd}}{M_{pl,Rd}}
\]  

(5.21)

where:

- \( M_{f,Rd} \) is the design plastic moment of resistance of the section consisting of the effective area of the flanges
- \( M_{pl,Rd} \) is the design plastic moment of resistance of the cross section consisting of the effective area of the flanges and the fully effective web irrespective of its section class.

\[
\overline{\eta}_1 = \frac{M_{Ed}}{M_{pl,Rd}}
\]

(5.22)

\[
\overline{\eta}_3 = \frac{V_{Ed}}{V_{bw,Rd}}
\]

(5.23)
Stresses are taken as positive. $M_{Ed}$ and $V_{Ed}$ should include second order effects where relevant.

The criterion given in Equation 5.21 should be verified at all sections other than those located at a distance less than $h_w/2$ from a support with vertical stiffeners.

If an axial force $N_{Ed}$ is present, then $M_{p,Rd}$ should be replaced by the reduced plastic resistance moment $M_{N,Rd}$ according to 6.2.9 of EN 1993-1-1 and $M_{f,Rd}$ should be reduced according to Equation 5.18. Reference should be made to EN 1993-1-5 if the axial force is so large that the whole web is in compression.

### 5.4.4 Web crushing, crippling and buckling

Provided that the flanges are laterally restrained, the resistance of an unstiffened web to forces from concentrated loads or support reactions will be governed by one of three possible failure modes:

- crushing of the web close to the flange, accompanied by plastic deformation of the flange
- crippling of the web in the form of localised buckling and crushing of the web close to the flange, accompanied by plastic deformation of the flange
- buckling of the web over most of the depth of the member.

For cold formed structural sections, the guidance in EN 1993-1-3 for carbon steel can be adopted.

For rolled beams and welded girders, the following approach should be adopted, based on the guidance in EN 1993-1-5.

For unstiffened or stiffened webs the design resistance to local buckling under transverse forces should be taken as:

$$ F_{Rd} = f_{yw} L_{eff} t_w / \gamma_{M1} $$

(5.24)

where:

- $t_w$ is the thickness of the web
- $f_{yw}$ is the yield strength of the web
- $L_{eff}$ is the effective length for resistance to transverse forces, which should be determined from

$$ L_{eff} = \chi_F l_y $$

where:

- $l_y$ is the effective loaded length appropriate to the length of stiff bearing
- $s_s$
- $\chi_F$ is the reduction factor due to local buckling

In addition the effect of the transverse force on the moment resistance of the member should be considered.

To determine $L_{eff}$, a distinction should be made between three types of force application, as follows:
• Forces applied through one flange and resisted by shear forces in the web (Figure 5.4a)
• Forces applied to one flange and transferred through the web directly to the other flange (Figure 5.4b)
• Forces applied through one flange close to an unstiffened end (Figure 5.4c)

\[ k_F = 6 + 2 \left[ \frac{h_w}{a} \right]^2 \]
\[ k_F = 3,5 + 2 \left[ \frac{h_w}{a} \right]^2 \]
\[ k_F = 2 + 6 \left[ \frac{s_s + c}{h_w} \right] \leq 6 \]

**Figure 5.4** Buckling coefficients for different types of load application

**Length of stiff bearing**

The length of stiff bearing, \( s_s \), on the flange is the distance over which the applied force is effectively distributed and it may be determined by dispersion of load through solid steel material at a slope of 1:1, see Figure 5.5. However, \( s_s \) should not be taken as larger than the depth of the web, \( h_w \).

If several concentrated loads are closely spaced, the resistance should be checked for each individual load as well as for the total load, with \( s_s \) as the centre-to-centre distance between outer loads.

**Effective loaded length**

The effective loaded length \( l_e \) should be calculated using two dimensionless parameters \( m_1 \) and \( m_2 \) obtained from:

\[ m_1 = \frac{f_{yt} b_f}{f_{yw} t_w} \]  \hspace{1cm} (5.25)

\[ m_2 = 0,02 \left( \frac{h_w}{t_f} \right)^2 \]  for \( \lambda_F > 0,5 \)  \hspace{1cm} (5.26a)

\[ m_2 = 0 \]  for \( \lambda_F \leq 0,5 \)  \hspace{1cm} (5.26b)
For cases a) and b) in Figure 5.4, \( l_y \) should be obtained using

\[
 l_y = s_x + 2t_f \left(1 + \sqrt{m_1 + m_2}\right) \quad (5.27)
\]

but \( l_y \) should not exceed the distance between adjacent transverse stiffeners.

For case c) \( l_y \) should be obtained as the smaller of the values given by Equations 5.28 and 5.29. In Equations 5.30, \( s_x \) should be taken as zero if the structure that introduces the force does not follow the slope of the girder, see Figure 5.5.

\[
 l_y = l_e + t_f \left[ \frac{m_1}{2} + \left( \frac{l_e}{t_f} \right)^2 + m_2 \right] \quad (5.28)
\]

\[
 l_y = l_e + t_f \sqrt{m_1 + m_2} \quad (5.29)
\]

where \( l_e \) is given by:

\[
 l_e = \frac{k_F E t_w^2}{2f_yw h_w} \leq s_x + c \quad (5.30)
\]

**Effective length of resistance**

The effective length of resistance should be obtained from:

\[
 L_{\text{eff}} = \chi_F l_y \quad (5.31)
\]

with

\[
 \chi_F = \frac{0.5}{\lambda_F} \leq 1.0 \quad (5.32)
\]

\[
 \lambda_F = \sqrt{\frac{l_y t_w f_yw}{F_{\text{cr}}}} \quad (5.33)
\]

\[
 F_{\text{cr}} = 0.9 k_F E \frac{t_w^3}{h_w} \quad (5.34)
\]

where:

- \( k_F \) is the buckling coefficient for different types of force application (Figure 5.4).

It should be noted that in order to calculate \( m_2 \), a value of \( \lambda_F \) needs to be assumed. Once the value of \( \lambda_F \) has been calculated, the value of \( m_2 \) may need to be recalculated.

### 5.4.5 Transverse stiffeners

Transverse stiffeners at supports and at other positions where significant external forces are applied should preferably be double-sided and symmetric about the centreline of the web. These stiffeners should be checked for
cross-section crushing and buckling. Intermediate stiffeners not subject to external forces need only be checked for buckling.

The effective cross-section to use in the buckling check should include a width of web plate as shown in Figure 5.6. At the end of a member (or at the openings in the web) the width of web included in the cross-section should not exceed that available.

![Figure 5.6 Effective cross-section of stiffeners for buckling](image)

The out-of-plane buckling resistance $N_{b,Rd}$ of the stiffener should be determined from Section 5.3.3 using $\alpha = 0.49$ and $\lambda = 0.2$. The buckling length $l$ of the stiffener should be appropriate for the conditions of restraint, but not less than $0.75h_w$, where both ends are fixed laterally. A larger value of $l$ should be used for conditions that provide less end restraint. The torsional buckling resistance of the cruciform section should also be checked.

For single-sided or other asymmetric stiffeners the resulting eccentricity should be allowed for in accordance with Section 5.5.2.

At supports or at intermediate positions where significant loads are applied, the buckling resistance should exceed the reaction or load. At other intermediate positions, the compression force $N_{Ed}$ in the stiffener may be obtained from:

$$N_{Ed} = V_{Ed} - \frac{1}{\lambda_w} \frac{f_{yw} h_w t_w}{\sqrt{3} \gamma_{M1}}$$

where:

$V_{Ed}$ is the design shear force in the member.

The above expression should be calculated assuming the stiffener under consideration is removed.

The second moment of area of an intermediate stiffener, $I_s$, should satisfy the following:

$$a / h_w < \sqrt{2}, \quad I_s \geq 1.5 h_w^3 t^3 / a^2$$

$$a / h_w \geq \sqrt{2}, \quad I_s \geq 0.75 h_w t^3$$

### 5.4.6 Determination of deflections

Deflections should be determined for the load combination at the relevant Serviceability Limit State.

The deflection of elastic beams (i.e. those not containing a plastic hinge) may be estimated by standard structural theory, except that the secant modulus of elasticity should be used instead of Young’s modulus. The secant modulus
varies with the stress level in the beam and values may be found in Appendix C. This is a simplified method which is accurate for predicting deflections when the secant modulus is based on the maximum stress in the member and this maximum stress does not exceed 65% of the 0.2% proof strength. At higher levels of stress, the method becomes very conservative and a more accurate method (e.g. one which involves integrating along the length of the member) should be used.

In the case of Class 4 cross-sections and/or members subject to shear lag, an effective section should be used in the calculations. As a first estimate, it is appropriate to use the effective section based on the effective widths established in Sections 4.4.1 and/or 4.4.2. As a refinement, it is possible to use an effective section based on the effective buckling widths determined for the actual stress in the elements by taking \( \varepsilon \) in Section 4.4.1 (but not in Section 4.4.2) as:

\[
\varepsilon = \left[ \frac{235}{\sigma} \frac{E}{210000} \right]^{1/2}
\]

(5.38)

where:

\( \sigma \) is the actual stress in the element in the associated effective cross-section

\( E \) is Young’s modulus.

### 5.5 Members subject to combinations of axial load and bending moments

#### 5.5.1 Axial tension and bending

Tension members with moments should be checked for resistance to lateral torsional buckling in accordance with Section 5.4.2 under the moment alone. They should also be checked for capacity under the combined effects of axial load and moment at the points of maximum bending moment and axial load. The following relationship should be satisfied:

\[
\frac{N_{Ed}}{N_{Rd}} + \frac{M_{y,Ed}}{M_{y,Rd}} + \frac{M_{z,Ed}}{M_{z,Rd}} \leq 1
\]

(5.39)

where:

\( N_{Ed} \) is the design axial tensile load in the member at the critical location

\( N_{Rd} \) is the design resistance of the member in tension

\( M_{y,Ed} \) is the design moment about the major axis at the critical section

\( M_{z,Ed} \) is the design moment about the minor axis at the critical section

\( M_{y,Rd} \) is the design moment resistance about the major axis in the absence of axial load and include any reduction that may be cased by shear effects (Section 4.7.4)

\( M_{z,Rd} \) is the design moment about the minor axis in the absence of axial load and includes any reduction that may be cased by shear effects (Section 4.7.4).
5.5.2 Axial compression and bending

In addition to satisfying the requirements of cross-sectional resistance (see Section 4.7.6) at every point along the length of the member and the general requirements for beam members (see Section 5.4), interaction effects should be considered between compressive loads and bending moments.

Axial compression and uniaxial major axis moment:

To prevent premature buckling about the major axis:

\[
\frac{N_{\text{Ed}}}{(N_{b,Rd})_{\min}} + k_y \left( \frac{M_{y,Ed} + N_{\text{Ed}} e_{Ny}}{\beta_{W,y} W_{pl,y} f_y / \gamma_M} \right) \leq 1
\] (5.40)

To prevent premature buckling about the minor axis (for members subject to lateral-torsional buckling):

\[
\frac{N_{\text{Ed}}}{(N_{b,Rd})_{\min_1}} + k_{LT} \left( \frac{M_{y,Ed} + N_{\text{Ed}} e_{Ny}}{M_{b,\text{Rd}}} \right) \leq 1
\] (5.41)

Axial compression and uniaxial minor axis moment:

To prevent premature buckling about the minor axis:

\[
\frac{N_{\text{Ed}}}{(N_{b,Rd})_{\min}} + k_z \left( \frac{M_{z,Ed} + N_{\text{Ed}} e_{Nz}}{\beta_{W,z} W_{pl,z} f_y / \gamma_M} \right) \leq 1
\] (5.42)

Axial compression and biaxial moments:

All members should satisfy:

\[
\frac{N_{\text{Ed}}}{(N_{b,Rd})_{\min}} + k_y \left( \frac{M_{y,Ed} + N_{\text{Ed}} e_{Ny}}{\beta_{W,y} W_{pl,y} f_y / \gamma_M} \right) + k_z \left( \frac{M_{z,Ed} + N_{\text{Ed}} e_{Nz}}{\beta_{W,z} W_{pl,z} f_y / \gamma_M} \right) \leq 1
\] (5.43)

Members potentially subject to lateral-torsional buckling should also satisfy:

\[
\frac{N_{\text{Ed}}}{(N_{b,Rd})_{\min_1}} + k_{LT} \left( \frac{M_{y,Ed} + N_{\text{Ed}} e_{Ny}}{M_{b,\text{Rd}}} \right) + k_z \left( \frac{M_{z,Ed} + N_{\text{Ed}} e_{Nz}}{\beta_{W,z} W_{pl,z} f_y / \gamma_M} \right) \leq 1
\] (5.44)

In the above expressions:
- \(e_{Ny}\) and \(e_{Nz}\) are the shifts in the neutral axes when the cross-section is subject to uniform compression
- \(N_{b,Rd}\), \(M_{y,Ed}\) and \(M_{z,Ed}\) are the design values of the compression force and the maximum moments about the y-y and z-z axis along the member, respectively
- \((N_{b,Rd})_{\min}\) is the smallest value of \(N_{b,Rd}\) for the following four buckling modes: flexural buckling about the y axis, flexural buckling about the z axis, torsional buckling and torsional-flexural buckling (see Sections 5.3.3. and 5.3.4)
- \((N_{b,Rd})_{\min_1}\) is the smallest value of \(N_{b,Rd}\) for the following three buckling modes: flexural buckling about the z axis, torsional buckling and torsional-flexural buckling (see Sections 5.3.3. and 5.3.4)
\( \beta_{W,y} \) and \( \beta_{W,z} \) are the values of \( \beta_W \) determined for the y and z axes respectively in which

\[
\beta_W = \begin{cases} 
  1 & \text{for Class 1 or 2 cross-sections} \\
  \frac{W_{el}}{W_{pl}} & \text{for Class 3 cross-sections} \\
  \frac{W_{eff}}{W_{pl}} & \text{for Class 4 cross-sections}
\end{cases}
\]

\( W_{pl,y} \) and \( W_{pl,z} \) are the plastic moduli for the y and z axes respectively

\( M_{b,Rd} \) is the lateral-torsional buckling resistance (see Section 5.4.2)

\( k_y, k_z, k_{LT} \) are the interaction factors

\[
k_y = 1.0 + 2\left(\bar{x}_y - 0.5\right) \frac{N_{Ed}}{N_{b,Rd,y}} \quad \text{but} \quad 1.2 \leq k_y \leq 1.2 + 2 \frac{N_{Ed}}{N_{b,Rd,y}}
\]

\[
k_z = 1.0 + 2\left(\bar{x}_z - 0.5\right) \frac{N_{Ed}}{N_{b,Rd,\min}} \quad \text{but} \quad 1.2 \leq k_z \leq 1.2 + 2 \frac{N_{Ed}}{N_{b,Rd,\min}}
\]

\[
k_{LT} = 1.0
\]

Note that the National Annexes may give other interaction formulae as alternatives to the above equations.

Note that for angles, the y and z axes in the above should be taken as the \( u \) and \( v \) axes respectively.
6 JOINT DESIGN

6.1 General recommendations

6.1.1 Durability

The design of joints, in particular, needs the most careful attention to maintain optimum corrosion resistance.

This is especially so for joints that may become wet from either the weather, spray, immersion, or condensation, etc. The possibility of avoiding or reducing associated corrosion problems by locating joints away from the source of dampness should be investigated. Alternatively, it may be possible to remove the source of dampness; for instance, in the case of condensation, by adequate ventilation or by ensuring that the ambient temperature within the structure lies above the dew point temperature.

Where it is not possible to prevent a joint involving carbon steel and stainless steel from becoming wet, consideration should be given to preventing bimetallic corrosion, see Section 3.7.2. The use of carbon steel bolts with stainless steel structural elements should always be avoided. In bolted joints that would be prone to an unacceptable degree of corrosion, provision should be made to isolate electrically the carbon steel and stainless steel elements. This entails the use of insulating washers and possibly bushes; typical suitable details are shown in Figure 6.1. For offshore structures, it will be found that certifying authorities may require such measures and the designer is strongly urged to liaise with the designated authority at an early stage to establish exact requirements.

![Figure 6.1 Typical detail for connecting dissimilar materials (to avoid bimetallic corrosion)](image)

With respect to welded joints involving carbon and stainless steels, it is generally recommended that any paint system applied to the carbon steel should extend over the weldment and cover some area of the stainless steel.

Care should be taken in selecting appropriate materials for the environment to avoid crevice corrosion in bolted joints (see Section 3.7.2).

The heating and cooling cycle involved in welding affects the microstructure of all stainless steels, though some grades more than others, and this is of
particular importance for duplex materials. It is essential that suitable welding procedures and consumables are used and that qualified welders undertake the work. Guidance on this matter is given in Section 10.4.

6.1.2 Design assumptions

Joints may be designed by distributing the internal forces and moments in a realistic manner, bearing in mind the relative stiffness of elements that make up the joint. The internal forces and moments must be in equilibrium with the applied forces and moments. Each element participating in the assumed load paths should be capable of resisting the forces assumed in the analysis and at the implied deformation within the element’s deformation capacity.

6.1.3 Intersections and splices

Members meeting at a joint should normally be arranged with their centroidal axes intersecting at a point. Where there is eccentricity at intersections, the members and connections should be designed to accommodate the resulting moments. In the case of joints with angles or tees connected by at least two bolts at each joint, the setting out lines for the bolts in the angles and tees may be substituted for the centroidal axes for the purpose of determining the intersection at the joints.

Splices in beams should preferably be located as near as possible to points of contraflexure (zero bending moment). In column splices, consideration should be given to moments caused by P-δ effects.

6.1.4 Other general considerations

Where a joint is subject to impact, vibration, or frequent reversal of significant stress, welding is the preferred method of joining. These connections should be checked for the effects of fatigue (see Section 8).

Ease of fabrication and erection are factors to be considered in the design of all joints and splices. Attention should be paid to:

- use of standarised details
- the clearances necessary for safe erection
- the clearances needed for tightening fasteners
- the need for access for welding
- the requirements of welding procedures
- the effects of angular and length tolerances on fit-up.

It should be noted that greater welding distortions will be associated with the austenitic stainless steels than with carbon steels (see Section 10.4.4). Attention should also be paid to the requirements for subsequent inspection and maintenance.
6.2 Bolted connections

6.2.1 General
The recommendations in this Section apply to connections with bolts in clearance holes where shear, tension or a combination of shear and tension is to be carried. It is good practice to provide washers under both the bolt head and the nut. Guidance on appropriate materials for bolts and nuts is given in Sections 3.1.2 and 10.5.

Shear forces are transferred by bearing between the bolts and the connected parts. No recommendations are given for connections in which shear is transferred by frictional resistance, but see Section 6.2.2.

The strength of a connection is to be taken as the lesser of the strength of the connected parts (see Section 6.2.3) and that of the fasteners (see Section 6.2.4).

To restrict irreversible deformation in bolted connections, the stresses in bolts and net cross-sections at bolt holes under the characteristic load combinations should be limited to the yield strength.

6.2.2 Preloaded bolts
Stainless steel bolts may be used as preloaded bolts provided appropriate tensioning techniques are used. If stainless steel bolts are highly torqued, galling can be a problem. When preload is applied, consideration should be given to time-dependent stress relaxation. Connections should not be designed as slip resistant at either the serviceability or ultimate limit state unless acceptability in the particular application can be demonstrated by test.

6.2.3 Connected parts

Holes
Holes can be formed by drilling or punching. However, the cold working associated with punching may increase the susceptibility to corrosion and therefore punched holes are less suitable in aggressive environments (e.g. heavy industrial and marine environments).

The maximum clearances in standard holes are:
1 mm for M12 and M14 bolts (M14 is non standard size)
2 mm for M16 to M24 bolts
3 mm for M27 and larger bolts

Position of holes
Edge distance is defined as the distance from the centre of a hole to the adjacent edge of the connecting part at right angles to the direction of stress; end distance is similarly defined but in the direction in which the fastener bears.

The minimum value of the end distance, \(e_1\), or that of the edge distance, \(e_2\), (see Figure 6.2) should be taken as \(1.2d_0\), where \(d_0\) is the diameter of the bolt hole. Note that the end distance may need to be larger than this to provide adequate bearing resistance, see below.

The maximum value of the end or edge distance should be restricted to \(4t + 40\) mm, where \(t\) is the thickness (in mm) of the thinner outer ply.
The minimum centre-to-centre bolt spacing is \(2,2d_0\) in the direction of stress, \(p_1\), (see Figure 6.2). The corresponding minimum spacing, \(p_2\), normal to the direction of stress is \(2,4d_0\).

The maximum spacing of bolts in any direction should be such that local compressive buckling of the plies is taken into account, see EN 1993-1-8.

**Figure 6.2  Symbols for defining position of holes**

For staggered bolt rows, a minimum line spacing \(p_2=1,2d_0\) may be used if the minimum distance, \(L\), between any two fasteners in a staggered row is greater or equal to \(2,4d_0\), see Figure 6.2.

**Bearing resistance**

The appropriate resistance of a bolted connection in stainless steel will usually be governed by serviceability criteria in which the hole elongation at serviceability loads is to be limited. In order to avoid carrying out a separate check for serviceability, a limit on hole elongation at ultimate load is placed by using a reduced value of the ultimate tensile strength \(f_{u,\text{red}}\) where:

\[
f_{u,\text{red}} = 0.5f_y + 0.6f_u \quad \text{but} \quad f_u
\]

(6.1)

The value of \(F_{b,Rd}\) is given by:

\[
F_{b,Rd} = \frac{k_1 \alpha_b f_{u,\text{req}} d t}{\gamma M_2}
\]

(6.2)

where \(\alpha_b\) is the smallest of:

- \(\alpha_d\)
- \(f_{ub} / f_{u,\text{red}}\)
- 1.0

where:

- \(d\) is the bolt diameter
- \(t\) is the ply thickness
\( f_{ub} \) is the characteristic ultimate tensile strength of the connected ply (taken as the minimum specified ultimate tensile strength, see Table 3.1).

\[ \alpha_d = \frac{e_1}{3d_0} \quad \text{for end bolts in the direction of load transfer} \]

\[ \alpha_d = \frac{p_1}{3d_0} - \frac{1}{4} \quad \text{for inner bolts in the direction of load transfer} \]

\( k_1 \) is the smaller of \( 2.8 \frac{e_2}{d_0} - 1.7 \) or 2.5 for edge bolts perpendicular to the direction of load transfer.

\( k_1 \) is the smaller of \( 1.4 \frac{p_2}{d_0} - 1.7 \) or 2.5 for inner bolts perpendicular to the direction of load transfer.

In the case of single lap joints of flats with only one bolt row, the bolts should be provided with washers under both the head and the nut and the bearing resistance for each bolt should be further limited to:

\[ F_{b,Rd} = \frac{1.5 f_{u,\text{red}}}{\gamma_{M2}} dt \quad (6.3) \]

The resistance of a group of fasteners may be determined as the sum of the bearing resistances \( F_{b,Rd} \) of the individual fasteners provided that the design shear resistance \( F_{v,Rd} \) of each individual fastener is greater or equal to the design bearing resistance \( F_{b,Rd} \). Otherwise the resistance of a group of fasteners should be determined by using the smallest resistance of the individual fasteners multiplied by the number of fasteners.

**Tension resistance**

The tensile resistance of the connected part should be based on the lesser of:

a) the plastic resistance of the gross cross-section

\[ N_{pl,Rd} = \frac{A f_y}{\gamma_{M0}} \quad (6.4) \]

b) the ultimate resistance of the net cross-section at holes for fasteners

\[ N_{u,Rd} = \frac{k_z A_{net} f_u}{\gamma_{M2}} \quad (6.5) \]

where the terms are defined in Section 4.7.2.

Note that the equation for the ultimate resistance of the net section should only be used for one shear plane when washers are present under both the head and nut of the bolt.

If ductile behaviour is required, then the plastic resistance of the gross section must be less than the net section ultimate resistance. Requirements for ductility
and rotation capacity are given in EN 1993-1-8. Requirements for seismic design are given in EN 1998.

**Design for block tearing**

The guidance in EN 1993-1-8 is applicable.

**Angles connected by one leg and other unsymmetrically connected members in tension**

The eccentricity of fasteners in end connections and the effects of the spacing and edge distances of the bolts should be taken into account in determining the design resistance of unsymmetrical members, as well as of symmetrical members that are connected unsymmetrically, such as angles connected by one leg.

Angles connected by a single row of bolts in one leg may be treated as concentrically loaded and the design ultimate resistance of the net section determined as follows:

With 1 bolt: \[ N_{u,Rd} = \frac{2,0 (e_2 - 0,5d_0 ) t f_u}{\gamma M_2} \] (6.6)

With 2 bolts: \[ N_{u,Rd} = \frac{\beta_2 A_{net} f_u}{\gamma M_2} \] (6.7)

With three or more bolts: \[ N_{u,Rd} = \frac{\beta_3 A_{net} f_u}{\gamma M_2} \] (6.8)

where:

\( \beta_2 \) and \( \beta_3 \) are reduction factors dependent on the pitch \( p_1 \) as given in Table 6.1. For intermediate values of \( p_1 \) the value of \( \beta \) can be determined by linear interpolation.

\( A_{net} \) is the net area of the angle. For an unequal-leg angle connected by its smaller leg \( A_{net} \) should be taken as equal to the net section area of an equivalent equal-leg angle of leg size equal to that of the smaller leg.

**Table 6.1 Reduction factors \( \beta_2 \) and \( \beta_3 \)**

<table>
<thead>
<tr>
<th>Connection</th>
<th>Factor</th>
<th>Pitch, ( p_1 )</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>( \leq 2,5d_0 )</td>
</tr>
<tr>
<td>2 bolts</td>
<td>( \beta_2 )</td>
<td>0,4</td>
</tr>
<tr>
<td>3 bolts or more</td>
<td>( \beta_3 )</td>
<td>0,5</td>
</tr>
</tbody>
</table>

**6.2.4 Fasteners**

**Net areas**

The area of the bolt to be used in calculations for bolts in tension should be taken as the tensile stress area, as defined in the appropriate product standard.

For bolts in shear, the greater shank area may be used if it can be guaranteed that the threaded portion will be excluded from the shear plane; consideration should be given to the possibility that bolts may be inserted from either
direction. If no such guarantee can be given, the tensile stress area should be used.

**Shear resistance**

The shear resistance of a bolted connection is dependent on the number of shear planes and their position along the bolt. For each shear plane, the shear resistance in the absence of tension may be determined as follows:

\[ F_{v,Rd} = \frac{\alpha f_{ub} A}{\gamma M_2} \]  \hspace{1cm} (6.9)

where:

- \( A \) is the gross cross-section area of the bolt (if the shear plane passes through unthreaded portion of the bolt); or the tensile stress area of the bolt (if the shear plane passes through the threaded portion of the bolt)
- \( f_{ub} \) is the ultimate tensile strength of the bolt.

The value of \( \alpha \) may be defined in the National Annex. The recommended values are:
- if the shear plane passes through the unthreaded portion of the bolt, \( \alpha = 0.6 \)
- if the shear plane passes through the threaded portion of the bolt, \( \alpha = 0.5 \).

**Tensile resistance**

The tension resistance of a bolt is given by \( F_{t,Rd} \):

\[ F_{t,Rd} = \frac{k_2 f_{ub} A_3}{\gamma M_2} \]  \hspace{1cm} (6.10)

where:

- \( k_2 = 0.63 \) for countersunk bolts, otherwise \( k_2 = 0.9 \).

Where fasteners are required to carry an applied tensile force, they should be proportioned to resist the additional force due to prying action, where this can occur. Guidance on accounting for prying forces is given in EN 1993-1-8.

**Combined shear and tension**

When a bolt is simultaneously subjected to a shear force, \( F_{v,Ed} \), and a tensile force (including prying effects), \( F_{t,Ed} \), interaction effects should be considered. This may be accounted for by satisfying the following interaction relationship:

\[ \frac{F_{v,Ed}}{F_{v,Rd}} + \frac{F_{t,Ed}}{1.4 F_{t,Rd}} \leq 1.0 \]  \hspace{1cm} (6.11)

where \( F_{v,Rd} \) and \( F_{t,Rd} \) are as given above. Note that the design tensile force (including any force due to prying action) must also be less than the tensile resistance.
Long joints and large grip lengths
For splices of unusual length (say 500 mm or 15 bolt diameters upwards) or when the grip length (i.e. the total thickness of the connected plies) exceeds 5 bolt diameters, the shear resistance should be reduced. In the absence of data for stainless steel, it is recommended to consult carbon steel rules for these situations in EN 1993-1-8.

6.3 Mechanical fasteners for thin gauge material
The design of connections for stainless steel sheets using self-tapping screws can be calculated in accordance with EN 1993-1-3, except that the pull-out strength should be determined by testing. In order to avoid seizure of the screw or stripping its thread, the ability of the screw to drill and form threads in stainless steel should be demonstrated by tests unless sufficient experience is available. The reduced value for the tensile strength, $f_{u,\text{red}}$, given in Equation 6.1, should be used in place of $f_u$.

6.4 Welded connections
6.4.1 General
It is essential that welds are made using correct procedures, including compatible consumables, with suitably qualified welders (see Section 10.4). This is important not only to ensure the strength of the weld and to achieve a defined weld profile but also to maintain corrosion resistance of the weld and surrounding material.

The following recommendations apply to full and partial penetration butt welds and to fillet welds made by an arc welding process such as:

<table>
<thead>
<tr>
<th>Process number</th>
<th>Process name</th>
</tr>
</thead>
<tbody>
<tr>
<td>111</td>
<td>Metal-arc welding with covered electrode (manual metal arc welding)</td>
</tr>
<tr>
<td>121</td>
<td>Submerged arc welding with wire electrode</td>
</tr>
<tr>
<td>122</td>
<td>Submerged arc welding with strip electrode</td>
</tr>
<tr>
<td>131</td>
<td>Metal-arc inert gas welding (MIG welding)</td>
</tr>
<tr>
<td>135</td>
<td>Metal-arc active gas welding (MAG welding)</td>
</tr>
<tr>
<td>137</td>
<td>Flux-cored wire metal-arc welding with inert gas shield</td>
</tr>
<tr>
<td>141</td>
<td>Tungsten inert gas welding (TIG welding)</td>
</tr>
<tr>
<td>15</td>
<td>Plasma arc welding</td>
</tr>
</tbody>
</table>

(Process numbers are as defined in EN ISO 4063.)

Compatible consumables should be used, such that the weld yield strength and ultimate strengths exceed those of the parent material. (For undermatched consumables, see Section 6.4.4.) Table 6.2 gives suitable welding consumables for different grades and Table 6.3 gives the mechanical properties of these consumables.
Table 6.2  Applicable steel grades and welding consumables

<table>
<thead>
<tr>
<th>Base material</th>
<th>Welding consumables</th>
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</thead>
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<tr>
<td></td>
<td>Covered electrodes</td>
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<tr>
<td></td>
<td>EN 1600</td>
</tr>
<tr>
<td>1.4301</td>
<td>E 19 9</td>
</tr>
<tr>
<td>1.4306</td>
<td>E 19 9 L</td>
</tr>
<tr>
<td>1.4307</td>
<td>E 19 9 L</td>
</tr>
<tr>
<td>1.4318</td>
<td>E 19 9 L</td>
</tr>
<tr>
<td>1.4541</td>
<td>E 19 9 Nb</td>
</tr>
<tr>
<td>1.4401</td>
<td>E 19 12 2</td>
</tr>
<tr>
<td>1.4404</td>
<td>E 19 12 3 L</td>
</tr>
<tr>
<td>1.4571</td>
<td>E 19 12 3 Nb</td>
</tr>
<tr>
<td>1.4362</td>
<td>E 25 7 2 N L</td>
</tr>
<tr>
<td>1.4462</td>
<td>E 25 7 2 N L</td>
</tr>
</tbody>
</table>

Table 6.3  Mechanical properties of welding consumables according to EN 1600, EN 12072 and EN 12073

<table>
<thead>
<tr>
<th>Weld material</th>
<th>Yield strength N/mm²</th>
<th>Ultimate tensile strength N/mm²</th>
</tr>
</thead>
<tbody>
<tr>
<td>E 19 9</td>
<td>350</td>
<td>550</td>
</tr>
<tr>
<td>E/G/T 19 9 L</td>
<td>320</td>
<td>510</td>
</tr>
<tr>
<td>E/G/T 19 9 Nb</td>
<td>350</td>
<td>550</td>
</tr>
<tr>
<td>E 19 12 2</td>
<td>350</td>
<td>550</td>
</tr>
<tr>
<td>E/G/T 19 12 3 L</td>
<td>320</td>
<td>510</td>
</tr>
<tr>
<td>E/G/T 19 12 3 Nb</td>
<td>350</td>
<td>550</td>
</tr>
<tr>
<td>E 25 7 2 N L</td>
<td>500</td>
<td>700</td>
</tr>
<tr>
<td>G 25 7 2 L</td>
<td>500</td>
<td>700</td>
</tr>
<tr>
<td>T 22 9 3 N L</td>
<td>450</td>
<td>550</td>
</tr>
</tbody>
</table>

Note that special consideration should be given to the case when a test value of the 0.2% proof stress is used as a basis of design (i.e. design to Section 3.2.4(ii)). Manufacturers of stainless steel and consumables may help in the selection of appropriate consumables. The weld metal should be at least as noble as the parent material.

Intermittent fillet welds and intermittent partial penetration butt welds are best avoided in all but the mildest of environments, to reduce the possibility of corrosion. Furthermore, intermittent butt welds should be used with care in marine or very heavily polluted onshore environments, particularly where flow induced by surface tension may occur.

6.4.2 Fillet welds

Application

Fillet welds may be used for connecting parts where fusion faces form an angle of between 60° to 120°. For angles smaller than 60°, fillet welds may be used but should be considered as partial penetration butt welds for design purposes. For angles over 120°, fillet welds should not be relied upon to transmit forces.

A fillet weld should not be used in situations which produce a bending moment about the longitudinal axis of the weld if this causes tension at the root of the weld.
**Effective length and throat size**

The effective length of a fillet weld may be taken as the overall length of the full-size fillet. However, welds with effective lengths shorter than 40 mm or 6 times the throat thickness, should not be relied upon to transmit forces.

The effective throat thickness, \(a\), of a fillet weld should be taken as the height of the largest triangle (with equal or unequal legs) that can be inscribed within the fusion faces and the weld surface, measured perpendicular to the outer side of this triangle, see Figure 6.3. Advantage may be taken of the additional throat thickness of deep penetration fillet welds, see Figure 6.4, provided that preliminary tests show that the required penetration can consistently be achieved.

![Figure 6.3 Fillet weld throat thickness](image)

![Figure 6.4 Deep penetration fillet weld throat thickness](image)

**Design stress and design shear strength**

The design stress is obtained as the vector sum of the stresses due to all forces and moments transmitted by the weld. The design stress is calculated for the effective length and throat thickness (see above).

The design resistance of the fillet weld will be sufficient if the following are both satisfied:

\[
\left[\sigma^2 + 3(\tau_\perp^2 + \tau_\parallel^2)\right]^{0.5} \leq \frac{f_u}{\beta_w \gamma M_2}
\]  
(6.12a)
\[ \sigma_\perp \leq \frac{0.9 f_u}{\gamma_{M2}} \]  

(6.12b)

where:

- \( \sigma_\perp \) is the normal stress perpendicular to the throat
- \( \tau_\perp \) is the shear stress (in the plane of the throat) perpendicular to the axis of the weld
- \( \tau_\parallel \) is the shear stress (in the plane of the throat) parallel to the axis of the weld
- \( f_u \) is the nominal ultimate tensile strength of the weaker part joined
- \( \beta_w \) is taken as 1.0 for all nominal strength classes of stainless steel, unless a lower value is justified by tests.

Alternatively, the Simplified method in 4.5.3.3 of EN 1993-1-8 can be used to calculate the design resistance of a fillet weld.

### 6.4.3 Butt welds

#### Full penetration butt welds

The design resistance of a full penetration butt weld should be taken as equal to the design resistance of the weaker of the parts joined, provided that the weld satisfies the recommendations of Section 6.3.1.

#### Partial penetration butt welds

Partial penetration butt welds may be used to transmit shear forces. They are not recommended in situations where they would be subjected to tension.

The resistance of a partial penetration butt weld may be determined as for a deep penetration fillet weld. The throat thickness of a partial penetration butt weld may be taken as the depth of penetration that can be consistently achieved, as determined by procedure trials. In the absence of procedure trials, the throat thickness can be assumed to be the depth of preparation less 3 mm.

### 6.4.4 Welding cold worked stainless steel

The same principles apply to welding cold worked stainless steel as to annealed stainless steel provided that:

- The welded joint is subjected to axial load.
- The cold worked strength level of the stainless steel does not exceed CP500 or C850.
- Welding consumables are chosen according to Table 6.2.
- The resistance of the base material in the heat affected zones is based on the tensile strength of the annealed base material.

The filler metal may have lower strength than the base material. For unmatched electrodes, the design resistance of fillet and butt welds should be based on the ultimate strength of the weld metal (see Table 6.3) with \( \beta_w \) taken as 1.0.
7 DESIGN FOR FIRE RESISTANCE

7.1 General
This Section deals with the design of stainless steel structures that, for reasons of
general fire safety, are required to fulfil certain functions, in terms of avoiding
premature collapse of the structure (load bearing function), when exposed to fire.
The recommendations are only concerned with passive methods of fire protection
and are applicable to stainless steel grades and structures that are generally
designed within the rules of Sections 1 to 6 of this document.

Austenitic stainless steels generally retain a higher proportion of their room
temperature strength than carbon steels above temperatures of about 550°C, and
a higher proportion of their stiffness at all temperatures.

EN 1991-1-2 gives the thermal and mechanical actions on structures exposed to
fire. Fire is designated an accidental design situation in the Eurocodes. EN 1990 gives combinations of actions for accidental design situations, and
recommends that the partial factors for actions are taken as 1.0. EN 1993-1-2
recommends that the partial material safety factor $\gamma_{M,fi}$ for the fire situation
should be taken as 1.0.

The performance requirements of a stainless steel structure that may be
subjected to accidental fire loading are no different to those of carbon steel, namely:

- Where mechanical resistance in the case of fire is required, the structure
  should be designed and constructed in such a way that it maintains its load
  bearing function during the relevant fire exposure.

- Deformation criteria should be applied where the means of fire protection,
  or the design criteria for separating elements, require the deformation of
  the load bearing structure to be considered. However, it is not necessary
  to consider the deformation of the load bearing structure if the fire
  resistance of the separating elements is based on the standard fire curve.

7.2 Mechanical properties at elevated
   temperatures

Table 7.1 gives strength and stiffness retention factors, relative to the
appropriate value at 20°C, for the stress-strain relationship and the parameter
$g_{2,0}$ for grades of stainless steel at elevated temperatures. The factors are
defined below:

\begin{align*}
  k_{0,2\text{proof},0} & \quad 0.2\% \text{ proof strength at temperature } \theta \text{ relative to design strength at } \\
  & \quad 20^\circ\text{C}, \text{ i.e. } \frac{f_{0,2\text{proof},0}}{f_y} \\
  g_{2,0} & \quad \text{a parameter used to calculate } f_{2,0} \text{, the strength at } 2\% \text{ total strain at } \\
  & \quad \text{temperature } \theta, \text{ using the following expression:} \\
  & \quad f_{2,0} = f_{0,2\text{proof},0} + g_{2,0}(f_{u,0} - f_{0,2\text{proof},0}) \quad (7.1) \\
  k_{u,0} & \quad \text{ultimate strength at temperature } \theta \text{ relative to ultimate strength at } \\
  & \quad 20^\circ\text{C}, \text{ i.e. } \frac{f_{u,0}}{f_u}
\end{align*}
where:

\[ E \] is Young’s modulus at 20°C (= 200 000 N/mm²)

\[ f_y \] is the characteristic yield strength at 20°C, as defined in Section 3.2.4

\[ f_u \] is the characteristic ultimate tensile strength at 20°C, as defined in Section 3.2.4.

In determining the structural fire resistance of stainless steel members, the following characteristic material strength should be used:

- **Columns**: \( f_{0.2\text{proof},\theta} \) (all cross-section Classes)
- **Restrained beams**: \( f_{2,\theta} \) (Class 1-3 cross-sections), \( f_{0.2\text{proof},\theta} \) (Class 4 cross-sections)
- **Unrestrained beams**: \( f_{0.2\text{proof},\theta} \) (all cross-section Classes)
- **Tension members**: \( f_{2,\theta} \) (all cross-section Classes).

For Class 1-3 restrained beams and tension members, in situations which require consideration of the deformation criteria, the strength at a total strain of 1.0%, \( f_{1,\theta} \) is recommended as a basis for the calculations instead of \( f_{2,\theta} \). The value of \( f_{1,\theta} \) should be calculated using the following relationship:

\[
 f_{1,\theta} = f_{0.2\text{proof},\theta} + 0.5 g_{2,\theta}(f_{u,\theta} - f_{0.2\text{proof},\theta}) \tag{7.2}
\]

Values for \( f_{0.2\text{proof},\theta} \) are given relative to the characteristic yield strength at 20°C by the factor \( k_{0.2\text{proof},\theta} \) in Table 7.1.
<table>
<thead>
<tr>
<th>Temperature θ (°C)</th>
<th>Retention factor $k_{0.2\text{proo}f}$</th>
<th>Parameter $g_{z_{q}}$</th>
<th>Retention factor $k_{u}$</th>
<th>Retention factor $k_{E}$</th>
</tr>
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<tr>
<td><strong>Grade 1.4301</strong></td>
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</tr>
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Table 7.1 (continued)  
Retention factors for strength and stiffness and parameter $g_{2\theta}$ at elevated temperature

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<tr>
<th>Temperature $\theta$ (°C)</th>
<th>Retention factor $k_{0,2\theta}$</th>
<th>Parameter $g_{2\theta}$</th>
<th>Retention factor $k_{u\theta}$</th>
<th>Retention factor $k_{E\theta}$</th>
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</table>

7.3 Thermal properties at elevated temperatures

7.3.1 Thermal elongation

The thermal elongation of austenitic stainless steel $\Delta l/l$ may be determined from the following:

$$\Delta l/l = (16 + 4.79 \times 10^{-3} \theta_a - 1.243 \times 10^{-6} \theta_a^2) \times (\theta_a - 20) \times 10^{-6}$$  \hspace{1cm} (7.3)

where:

- $l$ is the length at 20°C
- $\Delta l$ is the temperature induced expansion
- $\theta_a$ is the steel temperature [°C]

7.3.2 Specific heat

The specific heat of stainless steel $c_a$ may be determined from the following:

$$c_a = 450 + 0.280 \times \theta_a - 2.91 \times 10^{-4} \theta_a^2 + 1.34 \times 10^{-7} \theta_a^3 \text{ J/kgK}$$  \hspace{1cm} (7.4)
where:
\[ \theta_a \] is defined in Section 7.3.1

### 7.3.3 Thermal conductivity
The thermal conductivity of stainless steel \( \lambda_a \) may be determined from the following:

\[
\lambda_a = 14.6 + 1.27 \times 10^{-2} \theta_a \text{ W/mK} \tag{7.5}
\]

where:
\[ \theta_a \] is defined in Section 7.3.1.

### 7.4 Determination of structural fire resistance
Fire resistance may be determined by one or more of the following approaches:

- simple calculation method applied to individual members
- advanced calculation method
- testing.

The simple calculation method is based on conservative assumptions. Advanced calculation methods are design methods in which engineering principles are applied in a realistic manner to specific applications. Where no simple calculation model is given, it is necessary to use either a design method based on an advanced calculation model or a method based on test results.

Advanced calculation methods are covered in the Commentary to these Recommendations (see Foreword).

#### 7.4.1 Cross section classification
In fire design, the method of classification of cross-sections described in Section 4 of this document should be adopted, using design properties at 20°C.

#### 7.4.2 Tension members
The design resistance \( N_{fi,\theta,Rd} \) of a tension member at a uniform temperature \( \theta_a \) should be determined from:

\[
N_{fi,\theta,Rd} = k_{2,\theta} N_{Rd} [\gamma_{M0} / \gamma_{M,fi}] \tag{7.6}
\]

where:
\[ k_{2,\theta} = f_{2,\theta} / f_y \] i.e. the retention factor for the strength at 2% total strain at temperature \( \theta \)
\[ N_{Rd} \] is the design resistance of the cross-section \( N_{pl,Rd} \) for normal temperature design, according to Section 4.7.2.
\[ \gamma_{M0} \] and \[ \gamma_{M,fi} \] are partial factors, see Table 2.1

Where the temperature in the member is non-uniform, the design resistance is given by:
\[ N_{fi,t,Rd} = \sum_{i=1}^{n} A_i k_{2,0,i} f_Y / \gamma_{M,fi} \]  

(7.7)

where:

- \( A_i \) is an elemental area of the cross-section
- \( \theta_i \) is the temperature in the elemental area \( A_i \)
- \( k_{2,0,i} \) is the retention factor for the strength at 2% total strain at temperature \( \theta_i \) (see Section 7.2).

Alternatively, the design resistance \( N_{fi,t,Rd} \) at time \( t \) of a tension member with a non-uniform temperature distribution may conservatively be taken as equal to the design resistance \( N_{fi,0,Rd} \) of a tension member with a uniform temperature \( \theta_a \) equal to the maximum temperature \( \theta_{a,max} \) reached at time \( t \).

### 7.4.3 Compression members

The following recommendations apply to columns with Class 1, 2, 3 or 4 cross-sections that are:

- cold formed, open cross-sections (not welded), e.g. channels or angles, or
- cold formed hollow cross-sections (both seam welded or seamless), e.g. circular or rectangular hollow sections.

The design buckling resistance \( N_{b,fi,t,Rd} \) at time \( t \) of a compression member with a uniform temperature \( \theta_a \) is given by:

\[ N_{b,fi,t,Rd} = \chi_{fi} A k_{0,2\text{proof},\theta} f_y / \gamma_{M,fi} \]  

for Class 1, 2 or 3 sections  

(7.8)

\[ N_{b,fi,t,Rd} = \chi_{fi} A_{\text{eff}} k_{0,2\text{proof},\theta} f_y / \gamma_{M,fi} \]  

for Class 4 sections  

(7.9)

where:

- \( k_{0,2\text{proof},\theta} \) is the 0,2% proof strength retention factor at temperature \( \theta_a \) (see Section 7.2).
- \( \chi_{fi} \) is the reduction factor for flexural buckling in fire, given by:

\[ \chi_{fi} = \frac{1}{\varphi_0 + \sqrt{\varphi_0^2 - \lambda_0^2}} \]  

but \( \chi_{fi} \leq 1 \)  

(7.10)

where:

\[ \varphi_0 = 0.5 \left( 1 + \alpha \left( \overline{\lambda}_0 - \overline{\alpha}_0 \right) + \overline{\alpha}_0^2 \right) \]  

(7.11)

in which \( \alpha \) and \( \overline{\alpha}_0 \) are the room temperature buckling coefficients given in Table 5.1.

The modified non-dimensional slenderness \( \overline{\alpha}_0 \) at temperature \( \theta \) is given by:

\[ \overline{\alpha}_0 = \frac{k_{0.2\text{proof},\theta}}{k_{E,\theta}} \]  

for all Classes of cross-section  

(7.12)
where:

\[ k_{E,0} \] is the retention factor for the slope of the linear elastic range at temperature \( \theta_a \) (see Section 7.2).

Where the temperature of the member is non-uniform, the compression resistance may conservatively be estimated by assuming a uniform temperature that is equal to the maximum temperature in the member.

The buckling length \( l_{fi} \) of a column for fire design should generally be determined as for normal temperature design. However, in a braced frame, the buckling length \( l_{fi} \) may be determined by considering the column as fixed in direction at continuous or semi-continuous connections to the column lengths in the fire compartments above and below. This assumption can only be made if the fire resistance of the building components that separate these fire compartments is not less than the fire resistance of the column.

In the case of a braced frame in which each storey comprises a separate fire compartment with sufficient fire resistance, the buckling length of a column in an intermediate storey is given by \( l_{fi} = 0.5L \) and in the top storey the buckling length is given by \( l_{fi} = 0.7L \), where \( L \) is the system length in the relevant storey, see Figure 7.1.

![Figure 7.1 Buckling lengths \( l_{fi} \) of columns in braced frames](image)

### 7.4.4 Laterally restrained beams

The design moment resistance \( M_{fi,0,Rd} \) of a cross-section at a uniform temperature \( \theta_a \) should be determined from:

\[
M_{fi,0,Rd} = k_{2,0} \left[ \gamma_{M0} / \gamma_{M,fi} \right] M_{Rd} \quad \text{for Class 1, 2 or 3 cross-sections} \quad (7.13)
\]

\[
M_{fi,0,Rd} = k_{0,2,\text{proof,0}} \left[ \gamma_{M0} / \gamma_{M,fi} \right] M_{Rd} \quad \text{for Class 4 cross-sections} \quad (7.14)
\]

where:

\( M_{Rd} \) is the design plastic moment resistance of the gross cross-section \( M_{pl,Rd} \) (Class 1 or 2 cross-sections), the elastic moment resistance of the gross cross-section \( M_{el,Rd} \) (Class 3 cross-sections) or effective moment resistance of the effective cross section \( M_{eff,Rd} \) (Class 4 cross-sections) for normal temperature design.

\( k_{2,0} \) and \( k_{0,2,\text{proof,0}} \) are as defined in Section 7.4.3.
Where it is necessary to allow for the effects of shear, the reduced moment resistance for normal temperature design according to Section 4.7.6 should be used.

The design moment resistance $M_{f,i,Rd}$ at time $t$ of a cross-section in a member with a non-uniform temperature distribution, may conservatively be determined from:

$$M_{f,i,0,Rd} = M_{f,i,Rd} / \kappa_1 \kappa_2$$

(7.15)

where:

- $M_{f,i,Rd}$ is the design moment resistance of the cross-section (or effective cross section for Class 4 cross-section) at a uniform temperature $\theta_a$ equal to the maximum temperature in the cross-section.
- $\kappa_1$ is an adaptation factor for non-uniform temperature across the cross-section, see Table 7.2.
- $\kappa_2$ is an adaptation factor for non-uniform temperature along the beam, see Table 7.2.

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<th>Table 7.2 Adaptation factors</th>
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<td>Exposure condition</td>
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<td>for a beam exposed to fire on all four sides</td>
</tr>
<tr>
<td>for an unprotected beam exposed to fire on three sides, with a composite or concrete slab on its fourth side</td>
</tr>
<tr>
<td>for a protected beam exposed to fire on three sides, with a composite or concrete slab on its fourth side</td>
</tr>
<tr>
<td>at the supports of a statically indeterminate beam</td>
</tr>
<tr>
<td>in all other cases</td>
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</table>

The design shear resistance $V_{f,i,Rd}$ at time $t$ of a cross-section with a non-uniform temperature distribution should be determined from:

$$V_{f,i,Rd} = k_{2,0,web} V_{Rd} [\gamma_{M0} / \gamma_{M,fi}]$$ for Class 1, 2 or 3 cross-sections (7.16)

$$V_{f,i,Rd} = k_{0,2proof,0,web} V_{Rd} [\gamma_{M0} / \gamma_{M,fi}]$$ for Class 4 cross-sections (7.17)

where:

- $V_{Rd}$ is the shear resistance of the gross cross-section for normal temperature design, according to Section 4.7.5 (for temperatures above 400°C, $\eta$ should be taken as 1,0).
- $\theta_{web}$ is the temperature in the web of the section.

### 7.4.5 Laterally unrestrained beams

The design buckling resistance moment $M_{b,i,Rd}$ at time $t$ of a laterally unrestrained beam should be determined from:

$$M_{b,i,Rd} = \chi_{LT,fi} W_{pl,y} k_{0,2proof,0} f_y / \gamma_{M,fi}$$ for Class 1 and 2 sections (7.18)

$$M_{b,i,Rd} = \chi_{LT,fi} W_{el,y} k_{0,2proof,0} f_y / \gamma_{M,fi}$$ for Class 3 sections (7.19)

$$M_{b,i,Rd} = \chi_{LT,fi} W_{eff,y} k_{0,2proof,0} f_y / \gamma_{M,fi}$$ for Class 4 sections (7.20)
where:

\( \chi_{LT,fi} \) is the reduction factor for lateral-torsional buckling in fire, given by:

\[
\chi_{LT,fi} = \frac{1}{\varphi_{LT,0} + \sqrt{\varphi_{LT,0}^2 - \chi_{LT,fi}^2}} \quad \text{but} \quad \chi_{LT,fi} \leq 1
\]  
(7.21)

and

\[
\varphi_{LT,0} = 0.5 \left( 1 + \alpha_{LT} \left( \chi_{LT,fi} - 0.4 \right) + \chi_{LT,0}^2 \right)
\]  
(7.22)

in which \( \alpha_{LT} \) is the room temperature imperfection factor given in Section 5.4.2.

\( k_{0,2\text{proof},\theta} \) is the retention factor defined in Section 7.4.3 at the maximum temperature \( \theta \) reached anywhere in the section.

The non-dimensional slenderness \( \lambda_{LT,\theta} \) at temperature \( \theta \) is given by:

\[
\lambda_{LT,\theta} = \sqrt[0.5]{\frac{k_{0,2\text{proof},\theta}}{k_{E,0}}} \quad \text{for all Classes of cross-section}
\]  
(7.23)

where:

\( k_{E,0} \) is the reduction factor defined in Section 7.4.3 at temperature \( \theta \).

### 7.4.6 Members subject to axial compression and bending

The combined effects of compressive loads and bending moments should be checked in accordance with the following expressions to prevent premature major and minor axis buckling and lateral torsional buckling:

a) For Class 1, 2 or 3 cross-sections

\[
N_{fi,Ed} \chi_{\min,fi} k_{0,2\text{proof},\theta} \frac{f_y}{\gamma_{M,fi}} + k_y M_{y,fi,Ed} + k_z M_{z,fi,Ed} \leq 1
\]  
(7.24)

\[
N_{fi,Ed} \chi_{\min,1,fi} k_{0,2\text{proof},\theta} \frac{f_y}{\gamma_{M,fi}} + k_{LT} M_{y,fi,Ed} + k_y M_{z,fi,Ed} \leq 1
\]  
(7.25)

where:

\( N_{fi,Ed}, M_{y,fi,Ed} \) and \( M_{z,fi,Ed} \) are the axial design load and bending moments for the fire situation

\( M_{y,0,Rd} \) and \( M_{z,0,Rd} \) are as defined in Section 7.4.4

\( k_{0,2\text{proof},\theta} \) is the reduction factor at temperature \( \theta \), as defined in Section 7.4.3

\( \chi_{\min,fi} \) is the smallest reduction factor for flexural, torsional and torsional-flexural buckling at temperature \( \theta \), as defined in Section 7.4.3

\( \chi_{\min,1,fi} \) is the smallest reduction factor for flexural buckling about the z axis, torsional and torsional-flexural buckling at temperature \( \theta \), as defined in Section 7.4.3

\( \chi_{LT,fi} \) is the reduction factor for lateral torsional buckling at temperature \( \theta \), as defined in Section 7.4.5.
\[ k_{LT} = 1 - \frac{\mu_{LT} N_{fi,Ed}}{\chi_{z,fi} A k_{0,2\text{proof},0} f_y} \leq 1 \]  
(7.26)

\[ \mu_{LT} = 0.15 \bar{\lambda}_{z,0} \beta_{M,LT} - 0.15 \leq 0.9 \]  
(7.27)

\[ k_y = 1 - \frac{\mu_y N_{fi,Ed}}{\chi_{y,fi} A k_{0,2\text{proof},0} f_y} \leq 3 \]  
(7.28)

\[ \mu_y = (1.2 \beta_{M,y} - 3) \bar{\lambda}_{y,0} + 0.44 \beta_{M,y} - 0.29 \leq 0.8 \]  
(7.29)

\[ k_z = 1 - \frac{\mu_z N_{fi,Ed}}{\chi_{z,fi} A k_{0,2\text{proof},0} f_y} \leq 3 \]  
(7.30)

\[ \mu_z = (2 \beta_{M,z} - 5) \bar{\lambda}_{z,0} + 0.44 \beta_{M,z} - 0.29 \leq 0.8 \text{ and } \bar{\lambda}_{z,0} \leq 1.1 \]  
(7.31)

\( \beta_M \) is an equivalent uniform moment factor, given in Table 7.3.

b) For Class 4 cross-sections:

\[ \frac{N_{fi,Ed}}{\chi_{\min,fi} A_{\text{eff}} k_{0,2\text{proof},0} f_y} + \frac{k_y M_{y,fi,Ed} + N_{fi,Ed} e_y}{M_{y,fi,0,Rd}} + \frac{k_z M_{z,fi,Ed} + N_{fi,Ed} e_z}{M_{z,fi,0,Rd}} \leq 1 \]  
(7.32)

\[ \frac{N_{fi,Ed}}{\chi_{\min,fi} A_{\text{eff}} k_{0,2\text{proof},0} f_y} + \frac{k_{LT} M_{y,fi,Ed} + N_{fi,Ed} e_y}{M_{y,fi,0,Rd}} + \frac{k_z M_{z,fi,Ed} + N_{fi,Ed} e_z}{M_{z,fi,0,Rd}} \leq 1 \]  
(7.33)

where the terms are defined in (a) above except that in the calculation of \( k_y, k_z \) and \( k_{LT}, A \) should be replaced by \( A_{\text{eff}}. \)
Table 7.3  
Equivalent uniform moment factors, $\beta_M$

<table>
<thead>
<tr>
<th>Moment diagram</th>
<th>Equivalent uniform moment factor $\beta_M$</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>End moments</strong></td>
<td>$\beta_{\psi M} = 1.8 - 0.7 \psi$</td>
</tr>
</tbody>
</table>

\[
\psi_1 \leq \psi \leq 1
\]

| **Moments due to in-plane lateral loads** | $\beta_{M,Q} = 1.3$ |
| **Moments due to in-plane lateral loads plus end moments** | $\beta_M = \beta_{M,Q} + \frac{M_Q}{\Delta M} (\beta_{M,Q} - \beta_{M,Q})$ |

\[
\Delta M = \max |M| \text{ due to lateral load only}
\]

For moment diagram without change of sign:

\[
\Delta M = \max |M|
\]

For moment diagram with change of sign:

\[
\Delta M = \max |M| + \min |M|
\]

### 7.4.7 Calculation of temperature rise in stainless steel

The method for calculating the temperature rise in carbon steel can also be applied to stainless steel.

The incremental rise in temperature of a uniformly heated bare stainless steel section in time interval $\Delta t$ is given by:

\[
\Delta \theta_{s.t} = \frac{A_{m}}{\rho_s c_s} \frac{V}{h_{\text{net,d}}} \Delta t \tag{7.34}
\]

where:

- $\rho_s$ is the density of stainless steel (kg/m³), as given in Table 3.6 (usually considered as temperature independent)
- $A_{m}/V$ is the section factor for unprotected steel members
is the surface area of the member per unit length

is the volume of the member per unit length

\( \dot{h}_{\text{net},d} \) is the design value of the net heat flux per unit area

\[
\dot{h}_{\text{net},d} = \dot{h}_{\text{net},c} + \dot{h}_{\text{net},r}
\]  

(7.35)

in which:

\[
\dot{h}_{\text{net},c} = \alpha_c (\theta_s - \theta_a)
\]  

(7.36)

\[
\dot{h}_{\text{net},r} = \varphi \varepsilon_{\text{res}} 5.67 \times 10^{-8} \left[ (\theta_s + 273)^4 - (\theta_a + 273)^4 \right]
\]  

(7.37)

\( \alpha_c \) is the coefficient of heat transfer by convection (usually taken as 25W/m²K)

\( \theta_s \) is the gas temperature of the environment of the member in fire exposure (°C), given by the nominal temperature-time curve

\( \theta_a \) is the temperature of the steel section which is assumed to be uniform at time \( t \) (°C)

\( \varphi \) is the configuration factor

\( \varepsilon_{\text{res}} \) is the resultant emissivity.

The parameter \( \varepsilon_{\text{res}} \) represents the radiation transmitted between the fire and the stainless steel surface and its magnitude depends on the degree of direct exposure of the element to the fire. Elements which are partially shielded from the radiant effects of the heat of the fire would have a lower value of \( \varepsilon_{\text{res}} \). For stainless steel, \( \varepsilon_{\text{res}} \) can be taken as 0.2.

The above equation for the incremental temperature rise may be used to determine steel temperatures by incremental integration, if the variation of the fire temperature with time is known. The nominal temperature-time curve for a cellulosic fire is given in EN 1991-1-2 as:

\[
\theta_s = 20 + 345 \log_{10}(8t + 1)
\]  

(7.38)

where:

\( t \) is the elapsed time (minutes).
8 FATIGUE

Consideration should be given to metal fatigue in structures or parts of structures subjected to significant levels of repeated stress. No fatigue assessment is normally required for building structures, except for members supporting lifting appliances, rolling loads or vibrating machinery, and for members subject to wind-induced oscillation.

In common with carbon steel structures, the combination of stress concentrations and defects at welded joints leads to these locations being almost invariably more prone to fatigue failure than other parts of the structure. Guidance on estimating the fatigue strength of carbon steel structures is applicable to stainless steels (see EN 1993-1-9).

Much can be done to reduce the susceptibility of a structure to fatigue by adopting good design practice. This involves judiciously selecting the overall structural configuration and carefully choosing constructional details that are fatigue resistant. The key to fatigue resistant design is a rational consideration of fatigue early in the design process. A fatigue assessment performed only after other design criteria have been satisfied may result in an inadequate or costly structure. It is also important to consider the needs of the fabricator and erector. It is therefore recommended that early consultations be held with them to point out areas of the structure which are most sensitive to fatigue cracking, to discuss special precautions and to become aware of fabrication and erection problems. In particular, the use of holes or lifting attachments to ease fabrication or erection should be considered during the fatigue evaluation.

It may be possible to eliminate potential fatigue problems by giving due regard to constructional details and avoiding:

- sharp changes in cross-section and stress concentrations in general
- misalignments and eccentricities
- small discontinuities such as scratches and grinding marks
- unnecessary welding of secondary attachments, e.g. lifting lugs
- partial penetration welds, fillet welds, intermittent welding, and backing strips
- arc strikes.

Although weld improvement techniques such as weld profile control, weld toe grinding, and shot and hammer peening may improve the fatigue strength of a joint, there are insufficient data to quantify the possible benefits for stainless steel. It should also be noted that the techniques are all labour-intensive and require skill and experience of the operator to achieve maximum benefit. They should not, except in special cases, be seen as a design option.
9 TESTING

9.1 General
Testing of stainless steel materials and members may be required for a number of reasons:

- If the design is to be based on actual material data (see Section 3.2.4).
- If advantage is to be taken of the strength enhancement of cold formed corners in members (see Sections 3.2.2 and 4.7.1).
- If the geometry of a member is such that it lies outside applicable limits (such as those given in Section 4.2).
- If a number of structures or components are to be based on prototype testing.
- If confirmation of consistency of production is required.

The usual precautions and requirements for test procedures and results evaluation appertaining to carbon steel testing also apply to stainless steel testing. It is therefore generally recommended that such requirements are consulted, e.g. see Section 5.2 and Annex D of EN 1990 and Section 9 and Annex A of EN 1993-1-3. However, there are particular aspects of the behaviour of stainless steels which need to be given more thought in the design of the tests than perhaps would be the case for carbon steels. The following brief guidance is offered.

9.2 Stress-strain curve determination
The applicable European Standard for material tests is EN 10002-1 Tensile testing of metallic materials. Method of test at ambient temperature. This standard does not give end details for the test coupons, although the diagrams suggest that the ends would be gripped. However, it is recommended that loading should be accomplished by pins passing through the ends of the coupon which are of sufficient area to sustain the shear. This is to ensure the coupon is axially loaded, thus enabling the actual shape of the stress-strain curve to be discerned without any spurious effect caused by premature yielding due to load eccentricity. Axiallity of loading may be confirmed by elastic tests with an extensometer placed at various orientations about the specimen.

Cognisance should be taken of strain-rate effects, see Section 3.2.2.

9.3 Tests on members
It is recommended that member tests should be full scale or as near to full scale as possible, depending on test facilities, and that the specimens should be manufactured by the same fabrication processes to be used in the final structure. If the components are welded, the prototype should be welded in the same way.

Since stainless steel may exhibit anisotropy, it is recommended that the specimens are prepared from the plate or sheet in the same orientation (i.e. transverse or parallel to the rolling direction) as intended for the final structure.
If the final orientation is unknown or cannot be guaranteed, it may be necessary to conduct tests for both orientations and take the less favourable set of results.

Stainless steel displays higher ductility and greater strain hardening than carbon steel and therefore the test rig capabilities may need to be greater than those required for testing carbon steel members of equivalent material yield strength. This not only applies to rig loading capacity but also to the ability of the rig to allow greater deformation of the specimen.

It should be noted that at higher specimen loads, the effects of creep become more manifest and this may mean that strain or displacement readings do not stabilise within a reasonable time.

For work hardened materials, both the tensile and compressive strength should be determined in the direction in question. Evaluation of the test results should be carried out with the relevant strength as reference.
10 FABRICATION ASPECTS

10.1 Introduction
The purpose of this Section is to highlight relevant aspects of stainless steel fabrication for the design engineer, including recommendations for good practice. It also allows a preliminary assessment to be made of the suitability of a fabricator to perform the work.

Stainless steel is not a difficult material to work with. However, in some respects it is different from carbon steel and should be treated accordingly. Many fabrication and joining processes are similar to those used for carbon steel, but the different characteristics of stainless steel require special attention in a number of areas. It is important that effective communication is established between the designer and fabricator early in the project to ensure that appropriate fabrication practices can and will be adopted.

An overriding objective is to maintain the steel’s corrosion resistance. It is essential that precautions are taken at all stages of storing, handling and forming to minimise influences that jeopardise the formation of the self-repairing passive layer. Special care must be taken to restore the full corrosion resistance of the welded zone. Although essential, the precautions are simple and, in general, are matters of good engineering practice.

It is important to preserve the good surface appearance of stainless steel throughout fabrication. Not only are surface blemishes unsightly, but they are usually unacceptable and prove time-consuming and expensive to correct. Whereas surface blemishes will normally be hidden by paint in carbon steel structures, this will only rarely be the case for stainless steel structures.

The structural form may be dictated by the availability of materials. It should be recognised that the available range of hot rolled stainless steel sections is more limited than for carbon steel. This results in a greater use of cold formed and welded members than is normally encountered. Also, because of brake press length capabilities, only relatively short lengths can be formed, which leads to an increased use of splices. In detailing joints, consideration should be given to clearances for bolts near bend radii and to potential fit up problems arising from weld distortion.

The guidance on fabrication and erection is in accordance with ENV 1090-6 Execution of steel structures. Supplementary rules for stainless steel. This standard is currently being converted into EN 1090 Execution of steel structures and aluminium structures. EN 1090-1 will give rules for using CE marks on steel structures. EN 1090-2 will include execution classes dependent on the type of steel structure; specific fabrication and erection requirements will correspond to the different execution classes. It is expected that EN 1090-2 will be submitted for final vote at the beginning of 2007.

The relevant standard for welding stainless steels is EN 1011-3 Welding. Recommendations for welding of metallic materials. Arc welding of stainless steels.
10.2 Storage and handling
Generally, greater care is required in storing and handling stainless steel than carbon steel to avoid damaging the surface finish (especially for bright annealed or polished finishes) and to avoid contamination by carbon steel and iron. Storage and handling procedures should be agreed between the relevant parties to the contract in advance of any fabrication and in sufficient detail to accommodate any special requirements. The procedures should cover, for instance, the following items:

- The steel should be inspected immediately after delivery for any surface damage.
- The steel may have a protective plastic or other coating. This should be left on as long as possible, removing it just before final fabrication. The protective covering should be called for in the procurement document if it is required (e.g. for bright annealed finishes).
- Storage in salt-laden humid atmospheres should be avoided. Storage racks should not have carbon steel rubbing surfaces and should, therefore, be protected by wooden, rubber or plastic battens or sheaths. Sheets and plates should preferably be stacked vertically; horizontally stacked sheets may get walked on with a risk of iron contamination and surface damage.
- Carbon steel lifting tackle, e.g. chains, hooks, and cleats should be avoided. Again, the use of isolating materials, or the use of suction cups, will prevent iron pick-up. The forks of fork lift trucks should also be protected.
- Contact with chemicals including undue amounts of oils and greases (which may stain some finishes) should be avoided.
- Ideally, segregated fabrication areas for carbon steel and stainless steel should be used. Only tools dedicated to stainless steel should be employed (this particularly applies to grinding wheels and wire brushes). Note that wire brushes and wire wool should be of stainless steel and generally in a grade that is equivalent in terms of corrosion resistance (e.g. do not use ferritic stainless steel brushes on austenitic stainless steel).
- As a precaution during fabrication and erection, it is advisable to ensure that any sharp burrs formed during shearing operations are removed.
- Consideration should be given to any requirements needed in protecting the finished fabrication during transportation.

10.3 Shaping operations
Austenitic stainless steels work harden significantly during cold working. This can be both a useful property, enabling extensive forming during stretch forming without risk of premature fracture, and a disadvantage, especially during machining when special attention to cutting feeds and speeds is required. The rate of work hardening differs with different grades, for example grade 1.4318 work hardens at a greater rate than other grades used in construction applications.

10.3.1 Cutting
Stainless steel is a relatively expensive material compared to some other metals and care is needed in marking out plates and sheets to avoid wastage in cutting.
Note that more wastage may result if the material has a polishing grain (or a unidirectional pattern) which has to be maintained in the fabrication. Some marking pens/crayons will prove difficult to remove, or cause staining, if used directly on the surface (rather than on any protective film); checks should be made that markers are satisfactory.

Stainless steel may be cut using usual methods, e.g. shearing and sawing, but power requirements will be greater than those for similar thicknesses of carbon steel, due to work hardening. If possible, cutting (and machining in general) should be carried out when the metal is in the annealed (softened) state, to limit work hardening and tool wear.

For cutting straight lines, guillotine shearing is widely used. By using open ended guillotines, a continuous cut greater in length than the shear blades can be achieved, although at the risk of introducing small steps in the cut edge.

Plasma arc techniques are also used and are particularly useful for cutting thick plates and profiles and where the cut edges are to be machined, e.g. for weld preparation. Oxyacetylene cutting is not satisfactory for cutting stainless steel, unless a powder fluxing technique is used.

10.3.2 Cold forming

Stainless steel is readily shaped by commonly used cold forming techniques such as bending, spinning, pressing and deep drawing. For structural applications press brake bending is the most relevant technique though, for high volume thin gauge products, roll forming may be more economic.

Again, the power requirement for bending stainless steel will be higher than for bending carbon steel due to work hardening (by about 50% in the case of the austenitic stainless steels or more in the case of duplex grades). Also, stainless steel has to be overbent to a slightly higher degree than carbon steel to counteract the effects of springback. For complex cross-sections, it is prudent to involve the fabricator as early as possible in the design.

Stainless steel’s high ductility allows small radii to be formed, perhaps as low as half the thickness in annealed materials. However, it is generally recommended to adopt the following internal radii as minima:

2t for austenitic grades
2,5t for duplex grades

where t is the thickness of the material.

When bending tubulars, the following guidance may be given:

- the outer tube diameter to wall thickness ratio should not exceed 15 (to avoid costly tooling).
- the bend radius (to centreline of tube) should not be less than 2,5d where d is the outer diameter
- any welding bead should be positioned close to the neutral axis to reduce the bending stresses at the weld.

10.3.3 Holes

Holes may be drilled or punched. In drilling, positive cutting must be maintained to avoid work hardening and this requires sharp bits with correct
angles of rake and correct cutting speeds. The use of a round tipped centre punch is not recommended as this work hardens the surface. Either a centre drill should be used or if a centre punch has to be used, it should be of the triangular pointed type. Punched holes can be made in austenitic stainless steel up to about 20 mm in thickness; the higher strength of duplex grades leads to a smaller limiting thickness. The minimum diameter of hole that can be punched out is 2 mm greater than the sheet thickness. Punched holes should be avoided in corrosive environments, due to the presence of the work hardened edge.

10.4 Welding

10.4.1 Introduction

The welding of austenitic and duplex stainless steels is widely and successfully carried out using normal processes, provided that suitable consumables are used. General cleanliness and the absence of contamination are important for attaining good weld quality. Oils or other hydrocarbons and wax crayon marks should be removed, to avoid their decomposition and the risk of carbon pick-up. The weld should be free from zinc, including that arising from galvanised products, and from copper and its alloys. (Care needs to be taken when copper backing bars are used; a groove should be provided in the bar immediately adjacent to the fusion area.)

It is more important in stainless steel than carbon steel to reduce sites at which crevice corrosion (see Section 3.7.2) may initiate. Welding deficiencies such as undercut, lack of penetration, weld spatter, slag and stray arc strikes are all potential sites and should thus be minimised. Stray arc strikes or arcing at loose earthing connections also damage the passive layer, and possibly give rise to preferential corrosion, thereby ruining the appearance of a fabrication.

Where the weld appearance is important, the engineer should specify the as-welded profile and surface condition required. This may influence the welding process selected or the post weld treatment. Consideration should also be given to the location of the weld; is it possible to apply the appropriate post weld treatment?

Heat input and interpass temperatures need to be controlled to minimise distortion (see Section 10.4.4) and to avoid potential metallurgical problems (see Section 10.4.5).

Welding should be carried out to an approved welding procedure according to a standard such as EN ISO 15609-1 Specification and qualification of welding procedures for metallic materials. Welding procedure specification. Arc welding. Welders should be approved in accordance with EN 287-1 Qualification test of welders. Fusion welding. Steels. Welding procedures contain the following elements:

- verification of the welding method by detailing the derivation and testing requirements of weld procedures
- the qualifications of welders
- the control of welding operations during preparation, actual welding and post-weld treatment
- the level of inspection and non-destructive testing techniques to be applied
the acceptance criteria for the permitted level of weld defects.

Provided that suitable procedures are followed, welding problems should not occur. However, the engineer should be aware that welding distortion is generally greater in stainless steel than in carbon steel, see Section 10.4.4.

Lock welding of the nut to the bolt should never be allowed, as the materials are formulated for strength and not for fusion welding.

10.4.2 Processes

As mentioned above, the common fusion methods of welding can be used on stainless steel. Table 10.1 shows the suitability of various processes for thickness ranges, etc. In MIG or TIG welding, the shielding gas should not contain carbon dioxide due to the possibility of decomposition leading to carbon pick-up and, in the case of duplex grades, nitrogen should be also avoided.

Table 10.1  Welding processes and their suitability

<table>
<thead>
<tr>
<th>Weld process (EN ISO 4063)</th>
<th>Suitable product forms</th>
<th>Types of welded joint</th>
<th>Material thickness range</th>
<th>Weld positions</th>
<th>Suitable shop/site conditions</th>
</tr>
</thead>
<tbody>
<tr>
<td>111 Metal arc welding with covered electrode (Manual metal arc)</td>
<td>All but not sheet</td>
<td>All</td>
<td>3 mm(^{(1)}) or greater</td>
<td>All</td>
<td>All</td>
</tr>
<tr>
<td>131 Metal arc inert gas (MIG)</td>
<td>All</td>
<td>All</td>
<td>2 mm(^{(1)}) or greater</td>
<td>All</td>
<td>All(^{(2)})</td>
</tr>
<tr>
<td>141 Tungsten inert gas (TIG)</td>
<td>All</td>
<td>All</td>
<td>Up to 10 mm maximum</td>
<td>All</td>
<td>All(^{(2)})</td>
</tr>
<tr>
<td>121/122 Submerged arc welding</td>
<td>All but not sheet</td>
<td>All</td>
<td>3 mm(^{(1)}) or greater</td>
<td>Downhand positions only</td>
<td>All</td>
</tr>
<tr>
<td>2 Resistance welding</td>
<td>Sheet only</td>
<td>All</td>
<td>3 mm maximum approximate</td>
<td>All</td>
<td>All</td>
</tr>
</tbody>
</table>

Notes:
1) Depends upon type of weld joint used.
2) More sensitive to weather than other processes and better environmental protection is required.

10.4.3 Consumables

Commercial consumables have been formulated to give weld deposits of equivalent strength and corrosion resistance to the parent metal and to minimise the risk of solidification cracking. For specialist applications, such as unusually aggressive environments or where non-magnetic properties are required, the advice of steel producers and manufacturers of consumables should be sought. All consumables should be kept free from contaminants and stored according to the manufacturer’s instructions.

All welding consumables should conform to the requirements specified in ENV 1090 (to be superseded by EN 1090-2). It is important that consumables are kept free from contaminants and stored according to the manufacturer’s instructions.
10.4.4 Welding distortion

In common with other metals, stainless steel suffers from distortion due to welding. The types of distortion (angular, bowing, shrinkage etc.) are similar in nature to those found in carbon steel structures. However, the distortion of stainless steel, particularly of austenitic grades, is greater than that of carbon steel because of higher coefficients of thermal expansion and lower thermal conductivities (which lead to steeper temperature gradients), see Section 3.3.

Welding distortion can only be controlled, not eliminated. The following actions may be taken by the designer and the fabricator:

**Designer actions**
- Remove the necessity to weld.
- Reduce the extent of welding.
- Reduce the area of welds. For instance in thick sections, specify double V, U or double U preparations in preference to single V.
- Use symmetrical joints.
- Design to accommodate wider dimensional tolerances.

**Fabricator actions**
- Use efficient clamping jigs. If possible the jig should incorporate copper or aluminium bars to help conduct heat away from the weld area.
- When efficient jigging is not possible, use closely spaced tack welds laid in a balanced sequence.
- Ensure that good fit up and alignment is obtained prior to welding.
- Use the lowest heat input commensurate with the selected weld process.
- Use balanced welding and appropriate sequences (e.g. backstepping and block sequences).

10.4.5 Metallurgical considerations

It is not possible to cover here the metallurgy of stainless steels except for some of the more significant factors.

**Formation of precipitates in the austenitic grades**

In the austenitic steels, the heat affected zone is relatively tolerant to grain growth and to the precipitation of brittle and intermetallic phases. Welding procedures are usually designed to control the time spent in the critical temperature range for precipitation effects (450 - 900°C). Excessive weld repair naturally increases the time spent and is thus usually restricted to three major repairs.

The formation of chromium carbide precipitates, and the ensuing loss of corrosion resistance, is discussed in Section 3.7.2 *Intergranular corrosion* where it is noted that this is not normally a problem with the low carbon grades of austenitic stainless steel (i.e. 1.4307 and 1.4404). However, weld decay effects may be manifested in the standard carbon grades in welded construction involving plate thickness greater than about 10 mm.
Solidification cracking in the austenitic grades

Solidification cracking of welds is avoided when the weld structure contains approximately 5% ferrite. Steelmakers balance the composition and heat treatment of the common grades of austenitic steel to ensure that they contain virtually no ferrite when delivered but will form sufficient ferrite in an autogenous weld (i.e. a weld with no filler added). Even so, to reduce any likelihood of cracking, it is prudent to minimise heat inputs, interpass temperatures and restraint when making autogenous welds. In thicker materials filler metal is added and the use of good quality consumables will again ensure the appropriate amount of ferrite is formed. It is not normally necessary to measure the precise amount of ferrite formed; appropriate weld procedures and consumables will ensure that solidification cracking will not occur.

Embrittlement of duplex grades

Duplex steels are sensitive to 475°C and σ-phase embrittlement. The former occurs when the steel is held within or cooled slowly through the approximate temperature range 550°C to 400°C and this produces an increase in tensile strength and hardness with a decrease in tensile ductility and impact strength. The latter might occur after a long exposure at a temperature in the range 565°C to 900°C but can occur in as short as half an hour under appropriate conditions (depending on the composition and the thermo-mechanical state of the steel). The effects of σ-phase embrittlement are greatest at room temperature. Both forms of embrittlement have an adverse effect on corrosion resistance and toughness.

Both 475°C and σ-phase embrittlement can be adequately controlled by adopting correct welding procedures; a maximum interpass temperature of 200°C is suggested. Particular care must be exercised when welding heavy sections.

To avoid embrittlement, long term exposure at temperatures above 300°C should be avoided.

10.4.6 Post weld treatment

It is best, both technically and commercially, to produce structures by welding. Post weld treatment is generally necessary, as discussed in the following paragraphs, especially if arc welding processes are involved. It is important to define the required post weld treatment for avoiding cost overruns and possible poor service performance. Finishing techniques common to all fabrications are covered in Section 10.6

The processes usually employed for weld dressing are wire brushing, and grinding. The amount of dressing should be minimised by the fabricator and if possible limited to wire brushing. This is because the heat produced in grinding can affect the corrosion resistance. Note that wire brushes should be made of stainless steel (see Section 10.2).

It is good practice to remove all traces of heat tint. However, yellow heat tint may prove satisfactory when the stainless steel offers a good margin of resistance for the particular environment. Where this is not so, or where the tint is not acceptable on aesthetic grounds, it may be removed by pickling or glass bead blasting. Pickling may be carried out by immersion in a bath (see Section 10.6) or by using pastes in accordance with the manufacturer’s instructions.
Peening the surface of a weld is a beneficial post weld treatment. It introduces compressive stresses into the surface which improves fatigue and stress corrosion cracking resistance and aesthetic appearances. However, peening cannot be used to justify a change in fatigue assessment.

The action of removing metal during substantial machining will give rise to stress relieving and hence distortion of the as-welded product. In those cases where the distortion is such that dimensional tolerances cannot be achieved, a thermal stress treatment will be required. Generally, this will only be an option for small sized components and only for grades which resist sensitisation (see Section 3.7.2) such as the low carbon grades 1.4307 and 1.4404 or the stabilised grades 1.4541 and 1.4571.

10.4.7 Inspection of welds

Table 10.2 shows the inspection methods commonly used on stainless steel welds and on carbon steel welds.

The methods are used as necessary depending on the degree of structural and corrosion integrity required for the environment under consideration. However, visual inspection should be carried out during all stages of welding as it can prevent many problems becoming troublesome as fabrication continues. Surface examination of stainless steel is more important than that of carbon steel, since stainless steel is primarily used to combat corrosion and even a small surface flaw can render the material liable to corrosion attack.

Table 10.2 Inspection methods for welds

<table>
<thead>
<tr>
<th>NDT type</th>
<th>Austenitic stainless steel</th>
<th>Duplex stainless steel</th>
<th>Carbon steel</th>
</tr>
</thead>
<tbody>
<tr>
<td>Surface</td>
<td>Visual DPI</td>
<td>Visual DPI</td>
<td>Visual DPI</td>
</tr>
<tr>
<td></td>
<td></td>
<td>MPI MPI</td>
<td>MPI MPI</td>
</tr>
<tr>
<td>Volumetric</td>
<td>X-ray Gamma</td>
<td>X-ray Gamma</td>
<td>X-ray Gamma</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Ultrasonics</td>
</tr>
</tbody>
</table>

DPI – Dye penetrant inspection
MPI – Magnetic particle inspection

Magnetic particle inspection is not an option for the austenitic steels since these are non-magnetic. Ultrasonic methods are of limited use on welds because of difficulties in interpretation; however, they can be used on parent material. Gamma radiography is not suitable for detecting cracking or lack of fusion in stainless steel materials less than 10 mm thick.

10.5 Galling and seizure

If surfaces are under load and in relative motion, galling may result from local adhesion and rupture of the surfaces. In some cases weld bonding and seizure may result. The following methods may be used to avoid galling problems:

- Use dissimilar standard grades of stainless steel (grades which differ in composition, work hardening rate and hardness) For example use grade A2-C2, A4-C4 or A2-A4 bolt-nut combinations from EN ISO 3506
• In severe cases, use a proprietary high work-hardening stainless steel alloy for one component or apply a hard surface coating

• Use anti-galling agents.

Note that if dissimilar steels or coatings are used, it is necessary to ensure that the required corrosion resistance is obtained. Greasing bolts is beneficial but may result in contamination by dirt and can present problems for storage.

It is recommended that bolting material should be in the cold worked condition, property class 70 minimum (see Table 3.3). Bolting materials should not be used in the softened condition because of the propensity for galling. Using rolled as opposed to machined threads and avoiding the use of fine threads and tight fitting thread forms reduces the likelihood of galling.

10.6 Finishing

The surface finish of stainless steel is an important design criterion and should be clearly specified according to architectural or functional requirements. The finer the finish, the greater the cost. This is where precautions taken earlier in handling and welding will pay off. Initial planning is important in reducing costs. For instance, if a tube to tube weld in a handrail or balustrade is hidden inside an upright, there will be a reduced finishing cost and a significant improvement in the final appearance of the handrail.

The surface of the steel should be restored to its corrosion resisting condition by removing all scale and contamination. Pickling in an acid bath will loosen any scale, enabling it to be brushed off with a bristle brush, and also dissolve any embedded iron or carbon steel particles.

Abrasive treatments, such as grinding, finishing, polishing and buffing, produce unidirectional finishes and thus the blending of welds may not be easy on plates/sheets with normal rolled surfaces. A degree of experimentation may be required to determine detailed procedures to obtain a suitable finish.

Electrolytic polishing removes a thin surface layer. A range of finishes from dull to a bright lustre can be produced, depending largely on the initial surface of the material.

There are other finishing processes (electroplating, tumbling, etching, colouring, and surface blackening) but these would only rarely be used for structural stainless steel and so are not described here.

It is worth noting again that the surface should be free of contaminants in the assembled structure. Particular consideration should be given to the possibility of contamination arising from work on adjacent carbon steelwork, especially from grinding dust. Either the stainless steel should be protected by removable plastic film, or final cleaning after completion of the structure should be specified in the contract documents.
APPENDIX A  Correlation between stainless steel designations

Table A.1. gives the correlations between EN 10088, German, UK, French, Italian, Swedish, Spanish and US designations.
<table>
<thead>
<tr>
<th>Steel grade to EN 10088</th>
<th>Germany (DIN)</th>
<th>UK</th>
<th>France</th>
<th>Italy</th>
<th>Sweden</th>
<th>Spain</th>
<th>USA</th>
</tr>
</thead>
<tbody>
<tr>
<td>Name No.</td>
<td>BSI</td>
<td>AFNOR</td>
<td>UNI</td>
<td>SIS</td>
<td>UNE</td>
<td>AISI</td>
<td>UNS</td>
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<td>X5 CrNi 18 10</td>
<td>1.4301</td>
<td>304 S 15</td>
<td>304 S 16</td>
<td>Z 6 CN 18-09</td>
<td>X5 CrNi 18 10</td>
<td>2332</td>
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<tr>
<td>X2CrNi19-11 1.4306</td>
<td>X2 CrNi 19 11</td>
<td>1.4306</td>
<td>304 S 11</td>
<td>Z 2 CN 18-10</td>
<td>X2 CrNi 18 11</td>
<td>2352</td>
<td>3503</td>
</tr>
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<td>X2CrNi18-9 1.4307</td>
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<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>X6CrNiTi18-10 1.4541</td>
<td>X6 CrNiTi 18 10</td>
<td>1.4541</td>
<td>321 S 31</td>
<td>Z 6 CNT 18-10</td>
<td>X6 CrNiTi 18 11</td>
<td>2337</td>
<td>3523</td>
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<td>X5CrNiMo 17 12 2</td>
<td>1.4401</td>
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<td>Z 6 CND 17-11</td>
<td>X5 CrNiMo 17 12</td>
<td>2347</td>
<td>3534</td>
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<td>X2CrNiMo 17 13 2</td>
<td>1.4404</td>
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<td>Z 2 CND 17-12</td>
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<td>-</td>
<td>-</td>
</tr>
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<td>X2 CrNiMo 18 14 3</td>
<td>1.4435</td>
<td>316 S 13</td>
<td>Z 2 CND 17-13</td>
<td>X2 CrNiMo 17 13</td>
<td>2353</td>
<td>3533</td>
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<td>X1 NiCrMoCuN 25 20 5</td>
<td>1.4539</td>
<td>-</td>
<td>Z 1 CNDU 25-20</td>
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<td>2562</td>
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<td>X6 CrNiMoTi 17 12</td>
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<td>X2 CrNiMoN 17 12 2</td>
<td>1.4406</td>
<td>316 S 62</td>
<td>Z 2 CND 17-12 Az</td>
<td>-</td>
<td>-</td>
<td>316 LN</td>
</tr>
<tr>
<td>X2CrNiMo11-13-5 1.4439</td>
<td>X2 CrNiMoN 17 13 5</td>
<td>1.4439</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>317 LMN</td>
<td>S 31726</td>
</tr>
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<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
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<td>X2 CrNiN 18 7</td>
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<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>301 LN (302 LN)</td>
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<td>1.4462</td>
<td>Duplex 2205</td>
<td>Z 2 CND 22-5 Az</td>
<td>-</td>
<td>2377</td>
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APPENDIX B  Lateral-torsional buckling

B.1 General Case

The elastic critical moment for lateral-torsional buckling, $M_{cr}$, for a beam of uniform cross-section, is given by:

$$M_{cr} = C_1 \frac{\pi^2 EI_z}{(k_z L)^2} \left[ \left( \frac{k_z}{k_w} \right)^2 \frac{I_w}{I_z} + \frac{(k_z L)^2 GI_z}{\pi^2 EI_z} + (C_2 z_g - C_3 z_j)^2 \right]^{1/2} - (C_2 z_g - C_3 z_j)$$

where:

- $C_1$, $C_2$ and $C_3$ are factors depending on loading and end restraint conditions, see Tables B.1 and B.2.
- $I_t$ is the torsion constant
- $I_w$ is the warping constant
- $I_z$ is the second moment of area about minor axis
- $k_z$ and $k_w$ are effective length factors
- $L$ is the length of beam between points which have lateral restraint
- $z_g = z_a - z_s$
- $z_a$ is the co-ordinate of point of load application
- $z_s$ is the co-ordinate of the shear centre
- $z_j = \frac{\int z (y^2 + z^2) dA}{2 I_y}$

In evaluating $z_j$, $z$ is negative for the compression flange; $z_j$ is positive when the flange with the larger value of $I_z$ is in compression at the point of largest moment. Note that $z_j = 0$ for any equal flanged section including channels and z-shapes.

For gravity loads $z_g$ is negative for loads applied above the shear centre. In the general case, $z_g$ is negative for loads acting towards the shear centre from their point of load application. Note that if the load is restrained from moving sideways with the beam then $z_g = 0$.

The effective length factors $k_z$ and $k_w$ vary from 0,5 for full fixity to 1,0 for no fixity, with 0,7 for one end fixed and one end free. The normal conditions of restraint at each end are:

$$k_z = k_w = 1,0$$

- restrained against lateral movement, free to rotate on plan
- restrained against rotation about the longitudinal axis, free to warp

The factor $k_z$ refers to end rotation on plan. It is analogous to the ratio $l/L$ for a compression member. The factor $k_w$ refers to end warping. Unless special provision for warping fixity is made, $k_w$ should be taken as 1,0.
### Table B.1  \textit{Values of factors }C_1\textit{ and }C_3\textit{ corresponding to values of effective length factor }k_z\textit{: End moment loading}

<table>
<thead>
<tr>
<th>End moments and support conditions</th>
<th>Bending moment diagram</th>
<th>Value of ( k_z )</th>
<th>Values of factors</th>
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<tbody>
<tr>
<td></td>
<td>( \psi = +1 )</td>
<td>1,0</td>
<td>1,00</td>
</tr>
<tr>
<td></td>
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<td>0,5</td>
<td>1,05</td>
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<td></td>
<td>( \psi = +\frac{3}{4} )</td>
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</tr>
<tr>
<td></td>
<td></td>
<td>0,5</td>
<td>1,19</td>
</tr>
<tr>
<td></td>
<td>( \psi = +\frac{1}{2} )</td>
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<td>1,31</td>
</tr>
<tr>
<td></td>
<td></td>
<td>0,5</td>
<td>1,37</td>
</tr>
<tr>
<td></td>
<td>( \psi = +\frac{1}{4} )</td>
<td>1,0</td>
<td>1,52</td>
</tr>
<tr>
<td></td>
<td></td>
<td>0,5</td>
<td>1,60</td>
</tr>
<tr>
<td></td>
<td>( \psi = 0 )</td>
<td>1,0</td>
<td>1,77</td>
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<tr>
<td></td>
<td></td>
<td>0,5</td>
<td>1,86</td>
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<td>( \psi = -\frac{1}{4} )</td>
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<td>2,06</td>
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<tr>
<td></td>
<td></td>
<td>0,5</td>
<td>2,15</td>
</tr>
<tr>
<td></td>
<td>( \psi = -\frac{1}{2} )</td>
<td>1,0</td>
<td>2,35</td>
</tr>
<tr>
<td></td>
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<td>2,42</td>
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<td>( \psi = -\frac{3}{4} )</td>
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<td>2,57</td>
</tr>
<tr>
<td></td>
<td>( \psi = -1 )</td>
<td>1,0</td>
<td>2,60</td>
</tr>
<tr>
<td></td>
<td></td>
<td>0,5</td>
<td>2,45</td>
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</tbody>
</table>

\( \psi_f \) = \text{Effective length factor}
Table B.2  \emph{Values of factors $C_1$, $C_2$ and $C_3$ corresponding to values of effective length factor $k_z$: Transverse loading cases}

<table>
<thead>
<tr>
<th>Loading and support conditions</th>
<th>Bending moment diagram</th>
<th>Value of $k_z$</th>
<th>Value of factors $C_1$</th>
<th>$C_2$</th>
<th>$C_3$</th>
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<tr>
<td></td>
<td></td>
<td>1,0</td>
<td>1,12</td>
<td>0,45</td>
<td>0,525</td>
</tr>
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<td></td>
<td></td>
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<td>0,97</td>
<td>0,36</td>
<td>0,478</td>
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<tr>
<td></td>
<td></td>
<td>1,0</td>
<td>1,35</td>
<td>0,59</td>
<td>0,411</td>
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<td></td>
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<td>0,5</td>
<td>1,05</td>
<td>0,48</td>
<td>0,338</td>
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<td></td>
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<td>1,04</td>
<td>0,42</td>
<td>0,562</td>
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<td></td>
<td></td>
<td>0,5</td>
<td>0,95</td>
<td>0,31</td>
<td>0,539</td>
</tr>
</tbody>
</table>

Note that Tables B.1 and B.2 may be used only for the case of monosymmetrical I profiles for which $-0,9 \leq \psi_f \leq 0,9$

where:

$$\psi_f = \frac{I_{fc} - I_{ft}}{I_{fc} + I_{ft}}$$

in which:

$I_{fc}$ is the second moment of area of the compression flange about the minor axis of the cross-section

$I_{ft}$ is the second moment of area of the tension flange about the minor axis of the cross-section

$\psi_f = 0$ for bi-symmetric cross-sections

$\psi_f > 0$ for mono-symmetric cross-sections when the larger flange is in compression

$\psi_f < 0$ for monosymmetric cross-sections when the smaller flange is in compression

The following approximations for $z_j$ can be used:

$$z_j = 0,8\psi_f \frac{h_s}{2} \quad \text{when} \quad \psi_f \geq 0$$

$$z_j = \psi_f \frac{h_s}{2} \quad \text{when} \quad \psi_f < 0$$

where:

$h_s$ is the distance between the shear centres of the flanges.
B.2 Specific Cases

B.2.1 Bi-symmetric cross-sections

The elastic critical moment for lateral torsional buckling of a beam of uniform symmetrical cross-section with equal flanges, \( z_j = 0 \):

\[
M_{cr} = C_1 \frac{\pi^2 EI_z}{(k_z L)^2} \left[ \left( \frac{k_z}{k_w} \right)^2 \frac{I_w}{I_z} + \frac{(k_z L)^2}{\pi^2 EI_z} \left( C_2 z_g \right)^2 \right]^{-1/2} - C_2 z_g
\]

For end-moment loading and transverse loads applied at the shear centre \( C_2 z_g = 0 \). For these cases:

\[
M_{cr} = C_1 \frac{\pi^2 EI_z}{(k_z L)^2} \left[ \left( \frac{k_z}{k_w} \right)^2 \frac{I_w}{I_z} + \frac{(k_z L)^2}{\pi^2 EI_z} \right]^{1/2}
\]

For normal conditions of restraint at each end, \( k_z = k_w = 1,0 \):

\[
M_{cr} = C_1 \frac{\pi^2 EI_z}{L^2} \left[ \frac{I_w}{I_z} + \frac{L^2 GI_t}{\pi^2 EI_z} \right]^{1/2}
\]
APPENDIX C  Material data for deflection calculations

The secant modulus, $E_S$, to be used in deflection calculations (see Section 5.4.6) should be ascertained for the member with respect to the rolling direction. If the orientation is not known, or cannot be ensured, then the value for the longitudinal directions should be used.

The value of the secant modulus may be obtained as follows:

$$E_S = \frac{(E_{S1} + E_{S2})}{2}$$

where:

- $E_{S1}$ is the secant modulus corresponding to the stress in the tension flange
- $E_{S2}$ is the secant modulus corresponding to the stress in the compression flange.

Values of the secant moduli $E_{S1}$ and $E_{S2}$ for the appropriate orientation and serviceability design stress can be estimated from the following equation using the constants given in Table C.1. Alternatively, values for grades 1.4301, 1.4401 and 1.4462 may be taken from Table C.2 using linear interpolation as necessary.

$$E_{S,i} = \frac{E}{1 + 0.002 \frac{E}{\sigma_{i,Ed,ser}} \left( \frac{\sigma_{i,Ed,ser}}{f_y} \right)^n} \quad \text{and } i = 1,2$$

where:

- $\sigma_{i,Ed,ser}$ is the serviceability design stress in the tension or compression flange
- $E = 200\,000$ N/mm$^2$.

As a simplification, the variation of $E_S$ along the length of the member may be neglected and the minimum value of $E_S$ for that member (corresponding to the maximum values of the stresses $\sigma_1$ and $\sigma_2$ in the member) may be used throughout its length.
Table C.1  Values of constants to be used for determining secant moduli

<table>
<thead>
<tr>
<th>Grade</th>
<th>$f_y$ N/mm²</th>
<th>$n$</th>
<th>Longitudinal direction</th>
<th>Transverse direction</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.4301</td>
<td>210</td>
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<td></td>
</tr>
<tr>
<td>1.4307</td>
<td>200</td>
<td>6,0</td>
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<td>8,0</td>
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<td>1.4541</td>
<td>200</td>
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<tr>
<td>1.4318</td>
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<td>1.4401</td>
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<td>1.4362</td>
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<tr>
<td>1.4462</td>
<td>460</td>
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</tr>
</tbody>
</table>

Table C.2  Secant moduli for deflection calculations for grades 1.4301, 1.4401 and 1.4462

<table>
<thead>
<tr>
<th>Stress ratio ($\sigma/f_y$)</th>
<th>Secant modulus (kN/mm²)</th>
<th>Grade 1.4301</th>
<th>Grade 1.4401</th>
<th>Grade 1.4462</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Longitudinal direction</td>
<td>Transverse direction</td>
<td>Longitudinal direction</td>
<td>Transverse direction</td>
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<td>0,00</td>
<td>200</td>
<td>200</td>
<td>200</td>
<td>200</td>
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<tr>
<td>0,20</td>
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<td>200</td>
<td>200</td>
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<tr>
<td>0,25</td>
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<td>200</td>
<td>200</td>
<td>199</td>
</tr>
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<td>0,30</td>
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<tr>
<td>0,35</td>
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<tr>
<td>0,76</td>
<td>141</td>
<td>161</td>
<td>148</td>
<td>166</td>
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</tbody>
</table>
PART II – DESIGN EXAMPLES

This section gives thirteen design examples that illustrate the application of the design rules. The examples are:

*Design example 1*
A circular hollow section subject to axial compression.

*Design example 2*
A welded I-beam with a Class 4 cross-section subject to combined axial compression and bending.

*Design example 3*
Trapezoidal roof sheeting with a Class 4 cross-section subject to bending.

*Design example 4*
A welded hollow section joint subject to fatigue loading.

*Design example 5*
A welded joint.

*Design example 6*
A bolted joint.

*Design example 7*
A plate girder with a Class 4 cross-section subject to bending. Shear buckling is critical.

*Design example 8*
A plate girder with a Class 4 cross-section subject to bending. Resistance to transverse loads is critical.

*Design example 9*
A cold formed channel subject to bending with intermediate lateral restraints to the compression flange. Lateral torsional buckling between intermediate lateral restraints is critical.

*Design example 10*
A rectangular hollow section subject to combined axial compression and bending with 30 minutes fire resistance.

*Design example 11*
Trapezoidal roof sheeting with a Class 4 cross-section subject to bending – a comparison of designs with cold worked material and annealed material.

*Design example 12*
A lipped channel from cold worked material in an exposed floor subject to bending.
Design example 13

A stainless steel lattice girder from cold worked material subject to combined axial compression and bending with 30 minutes fire resistance.

The plate girders in examples 7 and 8 are from duplex grade 1.4462. The members in the other examples are from austenitic grades 1.4301 or 1.4401.

The references in the margin of the design examples are to text sections and expressions/equations in this publication, unless specifically noted otherwise.
DESIGN EXAMPLE 1 – CHS COLUMN

The circular hollow section column to be designed is an interior column of a multi-storey building. The column is simply supported at its ends. The inter-storey height is 3,50 m.

Structure
Simply supported column, length between supports:
\[ l = 3,50 \text{ m} \]

Actions
Permanent and variable actions result into a vertical design compression force equal to:
\[ N_{Ed} = 250 \text{ kN} \]

Cross-section properties
Try a 159 × 4 CHS, grade 1.4401
Geometric properties
\[ d = 159 \text{ mm} \quad t = 4 \text{ mm} \]
\[ A = 19,5 \text{ cm}^2 \quad I = 585,3 \text{ cm}^4 \]
\[ W_{el} = 73,6 \text{ cm}^3 \quad W_{pl} = 96,1 \text{ cm}^3 \]

Material properties
0,2% proof stress = 220 N/mm². Take \( f_y = 220 \text{ N/mm}^2 \).
\[ E = 200 000 \text{ N/mm}^2 \quad \text{and} \quad G = 76 900 \text{ N/mm}^2 \]

Classification of the cross-section
\[ \varepsilon = 1,01 \]
Section in compression: \[ \frac{d}{t} = \frac{159}{4} = 39,8 \]
For Class 1, \( \frac{d}{t} \leq 50 \epsilon^2 \), therefore the section is Class 1.

**Compression resistance of the cross-section**

For a Class 1 cross-section:

\[
N_{c,Rd} = \frac{A_g f_y}{\gamma_{M0}}
\]

\[
N_{c,Rd} = \frac{19.5 \times 220 \times 10^{-1}}{1.1} = 390 \text{ kN}
\]

**Resistance to flexural buckling**

\[
N_{b,Rd} = \chi A f_y / \gamma_{M1}
\]

\[
\varphi = 0.5 \left( 1 + \alpha (\bar{\lambda} - \bar{\lambda}_0) + \bar{\lambda}^2 \right)
\]

\[
\chi = \frac{1}{\varphi + \left[ \varphi^2 - \bar{\lambda}^2 \right]^{0.5}} \leq 1
\]

\[
\bar{\lambda} = \frac{A f_y}{\sqrt{N_{cr}}}
\]

Determine the elastic critical buckling load:

\[
N_{cr} = \pi^2 EI / L^2_{cr} = \frac{\pi^2 \times 200000 \times 585.3 \times 10^4 \times 10^{-3}}{(350 \times 10^3)^2} = 943.1 \text{ kN}
\]

Determine the flexural buckling slenderness:

\[
\bar{\lambda} = \sqrt{\frac{19.5 \times 10^2 \times 220}{943.1 \times 10^3}} = 0.67
\]

Using an imperfection factor \( \alpha = 0.49 \) and \( \bar{\lambda}_0 = 0.4 \) for hollow sections:

\[
\varphi = 0.5 \left( 1 + 0.49 (0.67 - 0.4) + 0.67^2 \right) = 0.79
\]

\[
\chi = \frac{1}{0.79 + \left[ 0.79^2 - 0.67^2 \right]^{0.5}} = 0.83
\]

\[
N_{b,Rd} = 0.83 \times 19.5 \times 220 \times 10^{-1} / 1.1 = 323.7 \text{ kN}
\]

The applied axial load is \( N_{Ed} = 250 \text{ kN} \).

Thus the member has adequate resistance to flexural buckling.
DESIGN EXAMPLE 2 – WELDED I-SECTION BEAM-COLUMN WITH LATERAL RESTRAINTS

The beam-column to be designed is a welded I-section, simply supported at its ends. Minor axis buckling is prevented by lateral restraints. The inter-storey height is equal to 3.50 m. The column is loaded by a vertical single load with an eccentricity.

Structure
Simply supported column, length between supports:
\[ l = 3.50 \text{ m} \]
Eccentricity of the load:
\[ e = 20 \text{ cm} \]

Actions
Permanent and variable actions result in a vertical design compression force equal to:
\[ N_{Ed} = 120 \text{ kN} \]

Structural analysis
Maximum bending moment occurs at the top of the column:
\[ M_{y,\text{max Ed}} = 120 \times 0.20 = 24 \text{ kNm} \]

Cross section properties
Try a bi-symmetric welded I-section 200 × 200, thickness = 6 mm, grade 1.4401

Geometric properties
\[ b = 200 \text{ mm} \quad t_f = 6 \text{ mm} \quad W_{el,y} = 259.1 \text{ cm}^3 \]
\[ h_w = 188 \text{ mm} \quad t_w = 6 \text{ mm} \quad W_{pl,y} = 285.8 \text{ cm}^3 \]
\[ a = 3 \text{ mm (weld thickness)} \quad I_y = 2591.1 \text{ cm}^4 \]
\[ A_g = 35.3 \text{ cm}^2 \quad i_y = 8.6 \text{ cm} \]
Material properties

$0.2\%$ proof stress $= 220 \text{ N/mm}^2$. Take $f_y = 220 \text{ N/mm}^2$

$E = 200\,000 \text{ N/mm}^2$ and $G = 76\,900 \text{ N/mm}^2$

Classification of the cross-section

$\varepsilon = 1.01$

Web subject to compression: $\frac{c}{t} = \frac{188 - 3 - 3}{6} = 30.3$

For Class 3, $\frac{c}{t} \leq 30.7 \varepsilon$, therefore web is Class 3 (at least)

Outstand flange subject to compression: $\frac{c}{t} = \frac{200 / 2 - 6 / 2 - 3}{6} = \frac{94}{6} = 15.7$

For Class 3, $\frac{c}{t} \leq 11.0 \varepsilon$, therefore outstand flange is Class 4

Therefore, overall classification of cross-section is Class 4

Effective section properties

Calculate reduction factor $\rho$ for welded outstand elements

$\rho = \frac{1}{\bar{\lambda}_p} - \frac{0.242}{\bar{\lambda}_p^2} \leq 1$

$\bar{\lambda}_p = \frac{\bar{b}/t}{28.4 \varepsilon \sqrt{\kappa_\sigma}}$ where $\bar{b} = c = 94 \text{ mm}$

Assuming uniform stress distribution within the compression flange,

$\psi = \frac{\sigma_2}{\sigma_1} = 1$

$\Rightarrow \kappa_\sigma = 0.43$

$\bar{\lambda}_p = \frac{94 / 6}{28.4 \times 1.01 \times \sqrt{0.43}} = 0.833$

$\rho = \frac{1}{\bar{\lambda}_p} - \frac{0.242}{\bar{\lambda}_p^2} = \frac{1}{0.833} - \frac{0.242}{0.833^2} = 0.852$

$b_{\text{eff}} = 0.852 \times 94$

$= 80.1 \text{ mm}$

Calculate effective cross-section for compression only
\[ A_{\text{eff}} = A_g - 4 \times (1 - \rho) c t = 35,3 - 4 \times (1 - 0.852) \times 94 \times 6 \times 10^{-2} = 31.9 \text{ cm}^2 \]

Calculate effective cross-section for major axis bending

\[ A_{\text{eff}} = A_g - 2 \times (1 - \rho) c t = 35,3 - 2 \times (1 - 0.852) \times 94 \times 6 \times 10^{-2} = 33.6 \text{ cm}^2 \]

Taking area moments about the neutral axis of the gross cross-section, calculate the shift in the position of the neutral axis:

\[
\zeta' = \frac{2 \times (1 - \rho) c t \times (h_w + t_f)}{2 A_{\text{eff}}} = \frac{2 \times (1 - 0.852) \times 94 \times 6 \times (188 + 6)}{33.6 \times 10^4} = 4.8 \text{ mm shifted in the direction away from the compression flange}
\]

Calculate effective 2nd moment of inertia for major axis bending

\[
I_{y,\text{eff}} = I_y - 2 \times (1 - \rho) c t \times \left[ \frac{t^2}{12} + \frac{(h_w + t_f)^2}{4} \right] - \zeta'^2 A_{\text{eff}}
\]

\[
= 2591,1 - 2 \times (1 - 0.852) \times 94 \times 6 \times \left[ \frac{6^2}{12} + \frac{(188 + 6)^2}{4} \right] \times 10^{-4} - (4.8)^2 \times 33.6 \times 10^{-2}\n\]

\[= 2426.2 \text{ cm}^4\]

And

\[
W_{\text{eff},y} = \frac{I_{y,\text{eff}}}{h_w / 2 + t_f + \zeta'} = \frac{2426.2}{18.8 / 2 + 0.6 + 0.48} = 231.5 \text{ cm}^3
\]

Resistance to major axis flexural buckling

\[ N_{b,Rd} = \chi A_{\text{eff}} f_y / f_{y,M1} \]

\[ A_{\text{eff}} = 31.9 \text{ cm}^2 \text{ for Class 4 cross-section subject to compression} \]

\[ \chi = \frac{1}{\phi + \left( \phi^2 - \lambda^2 \right)^{0.5}} \leq 1 \]

\[ \phi = 0.5 \left( 1 + \alpha (\lambda - \lambda_0) + \lambda^2 \right) \]

\[ \overline{\lambda} = \sqrt{\frac{A_{\text{eff}} f_y}{N_{cr}}} \]

\[ I = 350 \text{ cm} \text{ (buckling length is equal to actual length)} \]

\[
N_{cr} = \frac{\pi^2 EI}{l^2} = \frac{\pi^2 \times 200000 \times 2591.1 \times 10^4 \times 10^{-3}}{350^2 \times 10^2} = 4175.2 \text{ kN}
\]

\[ \overline{\lambda} = \sqrt{\frac{31.9 \times 10^2 \times 220}{4175.2 \times 10^3}} = 0.410 \]
Using imperfection factor $\alpha = 0.49$ and initial slenderness $\lambda_0 = 0.2$ for welded open sections, major axis bending:

$$\varphi = 0.5(1 + 0.49(0.410 - 0.2) + 0.410^2) = 0.636$$

$$\chi = \frac{1}{0.636 + \left[0.636^2 - 0.410^2\right]^{0.5}} = 0.891$$

$$N_{b,y,Rd} = 0.891 \times 31.9 \times 10^2 \times 220 \times 10^{-3} / 1.1 = 568.46 \text{ kN}$$

**Resistance to axial compression and uniaxial major axis moment**

$$\frac{N_{Ed}}{(N_{b,Rd})_{\min}} + k_y \frac{M_{y,Ed} + N_{Ed} e_{Ny}}{\beta_{W,y} W_{pl,y} f_y / \gamma_{M1}} \leq 1$$

$$\beta_{W,y} = W_{eff} / W_{pl,y} \text{ for a Class 4 cross-section}$$

$$= 231.5 / 285.8 = 0.810$$

$e_{Ny}$ is zero, due to the symmetry of the cross-section

$$k_y = 1.0 + 2(\lambda_y - 0.5) \frac{N_{Ed}}{N_{b,Rd,y}} = 1.0 + 2(0.410 - 0.5) \frac{120.0}{568.46} = 0.962$$

$$1.2 + \frac{2N_{Ed}}{N_{b,Rd,y}} = 1.2 + \frac{2 \times 120}{568.46} = 1.62$$

but $1.2 \leq k_y \leq 1.62$

Therefore, $k_y = 1.2$

$$\frac{120.0}{568.46} + 1.2 \frac{24.0 \times 10^6}{0.81 \times 285.8 \times 10^3 \times 220 / 1.1} = 0.833 \leq 1$$

Thus the member has adequate resistance.
DESIGN EXAMPLE 3 – DESIGN OF A TWO-SPAN TRAPEZOIDAL ROOF SHEETING

This example considers the design of a two-span trapezoidal roof sheeting. The material is grade 1.4401 stainless steel and the material thickness is 0.6 mm. The dimensions of the cross section are shown below.

The example shows the following design tasks:
- determination of effective section properties at the ultimate limit state
- determination of the bending resistance of the section
- determination of the resistance at the intermediate support
- determination of deflections at serviceability limit state.

This example refers to prEN 1993-1-3:2005 and adopts its symbols and terminology. Reference should be made to prEN 1993-1-3 for a full description of the design procedures and associated figures.

Design data

<table>
<thead>
<tr>
<th>Spans</th>
<th>$L = 2900$ mm</th>
</tr>
</thead>
<tbody>
<tr>
<td>Width of supports</td>
<td>$s_s = 100$ mm</td>
</tr>
<tr>
<td>Design load</td>
<td>$Q = 1.4$ kN/m$^2$</td>
</tr>
<tr>
<td>Design thickness</td>
<td>$t = 0.6$ mm</td>
</tr>
<tr>
<td>Yield strength</td>
<td>$f_{yb} = 240$ N/mm$^2$</td>
</tr>
<tr>
<td>Modulus of elasticity</td>
<td>$E = 200\ 000$ N/mm$^2$</td>
</tr>
<tr>
<td>Partial safety factor</td>
<td>$\gamma_{M0} = 1,1$</td>
</tr>
<tr>
<td>Partial safety factor</td>
<td>$\gamma_{M1} = 1,1$</td>
</tr>
</tbody>
</table>

Symbols and detailed dimensions used in calculations are shown in the figure below. The position of the cross section is given so that in bending at the support the upper flange is compressed.
CALCULATION SHEET

Job Title: ECSC Stainless Steel Valorisation Project

Subject: Design Example 3 – Design of a two-span trapezoidal roof sheeting

Client: ECSC

Made by: AAT  Date: June 2002

Checked by: JEK  Date: June 2002

Revised by: JBL/MEB  Date: April 2006

Centre line dimensions

\[ h_0 = 70 \text{ mm} \]
\[ w_0 = 212,5 \text{ mm} \]
\[ b_{su} = 65 \text{ mm} \]
\[ b_{s0} = 57 \text{ mm} \]
\[ b_{su} = 20 \text{ mm} \]
\[ b_{s0} = 8 \text{ mm} \]
\[ h_{su} = 6 \text{ mm} \]
\[ b_{k} = 20 \text{ mm} \]
\[ b_{k0} = 8 \text{ mm} \]
\[ h_{k} = 6 \text{ mm} \]

Internal radius of the corners \( r = 3 \text{ mm} \)

\[ \theta = \arctan \left( \frac{h_0}{0,5(w_0 - b_{s0} - b_{l0})} \right) = 57,1 \text{ deg} \]

EFFECTIVE SECTION PROPERTIES AT THE ULTIMATE LIMIT STATE

Check on maximum width-to-thickness ratios:
\[ \frac{h_0}{t} = 117 \text{ is less than } 400 \sin \theta = 336 \text{ and} \]
\[ \frac{b_{l0}}{t} = 95 \text{ is less than } 400. \]

Location of the centroidal axis when the web is fully effective

Effective width of the compressed flange:
\[ b_p = \frac{b_{s0} - b_{su}}{2} = 22,5 \text{ mm} \]
\[ \varepsilon = \left[ \frac{235}{f_y} \frac{E}{210,000} \right]^{0,5} = 0,966 \]

\[ k_{\sigma} = 4 \]
\[ \chi_p = \frac{b_p / t}{28,4 \varepsilon^{k_{\sigma}}} = 0,684 \]

\[ \rho = \frac{0,772}{\chi_p} - \frac{0,125}{\chi_p^2} = 0,862 \]

Because \( \rho < 1 \), \( b_{eff,0} = \rho b_p = 19,4 \text{ mm} \)

Reduced thickness of the flange stiffener:
\[ t_{su} = \sqrt{\frac{h_{su}^2 + \left( \frac{b_{su} - b_{s0}}{2} \right)^2}{h_{su}}} t = 0,849 \text{ mm} \]
\[ A_s = (b_{eff,u} + b_{su0})t + 2h_{su}t = 26,6 \text{ mm}^2 \]
\[ e_s = \frac{b_{su0}h_{su}t + 2h_{su}^2 t_{su}}{A_s} = 2,23 \text{ mm} \]
\[ I_s = 2\left(15t^3 \epsilon_s^2\right) + b_{su}t(h_{su} - e_s)^2 + 2h_{su}t_{su}\left(\frac{h_{su}}{2} - e_s\right)^2 + 2\left(\frac{15t^4}{12}\right) + \frac{b_{su}t^3}{12} + 2 \frac{t_{su}h_{su}^3}{12} \]
\[ = 159,53 \text{ mm}^4 \]
\[ b_s = 2\sqrt{h_{su}^2 + \left(\frac{h_{su} - b_{su0}}{2}\right)^2} + b_{su0} = 25,0 \text{ mm} \]
\[ l_b = 3,07\left(l_b^2 + 2b_{p} + 3b_{s}\right)^{1/4} = 251 \text{ mm} \]
\[ s_w = \sqrt{\frac{(w_0 - b_{u0} - b_{o0})^2}{2}} + h_0 = 83,4 \text{ mm} \]
\[ b_d = 2b_{p} + b_{s} \]
\[ k_{w0} = \frac{s_w + 2b_d}{s_w + 0.5b_d} = 1,37 \]
\[ l_b/s_w = 3,01 \quad \text{Because } l_b/s_w > 2, \quad k_w = k_{w0} = 1,37 \]
\[ \sigma_{cr,s} = \frac{4.2k_wE}{A_s} \sqrt{\frac{I_t^3}{4b_p^2(2b_p + 3b_s)}} = 515 \text{ N/mm}^2 \]
\[ \overline{x}_d = \sqrt{\frac{f_{yb}}{\sigma_{cr,s}}} = 0.683 \]
\[ \text{Because } 0.65 < \overline{x}_d < 1.38, \quad \chi = 1.47 - 0.723\overline{x}_d = 0.98 \]
\[ t_{red,u} = \chi t = 0.588 \text{ mm} \]

The distance of neutral axis from the compressed flange:
\[ t_1 = \frac{\sqrt{h_{ai}^2 + \left(\frac{b_{a0} - b_{a0}}{2}\right)^2}}{h_{ai}} - t = 0.849 \text{ mm} \]
\[ t_w = t / \sin \theta = 0.714 \text{ mm} \]
CALCULATION SHEET

\[ e_i = A_i = \begin{cases} 0 & 0,5b_{\text{eff},u}t \\ 0 & 0,5b_{\text{eff},u}X t \\ 0.5h_{\text{su}} & h_{\text{su}}X t_{\text{su}} \\ h_{\text{su}} & 0,5b_{\text{su}}X t \\ 0.5h_0 & h_{\text{w}} \\ h_0 & 0.5(h_0-b_{\text{sl}})t \\ h_0-0.5h_{\text{sl}} & h_{\text{sl}}t_{\text{sl}} \\ h_0-h_{\text{sl}} & 0.5h_{\text{sl}}t \end{cases} \]

\[ A_{\text{tot}} = \sum A_i = 87.5 \text{ mm}^2 \]

\[ e_c = \sum A_i e_i \]

\[ e_c = A_{\text{tot}} = 34.9 \text{ mm} \]

Effective cross-section of the compression zone of the web

\[ \psi = \frac{h_0-e_c}{e_c} = -1,006 \quad k_\alpha = 5.98(1-\psi)^2 = 24.1 \]

\[ b_p = \frac{h_0}{\sin \theta} = 83.4 \text{ mm} \]

\[ \bar{r}_p = \frac{b_p}{28.4e\sqrt{k_\sigma}} = 1.032 \]

\[ \rho = \frac{0.772}{\bar{r}_p} - \frac{0.125}{\bar{r}_p^2} = 0.630 \quad \text{Because } \rho < 1, b_{\text{eff}} = \rho \frac{b_p}{1-\psi} = 26.2 \text{ mm} \]

\[ s_{\text{eff},1} = 0,4h_{\text{eff}} = 10.5 \text{ mm} \]

\[ s_{\text{eff},n} = 0,6h_{\text{eff}} = 15.7 \text{ mm} \]

Effective cross section properties per half corrugation

\[ h_{\text{eff},1} = s_{\text{eff},1} \sin \theta \]

\[ h_{\text{eff},n} = s_{\text{eff},n} \sin \theta \]

\[ e_{\text{eff},j} = \begin{cases} A_{\text{eff},j} = I_{\text{eff},j} \\ 0 & 0,5b_{\text{eff},u}t \\ 0 & 0,5b_{\text{eff},u}X t \\ 0.5h_{\text{su}} & h_{\text{su}}X t_{\text{su}} \\ h_{\text{su}} & 0,5b_{\text{su}}X t \\ 0.5h_{\text{eff},1} & h_{\text{eff},1}t_{\text{w}} \\ h_0-0.5(h_0-e_c+h_{\text{eff},n}) & (h_0-e_c+h_{\text{eff},n})t_{\text{w}} \\ h_0 & 0.5(h_0-b_{\text{sl}})t \end{cases} \]

\[ t_{\text{w}}(h_0-e_c+h_{\text{eff},n})^3 / 12 \]

Section 4.4.1

Table 4.3

\[ \rho \]

Table 4.3

Because \( \rho < 1 \), \( b_{\text{eff}} = \rho \frac{b_p}{1-\psi} = 26.2 \text{ mm} \]
Optionally the effective section properties may also be redefined iteratively based on the location of the effective centroidal axis.

**Bending strength per unit width (1 m)**

\[
I = \frac{1000 \text{ mm}}{0,5w_0} I_{\text{tot}} = 549000 \text{ mm}^4
\]

\[
W_u = \frac{I}{e_c} = 14800 \text{ mm}^3
\]

\[
W_1 = \frac{I}{h_0 - e_c} = 16800 \text{ mm}^3
\]

Because \( W_u < W_1 \),

\[
W_{\text{eff,min}} = W_u = 14800 \text{ mm}^3
\]

\[
M_{c,Rd} = \frac{W_{\text{eff,min}} f_y}{\gamma_{M0}} = 3.22 \text{ kNm}
\]

**DETERMINATION OF THE RESISTANCE AT THE INTERMEDIATE SUPPORT**

**Web crippling strength**

Here \( \varphi = \theta \)

\[
l_a = s_a \quad \text{and} \quad \alpha = 0,15
\]

\[
R_{w,Rd} = \alpha t^2 \sqrt{f_y b E} \left( 1 - 0,1 \sqrt{\frac{t}{l}} \right) \left( 0,5 + \sqrt{0,02 \frac{l_a}{t}} \right) \left[ 2,4 + \left( \frac{\phi}{90 \text{ deg}} \right)^2 \right] \frac{1}{\gamma_{M1}} \frac{1000 \text{ mm}}{0,5w_0}
\]

\[
= 16,2 \text{ kN}
\]

**Combined bending moment and support reaction**

Factored actions per unit width (1m):

\[
\gamma_G = 1,35 \quad \gamma_Q = 1,5 \quad \text{Self weight: } G = 70 \text{ N/m}^2
\]

\[
q = (\gamma_G G + \gamma_Q Q) = 2,20 \text{ kN/m}
\]
**CALCULATION SHEET**

**Job Title**
ECSC Stainless Steel Valorisation Project

**Subject**
Design Example 3 – Design of a two-span trapezoidal roof sheeting

**Client**
ECSC

**Made by**
AAT
**Date**
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**Checked by**
JEK
**Date**
June 2002

**Revised by**
JBL/MEB
**Date**
April 2006

\[ M_{Ed} = \frac{qL^2}{8} = 2,31 \text{kNm} \]
\[ F_{Ed} = \frac{5}{4}qL = 7,96 \text{kN} \]

\[ \frac{M_{Ed}}{M_{c,Rd}} = 0,716 \quad \frac{F_{Ed}}{R_{W,Rd}} = 0,491 \quad \frac{M_{Ed} + F_{Ed}}{M_{c,Rd} + R_{W,Rd}} = 1,21 \]

**DETERMINATION OF DEFLECTIONS AT SERVICEABILITY LIMIT STATE (SLS)**

**Effective cross section properties**

For serviceability verification the effective width of compression elements should be based on the compressive stress in element under the serviceability limit state loading.

Maximum compressive stress in the effective section at SLS. A conservative approximation is made based on \( W_u \) determined above for ultimate limit state.

\[ M_{y,Ed,ser} = \frac{(G+Q)L^2}{8} = 1,55 \text{kNm} \]
\[ \sigma_{com,Ed,ser} = \frac{M_{y,Ed,ser}}{W_u} = 105 \text{N/mm}^2 \]

The effective section properties are determined as before in ultimate limit state except that \( f_{yb} \) is replaced by \( \sigma_{com,Ed,ser} \) and the thickness of the flange stiffener is not reduced.

The results of the calculation are:

- Effective width of the compressed flange: The flange is fully effective
- Location of the centroidal axis when the web is fully effective: \( e_c = 34,1 \text{ mm} \)
- Effective cross-section of the compression zone of the web: The web is fully effective
- Effective part of the web: The web is reduced \( (\rho = 0,88) \)
- Effective cross section properties per half corrugation:
  - \( A_{tot} = 86,6 \text{ mm}^2 \)
  - \( e_c = 34,8 \text{ mm} \)
  - \( I_{tot} = 63700 \text{ mm}^4 \)
- Effective section properties per unit width (1 m):
  - \( W_u = 17300 \text{ mm}^4 \)
  - \( W_f = 17300 \text{ mm}^4 \)
Determination of deflection

Secant modulus of elasticity corresponding to maximum value of the bending moment:

\[ \sigma_{1,Ed,ser} = \frac{M_{y,Ed,ser}}{W_u} = 89.5 \text{ N/mm}^2 \]

\[ \sigma_{2,Ed,ser} = \frac{M_{y,Ed,ser}}{W_f} = 90.8 \text{ N/mm}^2 \]

\[ E_{s,1} = \frac{E}{1 + 0.002 \cdot \frac{E}{\sigma_{1,Ed,ser}} \left( \frac{\sigma_{1,Ed,ser}}{f_{yb}} \right)^n} = 199 \text{ kN/mm}^2 \quad n = 7.0 \]

\[ E_{s,2} = \frac{E}{1 + 0.002 \cdot \frac{E}{\sigma_{1,Ed,ser}} \left( \frac{\sigma_{2,Ed,ser}}{f_{yb}} \right)^n} = 199 \text{ N/mm}^2 \]

\[ E_{s,ser} = \frac{E_{s,1} + E_{s,2}}{2} = 199 \text{ N/mm}^2 \]

Check of deflection:

As a conservative simplification, the variation of \( E_{s,ser} \) along the length of the member is neglected.

\[ x = \frac{1 + \sqrt{\frac{33}{16}}}{L} = 1.22 \text{ m} \quad \text{(location of max deflection)} \]

\[ \delta = \frac{(G+Q)I_4}{48E_{s,ser}I} \left( x - \frac{3}{L} x^3 + 2 \frac{x^4}{L^3} \right) = 4.7 \text{ mm} \]

The permissible deflection is \( L/200 = 14.5 \text{ mm} \), hence the calculated deflection is acceptable.
DESIGN EXAMPLE 4 - FATIGUE STRENGTH OF A WELDED HOLLOW SECTION JOINT

This example considers the fatigue strength of the chord of a welded hollow section joint. Fatigue may be a problem in stainless steel structures, which are subjected to repeated fluctuations of stresses. Fatigue of welded hollow section joints may be a problem e.g. in oil platforms, masts, chimneys, bridges, cranes and transport equipment.

EN 1993-1-9:2005 is applicable to stainless steels for estimating the fatigue strength of steel structures also. Therefore the section and clause references in this example are to EN 1993-1-9:2005.

The example shows the following design tasks for fatigue assessment:
- determination of the fatigue strength curve
- determination of secondary bending moments in the joint
- determination of the partial safety factor for fatigue strength and
- fatigue assessment for variable amplitude loading.

The chords of the joint are RHS 50x50x4 and braces RHS 30x30x2. The material is grade 1.4301 stainless steel with 0.2% proof stress of 220 N/mm².

Actions

Determined fatigue stress spectra for the chord during the required design life is:

<table>
<thead>
<tr>
<th>Nominal stress range</th>
<th>Number of cycles</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \Delta\sigma_1 = 100 \text{ N/mm}^2 )</td>
<td>( n_1 = 10 \times 10^3 )</td>
</tr>
<tr>
<td>( \Delta\sigma_2 = 70 \text{ N/mm}^2 )</td>
<td>( n_2 = 100 \times 10^3 )</td>
</tr>
<tr>
<td>( \Delta\sigma_3 = 40 \text{ N/mm}^2 )</td>
<td>( n_3 = 1000 \times 10^3 )</td>
</tr>
</tbody>
</table>
Structural analysis

The detail category of the joint depends on the dimensions of chord and braces. In this example $b_0 = 50 \text{ mm}$, $b_i = 30 \text{ mm}$, $t_0 = 4 \text{ mm}$ and $t_i = 2 \text{ mm}$.

Because $t_0 / t_i = 2$, the detail category is 71.

Because $0.5(b_0 - b_i) = 10 \text{ mm}$, $g = 11 \text{ mm}$, $1.1(b_0 - b_i) = 22 \text{ mm}$ and $2t_0 = 8 \text{ mm}$, the joint also satisfies the conditions $0.5(b_0 - b_i) \leq g \leq 1.1(b_0 - b_i)$ and $g \geq 2t_0$.

Effect of secondary bending moments in the joint

The effects of secondary bending moments are taken into account by multiplying the stress ranges due to axial member forces by coefficient $k_{1,0} = 1.5$.

Partial safety factors

When it is assumed that the structure is damage tolerant and the consequence of failure is low, the safety factor for fatigue strength is $\gamma_{MF} = 1.0$.

Partial safety factor for loading is $\gamma_{FF} = 1.0$.

Fatigue assessment

Reference stress range corresponding $2 \times 10^6$ stress fluctuations for detail category 71 is:

$$\Delta\sigma_c = 71 \text{ N/mm}^2$$

The fatigue strength curve for lattice girders has a constant slope $m = 5$.

The number of stress fluctuations corresponding nominal stress range $\Delta\sigma_i$ is

$$N_i = 2 \times 10^6 \left[ \frac{\Delta\sigma_c}{\gamma_{MF}\gamma_{FF}k_{1,0}\Delta\sigma_i} \right]^m$$

and

- $\Delta\sigma_1 = 100 \text{ N/mm}^2 \quad N_1 = 47.5 \times 10^3$
- $\Delta\sigma_2 = 70 \text{ N/mm}^2 \quad N_2 = 283 \times 10^3$
- $\Delta\sigma_3 = 40 \text{ N/mm}^2 \quad N_3 = 4640 \times 10^3$
Palmgren-Miner rule of cumulative damage

Partial damage because of $n_i$ cycles of stress range $\Delta\sigma_i$ is

$$D_{d,i} = \frac{n_{E_i}}{N_{E_i}}.$$  Therefore for

- $\Delta\sigma_1 = 100 \text{ N/mm}^2$  \hspace{1cm} $D_{d,1} = 0.21$
- $\Delta\sigma_2 = 70 \text{ N/mm}^2$  \hspace{1cm} $D_{d,2} = 0.35$
- $\Delta\sigma_3 = 40 \text{ N/mm}^2$  \hspace{1cm} $D_{d,3} = 0.22$

The cumulative damage during the design life $D_d = \sum_i \frac{n_{E_i}}{N_{R_i}} = \sum_i D_{d,i} = 0.78$  \hspace{1cm} A.5 (1)

Because the cumulative damage is less than unity, the calculated design life of the chord is more than the required design life.  \hspace{1cm} Clause 8(4)

The procedure described above shall also be repeated for the brace.
DESIGN EXAMPLE 5 – WELDED JOINT

The joint configuration and its loading are shown in the figure below. Noting that there are two identical plane fillet weld joints of constant throat size sharing the applied loading, the required throat size for the welds shall be determined. Right angle (equal leg) welds will be used throughout.

Material properties

Use material grade 1.4401

0.2% proof stress = 220 N/mm² and the tensile strength is = 530 N/mm²

Take \( f_y \) as the 0.2% proof stress \( = 220 \text{ N/mm}^2 \) and \( f_u = 530 \text{ N/mm}^2 \)

\( E = 200 \, 000 \text{ N/mm}^2 \) and \( G = 76 \, 900 \text{ N/mm}^2 \)

It is assumed that the yield and ultimate tensile strength of the weld exceed those of the parent metal.

Partial safety factor

Partial safety factor on weld resistance : \( \gamma_{M2} = 1.25 \)

\( \beta_w = 1.0 \)

The need to include a reduction factor on the weld resistance to account for its length will be examined.

Analysis

An elastic analysis approach is used here for designing the right-angle equal-leg fillet weld for the load case indicated above. An elastic analysis of the welded joint leads to a conservative estimate of the joint resistance.

The co-ordinates of a point \( (x_c, y_c, z_c) \) on the welded joint are taken with reference to a right hand axis system with an origin at the centre of gravity of the welded joint. (In the present case the joint is taken to be in the y-z plane so that \( x_c = 0 \) throughout.)

The main purpose of the elastic analysis is to determine the induced design forces in the weld at the most severely loaded point or points of the welded joint, often referred to as the “critical” points. For the welded joint being examined the critical point can be taken as being the point the farthest removed from the centre of gravity of the joint.
The vectors of the applied force, its eccentricity and the resulting moments acting on a welded joint of general form and centre of gravity C can be expressed as follows:

**Applied force**

\[ \mathbf{N}_{w, Ed} = [N_{x, Ed}, N_{y, Ed}, N_{z, Ed}] \]

**Eccentricity of the applied force**

\[ \mathbf{e}_N = [e_{xc}, e_{yc}, e_{zc}] \]

which are the co-ordinates of the point of application of the force vector \( \mathbf{N}_{w, Ed} \)

**Applied moments**

\[ M_{xc, Ed} = e_{yc}N_{z, Ed} - e_{zc}N_{y, Ed} \]
\[ M_{yc, Ed} = e_{zc}N_{x, Ed} - e_{xc}N_{z, Ed} \]
\[ M_{zc, Ed} = e_{xc}N_{y, Ed} - e_{yc}N_{x, Ed} \]

A linear elastic analysis of the joint for a general load case leads to the following induced force components per unit length of weld at a point with co-ordinates \((x_c, y_c, z_c)\), where the throat size is denoted by \(a\):

\[ F_{wx, Ed} = a \left[ \frac{N_{x, Ed}}{A_w} + \frac{z_c M_{yc, Ed}}{I_{yc}} - \frac{y_c M_{zc, Ed}}{I_{zc}} \right] \]
\[ F_{wy, Ed} = a \left[ \frac{N_{y, Ed}}{A_w} + \frac{x_c M_{zc, Ed}}{I_{zc}} - \frac{z_c M_{xc, Ed}}{I_{xc}} \right] \]
\[ F_{wz, Ed} = a \left[ \frac{N_{z, Ed}}{A_w} + \frac{y_c M_{xc, Ed}}{I_{xc}} - \frac{x_c M_{yc, Ed}}{I_{yc}} \right] \]

In the above expressions, the resisting sectional throat area and the inertias about the principal axes of the welded joint are:

\[ A_w = \int a dl = \sum a_i l_i \] for a weld of straight segments of length \(l_i\) and throat size \(a_i\),
\[ I_{xc} = \int a(y_c^2 + z_c^2) dl \]
\[ I_{yc} = \int a(x_c^2 + z_c^2) dl \]
\[ I_{zc} = \int a(x_c^2 + y_c^2) dl \]

As the throat size, \(a\), is constant throughout the plane joint, one can write:

\[ \frac{A_w}{a} = \int dl = \sum l_i \]

Since \(x_c = 0\),
### Design approaches

Determine the required weld throat size at the critical point.

Two different procedures are allowed for designing fillet welds:

The first procedure is based on the simplified, and more conservative, design shear strength for a fillet weld. The design shear force per unit length of weld at any point of the joint is defined as the vector sum of the induced forces per unit length due to all forces and moments transmitted by the welded joint. This design shear force per unit length should not exceed the design resistance per unit length which is taken as the design shear strength multiplied by the throat size. This approach ignores the throat plane orientation to the direction of resultant weld force per unit length.

The second procedure is based on comparing the basic design strength of the weaker part joined to the applied design weld stress in the weld throat determined by a Von Mises type of formula. This approach is the most precise as it allows for the throat plane orientation to the direction of resultant weld force per unit length.

1. Simplified design shear strength of the weld

The design resistance check of the fillet weld is as follows:

\[
\frac{I_{sc}}{a} = \int (y^2) dl, \quad \frac{I_{sc}}{a} = \int (z^2) dl, \quad \frac{I_{sc}}{a} = \int (y^2 + z^2) dl = \frac{I_{sc}}{a} + \frac{I_{sc}}{a}
\]

### Section 6.4.2

**Design approaches**

Determine the required weld throat size at the critical point.

Two different procedures are allowed for designing fillet welds:

The first procedure is based on the simplified, and more conservative, design shear strength for a fillet weld. The design shear force per unit length of weld at any point of the joint is defined as the vector sum of the induced forces per unit length due to all forces and moments transmitted by the welded joint. This design shear force per unit length should not exceed the design resistance per unit length which is taken as the design shear strength multiplied by the throat size. This approach ignores the throat plane orientation to the direction of resultant weld force per unit length.

The second procedure is based on comparing the basic design strength of the weaker part joined to the applied design weld stress in the weld throat determined by a Von Mises type of formula. This approach is the most precise as it allows for the throat plane orientation to the direction of resultant weld force per unit length.

1. Simplified design shear strength of the weld

The design resistance check of the fillet weld is as follows:

\[
F_{w,Ed} = \frac{F_{x,Ed}^2 + F_{y,Ed}^2 + F_{z,Ed}^2}{\sqrt{\beta_w \gamma_{M2}}} \leq F_{w,Rd} = a \left( \frac{f_{u} / \sqrt{3}}{\beta_w \gamma_{M2}} \right)
\]

Where:

- \(f_{u}\) is the design shear strength of the weld
- \(F_{w,Rd}\) is the design (shear) resistance per unit length of weld of throat size \(a\).

For stainless steel \(\beta_w\) may be take as 1.0

When the design procedure requires that a suitable throat size be obtained, the design expression becomes:

\[
a \geq \frac{F_{w,Ed}}{f_{vw,d}}
\]

### Section 6.4.2

**2. Basic design strength of the weld**

In this approach one must check the Von Mises type stress in the weld throat against the basic design strength of the fillet weld material. In general this requires that the stresses in the weld throat, \(\sigma_\perp\), \(\tau_{\perp}\) and \(\tau_{\parallel}\) be obtained, thus taking account of the orientation of the plane of the throat area to the direction of the resultant induced weld force per unit length.

The design formula is as follows:

\[
\sqrt{\sigma_\perp^2 + 3(\tau_{\perp}^2 + \tau_{\parallel}^2)} \leq \frac{f_u}{\beta_w \gamma_{M2}}
\]

It is also required to check the normal stress separately:

\[
\sigma_\perp \leq \frac{0.9 f_u}{\gamma_{M2}}
\]

### Section 6.4.2

**1. Simplified design shear strength of the weld**

The design resistance check of the fillet weld is as follows:

\[
F_{w,Ed} = \frac{F_{x,Ed}^2 + F_{y,Ed}^2 + F_{z,Ed}^2}{\sqrt{\beta_w \gamma_{M2}}} \leq F_{w,Rd} = a \left( \frac{f_{u} / \sqrt{3}}{\beta_w \gamma_{M2}} \right)
\]

Where:

- \(f_{u}\) is the design shear strength of the weld
- \(F_{w,Rd}\) is the design (shear) resistance per unit length of weld of throat size \(a\).

For stainless steel \(\beta_w\) may be take as 1.0

When the design procedure requires that a suitable throat size be obtained, the design expression becomes:

\[
a \geq \frac{F_{w,Ed}}{f_{vw,d}}
\]
For the present case of a plane fillet weld joint with right angle (equal leg) welds this latter check is not critical. However it may be so for partial penetration welds in bevelled joints.

Instead of having to calculate the stresses \((\sigma_\perp, \tau_\perp \text{ and } \tau_{\parallel})\) in the weld throat the following design check expression may be used for y-z plane joints with right angle (equal leg) welds:

\[
2F_{w,x}^2 + 2F_{w,y}^2 + 2F_{w,z}^2 + F_{w,x}^2 \cos^2 \theta + F_{w,z}^2 \sin^2 \theta - 2F_{w,x}F_{w,y} \sin \theta + 2F_{w,x}F_{w,z} \cos \theta + 2F_{w,y}F_{w,z} \sin \theta \cos \theta \leq \left(\frac{a f_u}{\beta_w \gamma_{M2}}\right)^2
\]

\textbf{Note : The subscripts have been shortened: } F_{w,x} \text{ for } F_{w,Ed} \text{ etc.}

In the above expression the angle \(\theta\) is that between the y axis and the axis of the weld as shown in the following figure.

\begin{align*}
\text{Section 1-1} & \quad \text{Attached element} \\
\text{Support} \quad F_{w,x} & \quad \text{Attached element} \\
\text{Fillet weld axis} & \quad \theta
\end{align*}

\begin{align*}
\text{Section 2-2} & \quad \text{Attached element} \\
\text{Support} \quad F_{w,x} & \quad \text{Attached element}
\end{align*}

\textbf{The force components at the critical point of the weld are determined in the Appendix to this design example.}

1. \textbf{Design using the simplified design shear strength approach}

The design shear strength for the simplified design approach is:

\[
F_{w,d} = \frac{f_u}{\beta_w \gamma_{M2} \sqrt{3}} = \frac{530}{1.0 \times 1.25 \times \sqrt{3}} \approx 245 \text{ N/mm}^2
\]

The value of the resultant induced force per unit length in a weld throat of 1mm is:

\[
F_{w,Ed} = \sqrt{F_{w,x,Ed}^2 + F_{w,y,Ed}^2 + F_{w,z,Ed}^2} = \sqrt{243^2 + 747^2 + 966^2} = 1245 \text{ N/mm}
\]

The required throat size is therefore:

\[
a \geq \frac{F_{w,Ed}}{f_{w,d}} = \frac{1245}{245} \approx 5.0 \text{ mm}
\]
2. Design of the weld using the basic design weld strength approach

The basic design strength of the weld material is taken as follows:

\[ \frac{0.9 f_u}{\gamma_{M2}} = \frac{0.9 \times 530}{1.25} = 381.6 \text{ N/mm}^2 \]

Where \( f_u \) is the ultimate tensile strength of the weaker part joined.

At the point (a), where the angle \( \theta \) is 0°, the design check expression becomes:

\[ 2F_{wX,Ed}^2 + 3F_{wY,Ed}^2 + 2F_{wZ,Ed}^2 + 2F_{wX,Ed}F_{wZ,Ed} \leq \left( a \frac{f_u}{\gamma_{Mw}} \right)^2 \]

The required throat size is therefore:

\[ a \geq \sqrt{2 \times (-243)^2 + 3 \times (747)^2 + 2 \times (966)^2 + 2 \times (-243) \times (966)} \div 381.6 = 4.7 \text{ mm} \]

Adopt a 5 mm throat size and assume that the weld is full size over its entire length.

Note:

A reduction factor is required for splice joints when the effective length of fillet weld is greater than 150a. The reduction factor would seem to be less relevant for the present type of joint. Nevertheless by considering, safely, the full length of the welded joint and a throat size of 5 mm one obtains:

\[ \beta_{LW,1} = 1.2 - 0.2L_j/(150a) = 1.2 - 0.2(600)/(150 \times 5) = 1.04 \]

Take \( \beta_{LW,1} = 1.0 \)

It is concluded that the use of a reduction factor on the design strength of the weld is not required.

EN 1993-1-8, Eq. 4.9
Appendix – Calculation of the force components at the critical point of the weld

Geometric properties of the welded joint

There are two similar joints, one on each side of the column, resisting the applied loads. Only one of the joints needs to be examined. It is placed in the y-z plane.

Throat area and positions of the centre of gravity and the critical point

Throat area (resisting section) of each of the joints made up of straight segments of length \( L_i \) and constant throat size \( a \) is, for each 1mm of throat size:

\[
A_w = \frac{a}{a} \int ds = \sum a_{w,i} = \sum aL_{w,i} = \sum L_i = (2 \times 175 + 250) = 600 \text{ mm}^2/\text{m}
\]

Distance of the centre of gravity from the vertical side (parallel to the z axis) of the joint of constant throat size \( a \):

\[
y = \frac{\sum y_i (A_{w,i} / a)}{\sum A_{w,i} / a} = \frac{\sum y_i L_i}{\sum L_i} = 2 \times (87.5 \times 175) + (0 \times 250) \approx 51 \text{ mm}
\]

The co-ordinates of the position of the critical point of the joint, the point (a), relative to the principal axes through centre of gravity (C) are:

\[
y_{ca} = + (175 - 51) = + 124 \text{ mm} \quad z_{ca} = - 125 \text{ mm}
\]

Note: the point (d) might also be chosen as a potential critical point, for which:

\[
y_{cd} = + (175 - 51) = + 124 \text{ mm} \quad z_{cd} = + 125 \text{ mm}
\]

However, for the load case considered it is evident that the point (a) is the most critical.

Inertias of the joint resisting section

For each of the joints, for each 1mm of throat size:

\[
I_{yc} = \int z_c^2 ds = 2 \times 175 \times 125^2 + 250^3 / 12 = 6.77 \times 10^6 \text{ mm}^4/\text{mm}
\]
\[ I_{zc} = \int y_c^2 ds = 250 \times 51^2 + 2 \times 175^3 / 12 + 2 \times 175 \times (87,5 - 51)^2 = 210 \text{ mm}^4/\text{mm} \]

For the “torsion” moment the relevant inertia, per joint, is:

\[ I_{xc} = a \int y_c^2 ds = a \int y_c^2 ds + a \int z_c^2 ds = I_{zc} + I_{yc} \]

So that

\[ \frac{I_{xc}}{a} = (6,77 + 2,01) \times 10^6 = 8,78 \times 10^6 \text{ mm}^4/\text{mm} \]

**Applied forces and moments**

It is assumed that applied loads and moments are shared equally by the two joints.

The applied axial and shear force components per joint are:

\[ N_{x,Ed} = -\frac{20}{2} = -10 \text{ kN}, \quad N_{y,Ed} = +\frac{30}{2} = +15 \text{ kN}, \]

\[ N_{z,Ed} = +\frac{300}{2} = +150 \text{ kN} \]

Applied moments are calculated using the applied force components and their eccentricities. The eccentricities, i.e. the co-ordinates of the effective load point, are:

\[ e_{xc} = 0 \text{ as the effective load point is taken to be in the y-z plane of the joint}, \]

\[ e_{yc} = (300 - 100 + 175 - 51) = +324 \text{ mm}, \]

\[ e_{zc} = -140 \text{ mm} \]

The applied moments, per joint, are then:

\[ M_{xc,Ed} = e_{yc} N_{z,Ed} - e_{zc} N_{y,Ed} = (+324) \times (+150) - (-140) \times (+15) = +50,7 \text{ kNm} \]

\[ M_{yc,Ed} = e_{zc} N_{x,Ed} - e_{xc} N_{y,Ed} = (-140) \times (-10) - (0) \times (+150) = +1,4 \text{ kNm} \]

\[ M_{zc,Ed} = e_{xc} N_{y,Ed} - e_{yc} N_{x,Ed} = (0) \times (+15) - (+324) \times (-10) = +3,24 \text{ kNm} \]

**Force components at the critical point of the weld**

For the y-z plane joint, the force components per unit length of weld at the point (a) are:

\[ F_{wx,Ed} = \frac{N_{x,Ed}}{A_w / a} + \frac{z_{ca} M_{yc,Ed}}{I_{yc} / a} - \frac{y_{ca} M_{zc,Ed}}{I_{zc} / a} \]

\[ F_{wy,Ed} = \frac{N_{y,Ed}}{A_w / a} - \frac{z_{ca} M_{xc,Ed}}{I_{xc} / a} \]

\[ F_{wz,Ed} = \frac{N_{z,Ed}}{A_w / a} + \frac{y_{ca} M_{xc,Ed}}{I_{xc} / a} \]
The contributions to the weld force components (at all points of the welded joint) from the applied force components are:

\[ F_{w, x} = \frac{N_{x, Ed}}{A_w / a} = \frac{-10}{600} = -0.017 \text{kN/mm} \]

\[ F_{w, y} = \frac{N_{y, Ed}}{A_w / a} = \frac{+15}{600} = +0.025 \text{kN/mm} \]

\[ F_{w, z} = \frac{N_{z, Ed}}{A_w / a} = \frac{+150}{600} = +0.25 \text{kN/mm} \]

The various contributions to the weld force components per unit length of weld at the point (a) from the applied moment components are:

\[ F_{w, y} = -M_{xc, Ed} \frac{y_{c, a}}{(I_{xc} / a)} = -50.7 \times 10^6 \times \frac{-125}{8.78 \times 10^6} = +722 \text{N/mm} \]

\[ F_{w, x} = +M_{xc, Ed} \frac{y_{c, a}}{(I_{xc} / a)} = +50.7 \times 10^6 \times \frac{+124}{8.78 \times 10^6} = +716 \text{N/mm} \]

\[ F_{w, z} = +M_{yc, Ed} \frac{z_{c, a}}{(I_{yc} / a)} = +1.41 \times 10^6 \times \frac{-125}{6.77 \times 10^6} = -26 \text{N/mm} \]

\[ F_{w, z} = -M_{zc, Ed} \frac{z_{c, a}}{(I_{zc} / a)} = -3.24 \times 10^6 \times \frac{+124}{2.01 \times 10^6} = -200 \text{N/mm} \]

Combining the contributions at the point (a) from the forces and the moments one obtains:

\[ F_{wx, Ed} = F_{w, x} + F_{w, y} + F_{w, z} = -17 +25 +722 -26 -200 = -43 N/mm \]

\[ F_{wy, Ed} = F_{w, y} + F_{w, x} + F_{w, y} = +25 +722 = +747 N/mm \]

\[ F_{wz, Ed} = F_{w, z} + F_{w, z} = +250 +716 = +966 N/mm \]

These resultant induced force components per unit length are for a welded joint with a weld throat size of 1mm throughout its entire effective length.
DESIGN EXAMPLE 6 – BOLTED JOINT

A 100×100×10 angle loaded in tension is to be connected to a gusset plate of 10 mm thickness. Stainless steel grade 1.4401 is used for the angle and the gusset plate. Eight austenitic 16 mm diameter bolts of property class 50 are used in a staggered line to connect one leg of the angle to the gusset plate. The proposed joint is shown in the following figure. It is required to determine the design resistance of the joint.

The connection is a Category A: Bearing Type connection. The design ultimate shear load should not exceed the design shear resistance nor the design bearing resistance.

Material properties

The angle and plate is of material grade 1.4401:
- The 0.2% proof stress = 220 N/mm² and the tensile strength is = 530 N/mm²
- Take $f_y$ as the 0.2% proof stress = 220 N/mm² and $f_u = 530$ N/mm²

The bolt material is of property class 50.
- Take $f_{yb}$ as the 0.2% proof stress = 210 N/mm² and $f_{ub} = 500$ N/mm²

Partial safety factors

- Partial safety factor on gross section resistance: $\gamma_M = \gamma_{M1} = 1,1$
- Partial safety factor on net section resistance: $\gamma_M = 1,25$
- Partial safety factor on bolt resistance in shear and in bearing: $\gamma_M = 1,25$

Position and size of holes

For M16 bolts a hole diameter $d_0 = 18$mm is required.

End distances $e_1 = 30$ mm and edge distances $e_2 = 25$ mm $e_1$ and $e_2 < 4t + 40 = 80$ mm and $> 1,2d_0 = 1,2 \times 18 = 21,6$ mm

For the staggered bolt rows:
- spacing $p_1 = 60$ mm $> 2,2d_0 = 39,6$ mm

EN 1993-1-8, clause 3.4.1
- distance between two bolts in staggered row
  \[ \sqrt{30^2 + 35^2} = 46.1 \text{ mm} > 2.4d_0 = 43.2 \text{ mm} \]
- therefore, spacing for staggered rows \( p_2 = 35 \text{ mm} > 1.2d_0 = 21.6 \text{ mm} \)

*Note:* For compression loading, \( e_2 \) and \( p_1 \) should be checked that they satisfy local buckling requirements for an outstand element and an internal element respectively. Checks on both the angle and gusset plate are required.

### Design resistance of the angle gross cross-section in tension

Gross cross-sectional area of the angle \( A_g = 1915 \text{ mm}^2 \)

Design plastic resistance

\[
N_{pl,Rd} = \frac{A_g f_y}{f_{M0}} = \frac{1915 \times 220}{1,1 \times 10^3} = 383 \text{ kN}
\]

Eq. 6.4

### Design resistance of the angle net cross-section in tension

For staggered holes the net cross-sectional area should be taken as the lesser of:

- gross area minus the deduction for non-staggered holes
  \[
  A_g - t \left( n d_0 - \sum \frac{s^2}{4p} \right)
  \]

Deductions for non-staggered holes

\[
A_g - t d_0 = 1915 - 10 \times 18 = 1735 \text{ mm}^2
\]

Net cross-sectional area through two staggered holes, \( n = 2 \), \( s = 30 \text{ mm} \) and \( p = 35 \text{ mm} \):

\[
A_{net} = A_g - t \left( n d_0 - \sum \frac{s^2}{4p} \right) = 1915 - 10 \left( 2 \times 18 - \frac{30^2}{4 \times 35} \right) = 1915 - 10(36.64) = 1619 \text{ mm}^2
\]

Therefore \( A_{net} = 1619 \text{ mm}^2 \)

Conservatively the reduction factor for an angle connected by one leg with a single row of bolts may be used. By interpolation for more than 3 bolts in one row: \( \beta_3 = 0.57 \).
Design ultimate resistance of the net cross-section of the angle:
\[ N_{u,\text{Rd}} = \frac{f_y A_{\text{net}} f_u}{\gamma_M} = \frac{0.57 \times 1619 \times 530}{1.25 \times 10^3} = 391.3 \text{kN} \]

**Design resistance of the angle in block tearing**
The expressions for block tearing are taken from EN 1993-1-8 rather than EN 1993-1-1 since EN 1993-1-8 explicitly covers angles.

Design resistance in block tearing considering rows as staggered:
\[ V_{\text{eff},2,\text{Rd}} = \frac{0.5 f_y A_{\text{nt}}}{\gamma_M} + \frac{f_y A_{\text{nv}}}{\sqrt{3} \gamma_M} = \frac{0.5 \times 530 \times (60 - 18) \times 10}{1.25 \times 10^3} + \frac{220 \times (240 - 4 \times 18) \times 10}{\sqrt{3} \times 1.1 \times 10^3} = 89 + 194 = 283 \text{kN} \]

Design resistance in block tearing considering rows as if non staggered:
\[ V_{\text{eff},2,\text{Rd}} = \frac{0.5 f_y A_{\text{nt}}}{\gamma_M} + \frac{f_y A_{\text{nv}}}{\sqrt{3} \gamma_M} = \frac{0.5 \times 530 \times (60 - 18 - 9) \times 10}{1.25 \times 10^3} + \frac{220 \times (240 - 3 \times 18 - 9) \times 10}{\sqrt{3} \times 1.1 \times 10^3} = 70 + 204 = 274 \text{kN} \]

**Design resistance of the gross cross-section of the gusset plate**
Gross cross-sectional area towards the end of the angle:
\[ A_g = 10 \times (100 + 70 + 70) = 2400 \text{ mm}^2 \]

Design plastic resistance
\[ N_{\text{pl},\text{Rd}} = \frac{A_g f_y}{\gamma_M} = \frac{2400 \times 220}{1.1 \times 10^3} = 480 \text{kN} \]

**Design resistance of the net cross-section of the gusset plate**
Net cross-sectional area towards the end of the angle (where the applied load is greatest) through one hole non symmetrically placed on an element of width:
\[ b = 100 + 70 + 70 = 240 \text{ mm}; \]
\[ A_{\text{net}} = A_g - d_y t = 2400 - 18 \times 10 = 2220 \text{ mm}^2 \]
Net cross-sectional area towards the end of the angle through two staggered holes with \( s = 30 \text{ mm} \) and \( p = 35 \text{ mm} \):

\[
A_{\text{net}} = A_g - 2d_ut + \frac{s^2t}{4p} = 2400 - 2 \times 18 \times 10 + \frac{30^2 \times 10}{4 \times 35}
\]

\[
= 2400 - 360 + 64 = 2104 \text{ mm}^2
\]

Therefore \( A_{\text{net}} = 2104 \text{ mm}^2 \)

Design ultimate resistance of the net cross-section of the gusset plate near the end of the angle:

\[
N_{u,Rd} = \frac{k_r A_{\text{net}} f_u}{\gamma_{M2}}
\]

Reduction factor \( k_r \): \( k_r = [1 + 3r(d_0 / u - 0,3)] \) but \( < 1.0 \)

\( u = 2e_2 \leq p_2 \) therefore, \( u = 35 \text{ mm} \)

\[
k_r = \left[ 1 + 2 \times \frac{2}{8} \times \left( \frac{18}{35} - 0,3 \right) \right] = 1,16 > 1,0
\]

Take \( k_r = 1,0 \)

\[
N_{u,Rd} = \frac{1,0 \times 2104 \times 530}{1,25 \times 10^3} = 892,1 \text{ kN}
\]

It is advisable to check the resistance of net cross-sections at intermediate cross-sections along the gusset plate.

Cross-section at the 1st bolt hole near the gusset plate edge

(Where \( b = 100 + 30/240 \times 140 = 117,5 \text{ mm} \))

\[
A_{\text{net}} = A_g - d_ut = 117,5 \times 10 - 18 \times 10 = 995 = 995 \text{ mm}^2
\]

This cross-section must be capable of transmitting the load from one bolt

Design ultimate resistance at the section:

\[
N_{u,Rd} = \frac{k_r A_{\text{net}} f_u}{\gamma_{M2}} = \frac{1,0 \times 995 \times 530}{1,25 \times 10^3} = 421,88 \text{ kN}
\]

It is obvious that there is no need to check any other cross-sections of the gusset plate as the load applied cannot exceed the design resistance of the angle itself which has been shown to be smaller than the above value.
Design resistance of the gusset plate in block tearing

Design resistance to block tearing considering rows as staggered:

\[ V_{\text{eff,1,Rd}} = \frac{f_u A_{\text{nt}} + f_y A_{\text{nv}}}{\gamma M_2} \left( \frac{1}{\sqrt{3} \gamma M_0} \right) \]

\[ = \frac{530 \times (35 - 9) \times 10 + 220 \times (240 - 4 \times 18 + 240 - 3 \times 18 - 9) \times 10}{1,25 \times 10^3 \sqrt{3} \times 1,1 \times 10^3} \]

\[ = 110,2 + 398,4 = 508,6 \text{ kN} \]

Design resistance to block tearing considering rows as if non staggered:

\[ V_{\text{eff,1,Rd}} = \frac{f_u A_{\text{nt}} + f_y A_{\text{nv}}}{\gamma M_2} \left( \frac{1}{\sqrt{3} \gamma M_0} \right) \]

\[ = \frac{530 \times (35 - 2 \times 9) \times 10 + 220 \times (2 \times 240 - 6 \times 18 - 2 \times 9) \times 10}{1,25 \times 10^3 \sqrt{3} \times 1,1 \times 10^3} \]

\[ = 72,1 + 408,8 = 480,9 \text{ kN} \]

**Design resistance of the bolts in shear**

The bolts are in single shear. Consider the shear to be in the plane of the threads. Therefore, \( \alpha = 0,5 \)

Sectional area of M16 bolt: \( A_s = 157 \text{ mm}^2 \)

Design resistance of class 50 M16 bolt of sectional area \( A_s = 157 \text{ mm}^2 \):

\[ F_{v,Rd} = \frac{\alpha f_u A_s}{\gamma M_2} = \frac{0,5 \times 500 \times 157}{1,25 \times 10^3} = 31,4 \text{ kN} \]

Design resistance of the bolt group in shear: \( n_b F_{v,Rd} = 8 \times 31,4 = 251,2 \text{ kN} \)
**Design resistance of the bolts/ply in bearing**

\[ F_{b,Rd} = \frac{k_1\alpha_b f_{u,\text{red}} dt}{\gamma M_2} \]

Design resistance in bearing on the 10 mm thick ply of the end M16 bolt where end distances \( e_1 = 30 \text{ mm} \), edge distances \( e_2 = 25 \text{ mm} \) (\( > 1,2d_0 = 21.6 \text{ mm} \)) and bolt spacings \( p_1 = 60 \text{ mm} \) and \( p_2 = 35 \text{ mm} \)

The deformations at the serviceability load level: reduced design bearing stress \( f_{u,\text{red}} \) is used here in order to avoid excessive bolt hole

\[ f_{u,\text{red}} = 0,5 f_y + 0,6 f_u \text{ but } f_{u,\text{red}} \leq f_u \]

\[ 0,5 \times 220 + 0,6 \times 530 = 428 \text{ N/mm}^2 < f_u \]

\[ \alpha_d = \frac{e_1}{3d_0} = \frac{30}{3 \times 18} = 0.556 \]

The reduction factor for the end bolt nearest the ends where \( e_1 = 30 \text{ mm}, \ p_1 = 60 \text{ mm} \):

\[ \alpha_b = \min (\alpha_d; \ f_{ub} / f_{u,\text{red}}; \ 1,0) \]

\[ = \min (0,556; \ 500/428 = 1,17; \ 1,0) = 0,556 \]

\[ k_1 = \min \left( 2,8 \frac{e_2}{d_0} - 1,7; \ 2,5 \right) \]

\[ = \min \left( 2,8 \frac{25}{18} - 1,7 = 2,2; \ 2,5 \right) = 2,2 \]

The bolt itself is not critical in bearing, since \( f_{ub}/f_u = 500/428 = 1,17 > 1,0 \)

Design bearing resistance for the end bolt :

\[ F_{b,Rd} = \frac{k_1\alpha_b f_{u,\text{red}} dt}{\gamma M_2} = \frac{2,2 \times 0,556 \times 428 \times 16 \times 10}{1,25 \times 10^3} = 67,0 \text{ kN} \]

Design resistance of the joint in bearing: \( n_F_{b,Rd} = 8 \times 67,0 = 536 \text{ kN} \)

Note : The critical mode of failure for all of the bolts in the joint is shear.

**Design resistance of the joint at the Ultimate Limit State**

The smallest design resistance found was that for block tearing of the connected angle leg:

Design resistance to block tearing of the connected angle leg: \( N_{\text{Rd}} = V_{\text{eff,2,Rd}} = 274 \text{ kN} \)
DESIGN EXAMPLE 7 – SHEAR RESISTANCE OF PLATE GIRDER

Design a plate girder with respect to shear resistance. The girder is a simply supported I-section with a span according to the figure below. The top flange is laterally restrained.

\[ F_{Ed} = 440 \text{ kN} \]

Use material grade 1.4462, hot rolled.

\[ f_y = 460 \text{ N/mm}^2 \]
\[ E = 200 \text{,}000 \text{ N/mm}^2 \]

Try a cross section with

Flanges: \( 12 \times 200 \text{ mm}^2 \)

Web: \( 4 \times 500 \text{ mm}^2 \)

Stiffeners: \( 12 \times 98 \text{ mm}^2 \)

Weld throat thickness: \( 4 \text{ mm} \)

**Structural analysis**

Maximum shear and bending moment are obtained as

\[ V_{Ed} = \frac{F_{Ed}}{2} = \frac{440}{2} = 220 \text{ kN} \]

\[ M_{Ed} = \frac{F_{Ed}L}{4} = \frac{440 \times 2.5}{4} = 275 \text{ kNm} \]

**Partial safety factors**

\[ \gamma_{M0} = 1,1 \]
\[ \gamma_{M1} = 1,1 \]

**Classification of the cross-section**

\[ \varepsilon = \sqrt{\frac{235 \times 200}{460 \times 210}} = 0,698 \]
Web, subject to bending
\[
\frac{c}{te} = \frac{500 - 2 \times \sqrt{2} \times 4}{4 \times 0.698} = 175 > 74.8, \text{ therefore the web is Class 4.}
\]

Flange, subject to compression
\[
\frac{c}{te} = \frac{200 - 4 - 2 \times \sqrt{2} \times 4}{2 \times 12 \times 0.698} = 11.0 \leq 11.0, \text{ therefore the compression flange is Class 3.}
\]

Thus, overall classification of cross-section is Class 4.

Shear resistance

The shear buckling resistance requires checking when
\[
h_w / t_w \geq \frac{23}{\eta} \sqrt{k_t} \text{ for vertically stiffened webs.}
\]

\[
a/h_w = 1250/500 > 1, \text{ hence}
\]

\[
k_t = 5.34 + 4 \left( h_w / a \right)^2 = 5.34 + 4 \left( \frac{500}{1250} \right)^2 = 5.98
\]

EN 1993-1-4 recommended value for \( \eta = 1.2 \)

\[
h_w / t_w = \frac{500}{4} = 125 \geq \frac{23}{1.2} \times 0.698 \times \sqrt{5.98} = 32.7
\]

Therefore the shear buckling resistance has to be checked. It is obtained as

\[
V_{b,Rd} = V_{bw,Rd} + V_{bf,Rd} \leq \frac{\eta f_{yw} h_w t_w}{\sqrt{3} \gamma_{M1}} = \frac{1.2 \times 460 \times 500 \times 4}{\sqrt{3} \times 1.1} = 579.47 \text{ kN}
\]

\[
V_{bw,Rd} = \frac{\chi_w f_{yw} h_w t_w}{\sqrt{3} \gamma_{M1}}
\]

\[
\chi_w = \eta = 1.2 \text{ for } \lambda_w \leq 0.60 / \eta = 0.5
\]

\[
\chi_w = 0.11 + \frac{0.64}{\lambda_w} - 0.05 \text{ for } \lambda_w > 0.60 / \eta = 0.5
\]

\[
\lambda_{w} = \frac{h_w}{37.4 t_w \sqrt{k_t}}
\]

\[
\lambda_{w} = \frac{500}{\left( 37.4 \times 4 \times 0.698 \times \sqrt{5.98} \right)} = 1.958 > 0.60 / \eta = 0.5
\]

Hence the contribution from the web is obtained as:

\[
\chi_w = 0.11 + \frac{0.64}{1.958} - \frac{0.05}{1.958^2} = 0.424
\]
\[ V_{bw,Rd} = \frac{X_w f_{yw} h_w t_w}{\sqrt{3} \gamma_{M1}} = \frac{0.424 \times 460 \times 500 \times 4}{\sqrt{3} \times 1.1} = 204.74 \text{kN} \]

The contribution from the flanges may be utilised if the flanges are not fully utilised in withstanding the bending moment. The bending resistance of a cross section consisting of the flanges only is obtained as

\[ M_{f,Rd} = 12 \times 200 \times \frac{460}{1.1} \times (500 + 12) = 513.86 \text{kNm} \]

\[ M_{f,Rd} > M_{Ed} = 275 \text{kNm}, \text{ therefore the flanges can contribute to the shear buckling resistance.} \]

\[ V_{bf,Rd} = \frac{b_t f_t^2 f_{yt}}{c \gamma_{M1}} \left[1 - \left(\frac{M_{Ed}}{M_{f,Rd}}\right)^2\right] \]

\[ c = a \left[0.17 + \frac{3.5 b_t t_f^2 f_{yt}}{t_w h_w f_{yw}}\right] \quad \text{but} \quad \frac{c}{a} \leq 0.65 \]

\[ = 1250 \times \left[0.17 + \frac{3.5 \times 200 \times 12^2 \times 460}{4 \times 500^2 \times 460}\right] = 338 \text{mm} < 0.65 \times 1250 = 812 \text{mm} \]

\[ V_{bf,Rd} = \frac{200 \times 12^2 \times 460}{338 \times 1.1} \times \left[1 - \left(\frac{275}{513.86}\right)^2\right] = 25.43 \text{kN} \]

\[ V_{b,Rd} = V_{bw,Rd} + V_{bf,Rd} = 230.17 \text{kN} \leq 579.47 \text{kN} \]

**Transverse stiffeners**

The transverse stiffeners have to be checked for crushing and flexural buckling using \( \alpha = 0.49, \quad \lambda_0 = 0.2 \). An effective cross section consisting of the stiffeners and parts of the web is then used. The part of the web included is \( 11 \varepsilon t_w \) wide, therefore the cross section of the transverse stiffener is Class 3.

\[ \frac{a}{h_w} = 1250/500 = 2.5 \geq \sqrt{2}, \text{ hence the second moment of area of the intermediate stiffener has to fulfil} \]

\[ I_{st} \geq 0.75 h_w t_w^3 = 0.75 \times 500 \times 4^3 = 24000 \text{mm}^4 \]

\[ I_{st} = 2 \times (11 \times 0.698 \times 4) \times 4^3 + 12 \times 200^3 / 12 = 8.00 \times 10^6 \text{mm}^4, \text{ hence fulfilled.} \]

The crushing resistance is obtained as

\[ N_{c,Rd} = A_s f_y / \gamma_M0 \]

\[ A_s = (12 \times 200 + 11 \times 0.698 \times 4 \times 2) = 2461.42 \text{mm}^2 \]
The flexural buckling resistance is obtained as

\[ N_{b,Rd} = \chi A_s f_y / \gamma_M \]

\[ \chi = \frac{1}{\varphi + \left( \frac{\varphi^2}{\varphi^2 - \overline{\chi}^2} \right)^{0.5}} \leq 1 \]

\[ \varphi = 0.5 \left( 1 + \alpha \left( \overline{\chi} - \overline{\chi}_0 \right) + \overline{\chi}^2 \right) \]

\[ \overline{\chi} = \frac{L_{cr}}{i} \frac{1}{\pi} \sqrt{\frac{f_{yw}}{E}} \]

\[ L_{cr} = 0.75 h_w = 0.75 \times 500 = 375 \text{ mm} \]

\[ \overline{\chi} = \frac{375}{8 \times 10^6} \frac{1}{\pi} \sqrt{\frac{460 \times 10^3}{200000}} = 0.100 \]

\[ \varphi = 0.5 \times \left( 1 + 0.49 \times (0.100 - 0.2) + 0.100^2 \right) = 0.481 \]

\[ \chi = \frac{1}{0.481 + \left[ 0.481^2 - 0.100^2 \right]^{0.5}} = 1.05 > 1 \Rightarrow \chi = 1.0 \]

Since \( N_{b,Rd} = N_{c,Rd} > N_{Ed} \), the transverse stiffeners are sufficient.

### Interaction shear and bending

If the utilization of shear resistance, expressed as the factor \( \overline{\eta}_3 \), exceeds 0.5, the combined effect of bending and shear has to be checked.

\[ \overline{\eta}_3 = \frac{V_{Ed}}{V_{bw,Rd}} \leq 1.0 \]

\[ \overline{\eta}_3 = \frac{220}{204.74} = 1.075 > 0.5 \text{, therefore interaction has to be considered.} \]

The condition is

\[ \overline{\eta}_1 + \left( 1 - \frac{M_{f,Rd}}{M_{pl,Rd}} \right) \left( 2 \overline{\eta}_3 - 1 \right)^2 \leq 1.0 \text{ for } \overline{\eta}_1 \geq \frac{M_{f,Rd}}{M_{pl,Rd}} \]

Where:

\[ \overline{\eta}_1 = \frac{M_{Ed}}{M_{pl,Rd}} \]
**Calculation of effective cross-section properties.**

The flanges are Class 3 and hence fully effective.

The depth of the web has to be reduced with the reduction factor $\rho$, welded web.

$$\rho = \frac{0.772}{\lambda_p} - \frac{0.125}{\lambda_p^2} \leq 1$$

**Eq. 4.1a**

$$\lambda_p = \frac{b/t}{28.4\varepsilon_k/k_{\sigma}}$$  \text{where}  \( b = d = 500 - 2 \times 4 \times \sqrt{2} = 488.68 \text{ mm} \)

**Eq. 4.2**

Assuming linearly varying, symmetric stress distribution within the web,

$$\psi = \frac{\sigma_2}{\sigma_1} = -1$$

$$\Rightarrow k_{\sigma} = 23.9$$

$$\lambda_p = \frac{488.68/4}{28.4 \times 0.698 \times \sqrt{23.9}} = 1.26$$

$$\rho = \frac{0.772}{1.26} - \frac{0.125}{1.26^2} = 0.534 \leq 1$$

$$b_{\text{eff}} = \rho b_c = \rho \frac{b}{(1-\psi)} = 0.534 \times 488.68/(1-(-1)) = 130.48$$

Table 4.3

$$b_{c1} = 0.4b_{\text{eff}} = 0.4 \times 130.48 = 52.19 \text{ mm}$$

$$b_{c2} = 0.6b_{\text{eff}} = 0.6 \times 130.48 = 78.29 \text{ mm}$$

Table 4.3

**Calculate effective section modulus under bending.**

$e_i$ is taken as positive from the centroid of the upper flange and downwards.

$$A_{\text{eff}} = \sum_i A_i = b_1 t_f \times 2 + b_3 t_w + b_2 t_w + \left( h_w / 2 \right) t_w = 6321.92 \text{ mm}^2$$

$$e_{\text{eff}} = \frac{1}{A_{\text{eff}}} \sum_i A_i e_i = \frac{1}{A_{\text{eff}}} \left[ b_1 t_f (0) + b_1 t_f (h_w + t_f) \right] + \left[ b_3 t_w (0.5(b_{c1} + t_f)) + b_3 t_w (0.5(b_{c2} + t_f)) + b_2 t_w (0.5(h_w + t_f) - b_{c2} / 2) + (h_w / 2) t_w (0.75h_w + 0.5t_f) \right] = 266.44 \text{ mm}$$

$$I_{\text{eff}} = \sum_i I_i + \sum_i A_i (e_{\text{eff}} - e_i)^2 = 2 \times \frac{b_1 t_f^3}{12} + \frac{t_w b_3^3}{12} + \frac{t_w b_{c1}^3}{12} + \frac{t_w b_{c2}^3}{12} + \frac{t_w (h_w / 2)^3}{12} + \frac{b_1 t_f (e_{\text{eff}} - 0)^2 + b_1 t_f (e_{\text{eff}} - (h_w + t_f))^2 + b_1 t_f (e_{\text{eff}} - 0.5(b_{c1} + t_f))^2 + b_3 t_w (e_{\text{eff}} - 0.5(b_{c2} + t_f))^2 + b_2 t_w (e_{\text{eff}} - 0.5(h_w + t_f))^2 + b_2 t_w (e_{\text{eff}} - 0.5(h_w + t_f))^2 + b_2 t_w (e_{\text{eff}} - 0.75h_w + 0.5t_f)^4}{4} = 3.459 \times 10^6 \text{ mm}^4$$
\[ \eta_1 = \frac{M_{Ed}}{M_{pl,Rd}} \]

\[ M_{f,Rd} = 513,86 \text{ kNm (Sheet 3)} \]

\( M_{pl,Rd} \) is the plastic resistance of the cross-section.

\[ M_{pl,Rd} = M_{f,Rd} + t_w h_w^2 f_y \frac{M}{f_{y,M0}} = 513,86 + \frac{4 \times 500^2 \times 460}{4 \times 1.1 \times 10^6} = 618,40 \text{ kNm} \]

**Evaluate conditions**

\[ M_{Ed} = 275 \text{ kNm}, \text{ hence:} \]

\[ \eta_1 = \frac{275}{618,40} = 0,44 \leq 1,0 \text{ OK} \]

\( \eta_1 \) fulfils its condition. Now it remains to check the interaction.

\[ \eta_1 + \left( 1 - \frac{M_{f,Rd}}{M_{pl,Rd}} \right) \left( 2 \eta_3 - 1 \right)^2 = 0,44 + \left( 1 - \frac{513,86}{618,40} \right) \left( 2 \times 1,075 - 1 \right)^2 = 0,664 < 1,0 \]

It therefore follows that under the conditions given, the resistance of the plate girder is sufficient with respect to shear, bending as well as interaction between shear and bending.
DESIGN EXAMPLE 8 – RESISTANCE TO CONCENTRATED LOADS

An existing plate girder, previously subjected to an evenly distributed load, will be refurbished and will be subjected to a concentrated load. Check if the girder can resist the new load applied through a 12 mm thick plate. The girder is a simply supported I-section with a span according to the figure below. The top flange is laterally restrained.

\[ F_{Ed} = 110 \text{ kN} \]

Material grade 1.4462, hot rolled.
\[ f_y = 460 \text{ N/mm}^2 \]
\[ E = 200 000 \text{ N/mm}^2 \]

Flanges: \( 12 \times 200 \text{ mm}^2 \)
Web: \( 4 \times 500 \text{ mm}^2 \)
Stiffeners: \( 12 \times 98 \text{ mm}^2 \)
Weld throat thickness: \( 4 \text{ mm} \)

**Structural analysis**

Maximum shear and bending moment are obtained as
\[
V_{Ed} = \frac{F_{Ed}}{2} = \frac{110}{2} = 55 \text{ kN}
\]
\[
M_{Ed} = \frac{F_{Ed}L}{4} = \frac{110 \times 2.5}{4} = 68.75 \text{ kNm}
\]

**Partial safety factors**
\[
\gamma_{M0} = 1.1
\]
\[
\gamma_{M1} = 1.1
\]

**Classification of the cross-section**
\[
\varepsilon = \frac{\sqrt{235 \times 200}}{\sqrt{460 \times 210}} = 0.698
\]
Web, subject to bending
\[ \frac{c}{t_e} = \frac{500 - 2 \times \sqrt{2} \times 4}{4 \times 0.698} = 175 > 74.8, \text{ therefore the web is Class 4} \]

Flange, subject to compression
\[ \frac{c}{t_e} = \frac{200 - 4 \times 2 \times \sqrt{2} \times 4}{2 \times 12 \times 0.698} = 11.0 \leq 11.0, \text{ therefore the compression flange is Class 3} \]

Thus, overall classification of cross-section is Class 4

**Resistance to concentrated force**

The design load should not exceed the design resistance, i.e.
\[ F_{Rd} = \frac{f_{yw} L_{eff} t}{\gamma M_1} \]

The effective length \( L_{eff} \) is given by
\[ L_{eff} = \chi F l_y \]

where the reduction function is
\[ \chi F = 0.5, \quad 0.5 \leq 1.0 \]

with the slenderness given by
\[ \lambda F = \sqrt{\frac{l_y t_w f_{yw}}{F_{cr}}} \]

The effective loaded length is given by
\[ l_y = s_s + 2 t_f \left( 1 + \sqrt{m_1 + m_2} \right) \]

Where
\[ s_s \text{ is the length of the stiff bearing and } m_1 \text{ and } m_2 \text{ are dimensionless parameters.} \]

\[ m_1 = \frac{f_{yt} b_f}{f_{yw} t_w} \]

\[ m_2 = \begin{cases} 0.02 \left( \frac{h_w}{t_f} \right)^2 & \text{for } \lambda F > 0.5 \\ 0 & \text{for } \lambda F \leq 0.5 \end{cases} \]

\[ s_s \text{ is conservatively taken as twice the thickness of the load bearing plate, i.e. 24 mm.} \]

\[ m_1 = \frac{460 \times 200}{460 \times 4} = 50 \]
The critical load is obtained as

\[ F_{cr} = 0.9 \times \bar{F} \times \frac{E}{h_w} \]

where the buckling coefficient is given by the load situation, type a.

\[ k_f = 6 + 2 \left( \frac{h_w}{a} \right)^2 \]

\[ = 6 + 2 \left( \frac{500}{2500} \right)^2 = 6.08 \]

\[ F_{cr} = 0.9 \times 6.08 \times 200000 \times \frac{4^3}{500} = 140.08 \text{kN} \]

\[ \bar{F}_{cr} = \sqrt{\frac{268.90 \times 4 \times 460}{140.08 \times 10^3}} = 1.88 > 0.5, \text{ assumption OK} \]

\[ \chi_{cr} = 0.5 \times \frac{1.88}{1.88} = 0.266 \leq 1.0, \text{ OK} \]

\[ L_{eff} = 0.266 \times 268.90 = 71.53 \text{ mm} \]

\[ F_{Ed} = 110 \leq 460 \times 71.53 \times 4/(1.1 \times 10^3) = 119.65 \text{kN} \]

Hence the resistance exceeds the load.

**Interaction between transverse force, bending moment and axial force**

Interaction between concentrated load and bending moment is checked according to prEN 1993-1-5:2004.

\[ 0.8 \times \eta_1 + \eta_2 \leq 1.4 \]

Where

\[ \eta_1 = \frac{N_{Ed}}{f_y A_{eff} / \gamma_{M0}} + \frac{M_{Ed} + N_{Ed} e_N}{f_y W_{eff} / \gamma_{M0}} \leq 1.0 \]

prEN 1993-1-5, Eq. 4.14
η₂ = \frac{F_{Ed}}{f_{yw} L_{eff} t / \gamma_{M1}} \leq 1.0

Calculation of effective cross-section properties
The flanges are Class 3 and hence fully effective.
The depth of the web has to be reduced with the reduction factor \( \rho \), welded web.

\[ \rho = \frac{0.772}{\lambda_p} - \frac{0.125}{\lambda_p^2} \leq 1 \]

\[ \lambda_p = \frac{b/t}{28.4 \sqrt{k_\sigma}} \]

where \( b = d = 500 - 2 \times 4 \times \sqrt{2} = 488.68 \text{ mm} \)

Assuming linearly varying symmetric stress distribution within the web,

\[ \psi = \frac{\sigma_2}{\sigma_1} = -1 \]

\[ \Rightarrow k_\sigma = 23.9 \]

\[ \lambda_p = \frac{488.68/4}{28.4 \times 0.698 \times \sqrt{23.9}} = 1.26 \]

\[ \rho = \frac{0.772}{1.26} - \frac{0.125}{1.26^2} = 0.534 \leq 1 \]

\[ b_{eff} = \rho b_c = \rho \frac{b}{1-\psi} = 0.534 \times 488.68/(1-(-1)) = 130.48 \]

\[ b_{e1} = 0.4b_{eff} = 0.4 \times 130.48 = 52.19 \text{ mm} \]

\[ b_{e2} = 0.6b_{eff} = 0.6 \times 130.48 = 78.29 \text{ mm} \]

Calculate effective section modulus under bending

\[ e_i \] is taken as positive from the centroid of the upper flange and downwards

\[ A_{eff} = \sum_i A_i = b_t t_f \times 2 + b_{e1} t_w + b_{e2} t_w + (h_w / 2) t_w = 6321.92 \text{ mm}^2 \]

\[ e_{eff} = \frac{1}{A_{eff}} \sum A_i e_i = 1 \left[ b_t t_f (0) + b_t t_f (h_w + t_f) \right] + b_{e1} t_w (0.5(b_{e1} + t_f) + b_{e2} w (0.5(h_w + t_f) - b_{e2} / 2) + (h_w / 2) t_w (0.75 h_w + 0.5 t_f) \right] = 266.44 \text{ mm}^2 \]

\[ I_{eff} = \sum_i I_i + \sum_i A_i (e_{eff} - e_i)^2 = 2b_t t_f^3 + t_w b_{e1}^3 + t_w b_{e2}^3 + \frac{t_w (h_w / 2)^3}{12} + b_t t_f \left( e_{eff} - e_i \right)^2 + b_t t_f \left[ e_{eff} - (h_w + t_f) \right]^2 + b_{e1} t_w \left[ e_{eff} - 0.5(b_{e1} + t_f) \right]^2 + b_{e2} t_w \left[ e_{eff} - 0.5(h_w + t_f) \right]^2 \]

\[ = 3.459 \times 10^8 \text{ mm}^4 \]
CALCULATION SHEET

\[ W_{\text{eff}} = \frac{I_{\text{eff}}}{\varepsilon_{\text{eff}} + 0.5t} = 1.270 \times 10^6 \text{ mm}^3 \]

\[ \eta_1 = \frac{68.75 \times 10^6}{460 \times 1,270 \times 10^6 / 1.1} = 0.129 \]

\[ \eta_2 = \frac{110}{119.63} = 0.920 \]

0.8 × \eta_1 + \eta_2 = 0.8 \times 0.129 + 0.920 = 1.023 < 1.4

Therefore, the resistance of the girder to interaction between concentrated load and bending moment is adequate.

**Shear resistance**

The shear buckling resistance requires checking when \( h_w / t_w \geq \frac{52}{\eta} \) for unstiffened webs.

\[ h_w / t_w = \frac{500}{4} = 125 \geq \frac{52}{1.2} \times 0.698 = 30.2 \]

Therefore the shear buckling resistance has to be checked. It is obtained as

\[ V_{b,Rd} = V_{bw,Rd} + V_{bf,Rd} \leq \frac{\eta f_{yw} h_w t_w}{\sqrt{3} \gamma_{M1}} \]

\[ V_{bw,Rd} = \frac{\chi_w f_{yw} h_w t_w}{\gamma_{M1} \sqrt{3}} \]

\[ \chi_w = \eta = 1.2 \quad \text{for } \chi_w \leq 0.60 / \eta = 0.5 \]

\[ \chi_w = 0.11 + \frac{0.64}{\chi_w^2} - 0.05 \frac{1}{\chi_w^2} \quad \text{for } \chi_w > 0.50 \]

\[ \chi_w = \left( \frac{h_w}{86.4 t_w e} \right) = \left( \frac{500}{86.4 \times 4 \times 0.698} \right) = 2.072 > 0.5 \]

\[ \chi_w = 0.11 + \frac{0.64}{2.072} - 0.05 \frac{1}{2.072^2} = 0.407 \]

The contribution from the flanges may be utilised if the flanges are not fully utilised to withstand the bending moment. However, the contribution is small and is conservatively not taken into account, i.e. \( V_{bf,Rd} = 0 \).

The shear buckling resistance can be calculated as:

\[ V_{bw,Rd} = \frac{0.407 \times 460 \times 500 \times 4}{1.1 \times \sqrt{3}} = 196.53 \text{ kN} > V_{Ed} = 55 \text{ kN} \]

The shear resistance of the girder is thus adequate.
Interaction between shear and bending

If $\eta_3$ does not exceed 0.5, the resistance to bending moment and axial force does not need to be reduced to allow for shear

$$\eta_3 = \frac{V_{Ed}}{V_{bw,Rd}} \leq 1,0$$

$$= \frac{55}{196,53} = 0,280 \leq 0,5$$, therefore interaction need not to be considered.

Concluding remarks

The resistance of the girder exceeds the load imposed. Note that the vertical stiffeners at supports have not been checked. It should be done according to the procedure used in Design Example 7.
**DESIGN EXAMPLE 9 - BEAM WITH UNRESTRAINED COMPRESSION FLANGE**

Design a staircase support beam. The beam is a single section channel, simply supported between columns. The flight of stairs lands between A and C and provides restraint to the top flange of this part of the beam. The top flange is unrestrained between B and C. The overall span of the beam is taken as 4,2 m.

**Actions**

Assuming the beam carries the load from the first run of stairs to the landing only:

- **Permanent actions (G):** Load on stairs 1,0 kN/m² = (1,0 × 2,2) = 2,2 kN/m
  Self weight of beam 0,13 kN/m

- **Variable actions (Q):** Load on stairs 4 kN/m² = (4,0 × 2,2) = 8,8 kN/m

Load case to be considered (ultimate limit state):

\[ \sum_{j} \gamma_{G,j} G_{k,j} + \gamma_{Q,1} Q_{k,1} + \sum_{i} \gamma_{Q,i} \psi_{Q,i} Q_{k,i} \]

As there is only one variable action (Q_{k,1}) the last term in the above expression does not need to be considered in this example.

\[ \gamma_{Q,1} = 1,5 \] (unfavourable effects)

**Factored actions:**

- **Permanent action:** Load on stairs = 1,35 × 2,2 = 2,97 kN/m
  Self weight of beam = 1,35 × 0,13 = 0,17 kN/m
- **Variable action:** Load on stairs = 1,5 × 8,8 = 13,2 kN/m

**Structural analysis**

Reactions at support points

\[ R_{A} + R_{B} = (2,97 + 13,2) \times 1,5 + 0,17 \times 4,2 \]

\[ = 24,97 \text{ kN} \]
Taking moments about $A$

$$R_B = \frac{1,5 \times 16,17 \times 0,75 + 0,17 \times 4,2 \times (4,2/2)}{4,2} = 4,69 \text{kN}$$

$$\Rightarrow R_A = 24,97 - 4,69 = 20,28 \text{kN}$$

Maximum bending moment occurs at a distance $1,5 \left(1 - \frac{1,5}{2 \times 4,2}\right) = 1,23 \text{m from A}$

$$M_{\text{max}} = 20,28 \times 1,23 - 16,17 \times \frac{1,23^2}{2} - 0,17 \times \frac{1,23^2}{2} = 12,58 \text{kNm}$$

Maximum shear occurs at $A$

$$F_{\text{sd}} = 20,28 \text{kN}$$

**Material properties**

Use material grade 1.4401

0,2% proof stress = 220 N/mm²

Take $f_y$ as the 0,2% proof stress = 220 N/mm²

$E = 200 \text{000 N/mm}^2$ and $G = 76 \text{900 N/mm}^2$

Try a $200 \times 75$ channel section, thickness = 5 mm

**Cross section properties**

$$I_y = 9,456 \times 10^6 \text{mm}^4 \quad W_{\text{el,y}} = 94,56 \times 10^3 \text{mm}^3$$

$$I_z = 0,850 \times 10^6 \text{mm}^4 \quad W_{\text{pl,y}} = 112,9 \times 10^3 \text{mm}^3$$

$$I_w = 5085 \times 10^6 \text{mm}^4 \quad A_g = 1650 \text{mm}^2$$

$$I_t = 1,372 \times 10^4 \text{mm}^4$$

**Classification of the cross-section**

$$\varepsilon = 1,01$$

Assume conservatively that $c = h - 2t = 200 - 10 = 190 \text{mm}$ for web

Web subject to bending: $\frac{c}{t} = \frac{190}{5} = 38$

For Class 1, $\frac{c}{t} \leq 56\varepsilon$, therefore web is Class 1

Outstand flange subject to compression: $\frac{c}{t} = \frac{75}{5} = 15$
For Class 3, \( \frac{c}{t} \leq 11.9 \), therefore outstand flange is Class 4

Therefore, overall classification of cross-section is Class 4

**Calculation of effective section properties**

Calculate reduction factor \( \rho \) for cold formed outstand elements

\[
\rho = \frac{1}{\lambda_p} - \frac{0.231}{\lambda_p^2} \quad \text{but} \quad \lambda_p \leq 1
\]

\[
\lambda_p = \frac{\bar{b}/t}{28.4e\sqrt{k_\alpha}} \quad \text{where} \quad \bar{b} = c = 75\text{mm}
\]

Assuming uniform stress distribution within the compression flange,

\[
\psi = \frac{\sigma_2}{\sigma_1} = 1
\]

\[
\Rightarrow k_\alpha = 0.43
\]

\[
\lambda_p = \frac{75/5}{28.4\times1.01\times\sqrt{0.43}} = 0.797
\]

\[
\rho = \frac{1}{0.797} - \frac{0.231}{0.797^2} = 0.891
\]

\[
c_{\text{eff}} = 0.891 \times 75 = 66.8 \text{ mm}
\]

\[
A_{\text{eff}} = A_g - (1 - \rho) c t = 1650 - (1 - 0.891) \times 75 \times 5 = 1609 \text{ mm}^2
\]

Calculate shift of neutral axis of section under bending

\[
\Delta y \cdot \gamma = \left( \frac{A_g}{2} - (1 - \rho) c t \right) \times \frac{h - t}{2} \times \frac{200}{2} - (1 - 0.891) \times 75 \times 5 = 1609
\]

\[
\bar{y} = \frac{1650 \times \frac{200}{2} - (1 - 0.891) \times 75 \times 5 \times \left( \frac{200}{2} - \frac{5}{2} \right)}{1609} = 97.53 \text{ mm}
\]
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CALCULATION SHEET

Job Title
ECSC Stainless Steel Valorisation Project

Subject
Design Example 9 – Beam with unrestrained compression flange

Client
ECSC

Made by
SMH
Date
Aug 2001

Checked by
NRB
Date
Dec 2001

Revised by
MEB
Date
April 2006

Shift of neutral axis position, \( \Delta y = \frac{h}{2} - y = \frac{200}{2} - 97.53 = 2.47 \text{ mm} \)

Calculate \( I_{eff,y} \)

\[
I_{eff,y} = \left( I_y - \frac{(1-\rho)c_t^3}{12} - (1-\rho)c_t \left( \frac{h-t}{2} \right)^2 - A_{eff} \Delta_{y-y}^2 \right)
\]

\[
I_{eff,y} = 9.456 \times 10^6 - \frac{(1-0.891) \times 75 \times 5^3}{12} - (1-0.891) \times 75 \times 5 \times (100 - 2.5)^2
\]

\[
-1609 \times 2.47^2
\]

\[
= 9.06 \times 10^6 \text{ mm}^4
\]

\[
W_{eff,y} = \frac{I_{eff,y}}{\frac{h}{2} + \Delta_{y-y}} = \frac{9.06 \times 10^6}{\frac{200}{2} + 2.47} = 88.4 \times 10^3 \text{ mm}^3
\]

Shear lag

Shear lag may be neglected provided that \( b_0 \leq L_e/50 \) for outstand elements

\( L_e = \) distance between points of zero moment = 4200 mm

\( L_e/50 = 84 \text{ mm}, \quad b_0 = 75 \text{ mm} \), therefore shear lag can be neglected

Flange curling

\[
u = \frac{2\sigma_a^2 b_s^4}{E^2 t^2 z}
\]

\( \sigma_a = \) average longitudinal stress in flange = 220 N/mm\(^2\) (maximum possible value)

\( b_s = (75 - 5) = 70 \text{ mm} \)

\( z = (100 - 2.5) = 97.5 \text{ mm} \)

\[
\therefore \quad u = \frac{2 \times 220^2 \times 70^4}{200000^2 \times 5^2 \times 97.5} = 0.024 \text{ mm}
\]

Flange curling can be neglected if \( u < 0.05 \times 200 = 10 \text{ mm} \)

Therefore flange curling is negligible

Partial safety factors

The following partial safety factors are used throughout the design example:

\( \gamma_{M0} = 1.1 \) and \( \gamma_{M1} = 1.1 \)
### Moment resistance of cross-section

For a class 4 cross section

\[ M_{c,Rd} = \frac{W_{eff, min} f_y}{\gamma_{M0}} \]

\[ M_{c,Rd} = \frac{88.4 \times 10^3 \times 220}{1.1 \times 10^6} = 17.7 \text{kNm} \]

Design moment = 12.58 kNm, \( \therefore \) cross-section moment resistance is OK

### Cross-section resistance to shear

\[ V_{p,Rd} = A_v \left( \frac{f_y}{\sqrt{3}} \right) / \gamma_{M0} \]

\[ A_v = h \times t = 200 \times 5 = 1000 \text{ mm}^2 \]

\[ V_{Rd} = \frac{1000 \times 220}{\sqrt{3} \times 1.1 \times 1000} = 115.5 \text{kN} \]

Design shear force = 20.28 kN, therefore shear resistance of cross-section is OK

Check that shear resistance is not limited by shear buckling

Assume that \( h_w = h - 2t = 200 - 10 = 190 \text{ mm} \)

\[ \frac{h_w}{t} = \frac{190}{5} = 38, \text{ shear buckling resistance needs to be checked if } \frac{h_w}{t} \leq \frac{52\varepsilon}{\eta} = 43.2\varepsilon \]

\( \therefore \) Shear resistance is not limited by shear buckling.

### Resistance to lateral torsional buckling

Compression flange of beam is laterally unrestrained between B and C. Check this portion of beam for lateral torsional buckling.

\[ M_{b,Rd} = \chi_{LT} W_{eff, y} f_y / \gamma_{M1} \] for a Class 4 cross-section

\[ W_{eff, y} = 88.4 \times 10^3 \text{ mm}^3 \]

\[ \chi_{LT} = \frac{1}{\phi_{LT} + \left( \phi_{LT}^2 - \lambda_{LT} \right)^{0.5}} \leq 1 \]

\[ \phi_{LT} = 0.5 \left( 1 + \alpha_{LT} (\lambda_{LT} - 0.4) + \lambda_{LT}^2 \right) \]

\[ \lambda_{LT} = \sqrt{\frac{W_{eff, y} f_y}{M_{cr}}} \]

Determine the elastic critical moment (\( M_{cr} \))

\[ M_{cr} = C_1 \frac{\pi^2 EI_z}{(k_z L)^2} \left( \frac{k_z}{k_w} \right)^2 I_w + \left( \frac{k_z L^2 GI_t}{\pi^2 EI_z} \right) + \left( C_2 z_g - C_3 z_j \right)^2 \right]^{1/2} \]
C is simply supported, while B approaches full fixity. Assume most conservative case: 
k_c = k_w = 1.0.

C_1, C_2 and C_3 are determined from consideration of bending moment diagram and end conditions.

From bending moment diagram, \( \psi = 0 \)
\( \Rightarrow C_1 = 1.77, \ C_2 = 0 \) and \( C_3 = 1.00 \)

\( z_j = 0 \) for a cross-section with equal flanges

\[
M_{cr} = 1.77 \times \frac{\pi^2 \times 200000 \times 0.850 \times 10^6}{(1.00 \times 2700)^2} \times \left[ \frac{(1.00)^2}{0.850 \times 10^6} + \left(1.00 \times 2700\right)^2 \times 76900 \times 1.372 \times 10^6}{\pi^2 \times 200000 \times 0.850 \times 10^6} \right]^{0.5}
\]

\( M_{cr} = 41.9 \text{ kNm} \)

\( \lambda_{LT} = \sqrt{\frac{88.4 \times 10^3 \times 220}{41.9 \times 10^6}} = 0.68 \)

Using imperfection factor \( \alpha_{LT} = 0.34 \) for cold formed sections
\( \varphi = 0.5 \left( 1 + 0.34(0.68 - 0.4) + 0.68^2 \right) = 0.779 \)

\( \chi_{LT} = \frac{1}{0.779^2 - 0.68^2}^{0.5} = 0.863 \)

\( M_{b,Rd} = 0.863 \times 88.4 \times 10^3 \times 220 \times 10^{-6} / 1.1 \)
\( = 15.3 \text{ kNm} \)

From bending moment diagram, maximum moment in unrestrained portion of beam = 12.0 kNm

Thus member has adequate resistance to lateral torsional buckling.

Deflection

Load case (serviceability limit state): \( \sum_{j=1}^{G_{k,j}} Q_{k,j} + \sum_{j=1}^{k} \psi_{0,j} Q_{k,j} \)

As there is only one variable action \( Q_{k,j} \) the last term in the above expression does not need to be considered in this example.

Secant modulus is used for deflection calculations - thus it is necessary to find the maximum stress due to unfactored permanent and variable actions.
The secant modulus $E_S = \left( \frac{E_{S1} + E_{S2}}{2} \right)$, where

$$E_{s,i} = \frac{E}{1 + 0.002 \frac{E}{\sigma_{i,Ed,ser}} \left( \frac{f_y}{\sigma_{i,Ed,ser}} \right)}$$

and $i = 1,2$

From structural analysis calculations the following were found:
- Maximum moment due to permanent actions = 1.90 kNm
- Maximum moment due to imposed actions = 6.68 kNm
- Total moment due to unfactored actions = 8.58 kNm

Section is Class 4, therefore $W_{eff}$ is used in the calculations for maximum stress in the member.

Assume, conservatively that the stress in the tension and compression flange are approximately equal, i.e. $E_{S1} = E_{S2}$.

The following constants are used to determine the secant moduli:

For grade 1.4401 stainless steel, $n$ (longitudinal direction) = 7.0

Serviceability design stress, $\sigma_{i,Ed,ser} = M_{max} / W_{eff,y} = 8.58 \times 10^6 / 88.4 \times 10^3 = 97.1$ N/mm$^2$

$$E_{s,i} = \frac{200000}{1 + 0.002 \frac{200000}{97.1} \times \left( \frac{97.1}{220} \right)} = 197348 \text{ N/mm}^2$$

Maximum deflection due to patch loading occurs at a distance of approximately 1.9 m from support $A$.

Deflection at a distance $x$ from support $A$ due to patch load extending a distance $a$ from support $A$ is given by the following formulae:

When $x \geq a$  

$$\delta = \frac{waL^4}{24aE_Sl} n^2 \left[ 2m^3 - 6m^2 + m(4 + n^2) - n^2 \right]$$

Where $m = x/L$ and $n = a/L$

When $x = 1.9$ m, and $a = 1.5$ m:  

$m = 1.9/4.2 = 0.452$, $n = 1.5/4.2 = 0.357$

Patch load (permanent+variable unfactored actions) $w = 11.0$ kN/m

Uniform load (permanent action) $w = 0.128$ kN/m

Deflection due to patch loads at a distance of 1.9 m from support $A$, $\delta_1$

$$\delta_1 = \frac{11000 \times 1.5 \times 4200^4}{24 \times 1500 \times 197348 \times 9.06 \times 10^6} \times 0.357^2 \left[ 2 \times 0.452^2 - 6 \times 0.452^2 + 0.452(4 + 0.357^2) - 0.357^2 \right]$$

$$= 7.09 \text{ mm}$$
Deflection at midspan due to self weight of beam, $\delta_2$

$$\delta_2 = \frac{5}{384} \times \frac{(w \times L) L^3}{E_s I} = \frac{5}{384} \times \frac{(0.128 \times 10^3 \times 4.2) \times 4200^3}{197348 \times 9.06 \times 10^6} = 0.29 \text{ mm}$$

Total deflection $\approx \delta_2 + \delta_2 = 7.09 + 0.29 = 7.38 \text{ mm}$

$$\delta_{\text{limiting}} \frac{\text{span}}{250} = \frac{4200}{250} = 16.8 \text{ mm}$$

Therefore deflection is acceptably small.
DESIGN EXAMPLE 10 - AXIALLY LOADED COLUMN IN FIRE

Design an unprotected rectangular hollow section subject to axial load and bending for 30 minutes fire resistance.

The column length is 2.7 m and is subject to axial load from the end reaction of a floor beam at an eccentricity of 90 mm from the narrow face of the column.

Actions

This eccentricity is taken to be 90 mm + \( h/2 \), where \( h \) is the depth of the section. Thus the beam introduces a bending moment about the column’s major axis.

The unfactored actions are:

- Permanent action: 6 kN
- Variable action: 7 kN

The column will initially be checked at the ultimate limit state (LC1) and subsequently at the fire limit state (LC2) for a fire duration of 30 minutes. The loadcases are as follows:
LC1 (ultimate limit state) \[ \sum_j \gamma_{G,j} G_{k,j} + \gamma_{Q,1} Q_{k,1} \]  
\( \gamma_{G,j} = 1,35 \) (unfavourable effects)  
\( \gamma_{Q,1} = 1,5 \)  

LC2 (fire limit state) \[ \sum_j \gamma_{G_A,j} G_{k,j} + \psi_{1,1} Q_{k,1} \]  
\( \gamma_{G_A} = 1,0 \)  
Values for \( \psi_{1,1} \) are given in EN 1990 and NA for EN 1990, but for this example conservatively assume \( \psi_{1,1} = 1,0 \)

**Design at the Ultimate Limit State (LC1)**

Loading on the corner column due to shear force at end of beam (LC1):

Axial force \( N_{Ed} = 1,35 \times 6 + 1,5 \times 7 = 18,6 \text{ kN} \)

Try 100 × 50 × 6 Rectangular Hollow Section

Major axis bending moment (due to eccentricity of shear force from centroid of column),  
\( M_{N,Ed} = 18,6 \times (0,09+0,10/2) = 2,60 \text{ kNm} \)

**Material properties**

Use material grade 1.4401  
0,2% proof stress = 220 N/mm\(^2\) and \( f_u = 530 \text{ N/mm}^2 \)

Take \( f_y \) as the 0,2% proof stress = 220 N/mm\(^2\)  
\( E = 200 000 \text{ N/mm}^2 \) and \( G = 76 900 \text{ N/mm}^2 \)

**Cross-section properties – 100 × 50 × 6 mm RHS**

\( W_{el,y} = 32,58 \times 10^3 \text{ mm}^3 \) \( i_y = 32,9 \text{ mm} \)

\( W_{pl,y} = 43,75 \times 10^3 \text{ mm}^3 \) \( i_z = 19,1 \text{ mm} \)

\( A_g = 1500 \text{ mm}^2 \) \( t = 6 \text{ mm} \)

**Classification of the cross-section**

\( \varepsilon = 1,01 \)  
Assume conservatively that \( c = h - 2t = 100 - 12 = 88 \text{ mm} \) for web

Webs subject to compression: \( \frac{c}{t} = \frac{88}{6} = 14,7 \)

For Class 1, \( \frac{c}{t} \leq 25,7 \varepsilon = 25,96 \) \( \therefore \) Web is Class 1
By inspection, if the web is Class 1 subject to compression, then the flange will also be Class 1. \(\therefore\) Cross-section is Class 1

**Partial safety factors**

The following partial safety factors are used throughout the design example for LC1:

- \(\gamma_{M0} = 1.1\)
- \(\gamma_{M1} = 1.1\)

**Buckling resistance to axial compression**

Resistance to flexural buckling about the \(z-z\) axis:

\[
N_{b,z,Rd} = \frac{z A_s f_y}{\gamma_{M1}}
\]

For Class 1, 2 and 3 cross-sections

\[
\chi = \text{reduction factor to account for buckling} = \frac{1}{\psi + \left[\psi^2 - \chi^2\right]^{0.5}} \leq 1
\]

\[
\psi = 0.5 \left(1 + \alpha(\bar{\chi} - \bar{\chi}_0) + \bar{\chi}^2\right)
\]

\[
\bar{\chi} = \frac{L_{cr} 1}{i_z} \sqrt{\frac{f_y}{E}}
\]

\(L_{cr} = \text{buckling length of column, taken conservatively as } 1.0 \times \text{column length } = 2.7 \text{ m}\)

\[
\bar{\chi} = \frac{2700 1}{19.1 \pi} \sqrt{\frac{220}{200000}} = 1.492
\]

For hollow sections subject to flexural buckling, \(\alpha = 0.49\) and \(\bar{\chi}_0 = 0.40\)

\[
\psi = 0.5 \left(1 + 0.49(1.492 - 0.4) + 1.492^2\right) = 1.881
\]

\[
\chi = \frac{1}{1.881 + \left[1.881^2 - 1.492^2\right]^{0.5}} \leq 1
\]

\[
\chi = 0.3305
\]

\[
N_{b,z,Rd} = \frac{0.3305 \times 1500 \times 220}{1.1} = 99.15 \text{ kN}
\]

(Resistance to torsional buckling will not be critical for a rectangular hollow section with a \(h/b\) ratio of 2.)

\[
N_{Ed} = 18.6 \text{ kN} \quad \text{Buckling resistance of cross-section is OK}
\]
Axial compression and bending resistance

Cross sectional resistance interaction check

\[
\frac{N_{Ed}}{N_{c,Rd}} + \frac{M_{y,Ed} + N_{Ed} e_{Ny}}{M_{c,y,Rd}} + \frac{M_{z,Ed} + N_{Ed} e_{Nz}}{M_{c,z,Rd}} \leq 1
\]

\[
N_{c,Rd} = \frac{A_g f_y}{\gamma_{M0}} = \frac{1500 \times 220}{1,1} = 300 \text{ kN}
\]

\[
e_{Ny} = e_{NZ} = 0
\]

\[
M_{z,Ed} = 0
\]

\[
M_{c,y,Rd} = \frac{W_{pl,y} f_y}{\gamma_{M0}} = \frac{43,75 \times 10^3 \times 220}{1,1} = 8,75 \text{ kNm}
\]

\[
\frac{N_{Ed}}{N_{c,Rd}} + \frac{M_{y,Ed}}{M_{c,y,Rd}} = \frac{18,6}{300} + \frac{2,60}{8,75} = 0,062 + 0,297 = 0,359 < 1,00
\]

\[\therefore\text{ Resistance of cross-section is OK}\]

Buckling resistance interaction check

\[
\frac{N_{Ed}}{\left(\frac{N_{b,Rd}}{N_{b,Rd,y}}\right)_{\text{min}}} + k_y \left(\frac{M_{y,Ed} + N_{Ed} e_{Ny}}{\beta_{W,y} W_{pl,y} f_y / \gamma_{M1}}\right) \leq 1
\]

\[
\beta_{W,y} = 1,0 \text{ for Class 1 cross-sections}
\]

\[
k_y = 1,0 + 2\left(\bar{\chi}_y - 0,5\right)\frac{N_{Ed}}{\frac{N_{b,Rd}}{N_{b,Rd,y}}} \text{ but } 1.2 \leq k_y \leq 1,2 + 2\left(\frac{N_{Ed}}{\frac{N_{b,Rd}}{N_{b,Rd,y}}}\right)
\]

Determine \(N_{b,Rd,y}\) using the same method used to calculate \(N_{b,Rd,z}\) given on sheet 3.

For hollow sections subject to flexural buckling, \(\alpha = 0,49\) and \(\bar{\lambda}_0 = 0,40\)

\[
\frac{L_{cr}}{\overline{\lambda}_y} = \frac{1}{\pi} \sqrt{\frac{f_y}{E}} = \frac{2700}{32,9} \left(\frac{1}{200000}\right) = 0,866
\]

\[
\phi = 0,5 (1 + 0,49(0,866 - 0,4) + 0,866^2) = 0,989
\]

\[
\chi_y = \frac{1}{0,989 + \left[0,989^2 - 0,866^2\right]^{0,5}} \leq 1
\]

\[
\chi_y = 0,682 < 1,0
\]

\[
\frac{N_{b,Rd,y}}{1,1} = 0,682 \times 1500 \times 220 = 204,6 \text{ kN}
\]
Design at the Fire Limit State (LC2)

For LC2, the column is designed for the following axial loads and moments.

Axial compressive force, $N_{f,Ed} = 1,0 \times 6 + 1,0 \times 7 = 13,0$ kN

Maximum bending moment $M_{y,fi,Ed} = 13,0 \times (0,09+0,05) = 1,82$ kNm

Determine temperature in steel after 30 minutes fire duration

Assume that the section is unprotected and that there is a uniform temperature distribution within the steel section. Increase in temperature during time interval $\Delta t$ is found from:

$$
\Delta \theta_{a,t} = \frac{A_m/V}{c_m \rho_m} h_{net,d} \Delta t 
$$

Eq. 7.34

$$
\dot{h}_{net,d} = \dot{h}_{net,c} + \dot{h}_{net,r} 
$$

Eq. 7.35

$$
\dot{h}_{net,c} = \alpha_c (\theta_g - \theta_a) 
$$

Eq. 7.36

Where:

$\theta_g$ = gas temperature of the environment of the member in fire exposure, given by the nominal temperature time curve:

$\theta_g = 20 + 345\log_{10}(8t + 1)$

Eq. 7.38

$\theta_a$ = surface temperature of the member

$\dot{h}_{net,r} = \varphi e_{res} 5,67 \times 10^{-8} \left(\theta_g + 273\right)^4 - \left(\theta_a + 273\right)^4$

Eq. 7.37

Initial input values for determination of final steel temperature are as follows:

$A_m/V = 200$ m$^{-1}$

$\alpha_c = 25$ W/m$^2$K

Thus member is OK for combined axial loading and uniaxial moment under LC1.
**Initial steel temperature**, $\theta_a = 20^\circ$C

**Resultant emissivity**, $\varepsilon_{res} = 0,2$

**Unit mass of stainless steel**, $\rho_a = 7850 \text{ kg/m}^3$

**Configuration factor**, $\varphi = 1,0$

The specific heat is temperature-dependent and is given by the following expression:

$$c_a = 450 + 0,28 \theta_a - 2,91 \times 10^{-4} \theta_a^2 + 1,34 \times 10^{-7} \theta_a^3 \text{ J/kgK}$$  
Eq. 7.4

$\Delta t = 2$ seconds

The above formulae and initial input information were coded in an Excel spreadsheet and the following steel temperature, after a fire duration of 30 minutes, was obtained.

$\theta_a = 811^\circ$C

**Reduction of mechanical properties at elevated temperature**

The following reduction factors are required for calculation of resistance at elevated temperatures.

- **Young’s modulus retention factor** $k_{E,0} = E_0/E$
- **0,2% proof strength retention factor** $k_{0,2\text{proof},0} = f_{0,2\text{proof},0}/f_y$
- **Ultimate tensile strength retention factor** $k_{u,0} = f_{u,0}/f_y$

The value of the 2% yield strength at elevated temperature is also required for resistance calculations. This is given by the following expression:

$$f_{2,0} = f_{0,2\text{proof},0} + 2 \theta_a (f_{u,0} - f_{0,2\text{proof},0})$$  
Eq. 7.1

The values for the retention factors at 811°C are obtained by linear interpolation.

- $k_{0,2\text{proof},0} = 0,377$
- $k_{u,0} = 0,322$
- $k_{E,0} = 0,610$
- $g_{2\theta} = 0,353$

Thus

- $f_{2,0} = 0,377 \times 220 + 0,353 \times (0,322 \times 530 - 0,377 \times 220) = 113,9 \text{ N/mm}^2$
- $k_{2,0} = 113,9/220 = 0,518$

**Partial safety factor**

$\gamma_{M,fi} = 1,0$

**Buckling resistance**

$$N_{b,fi,Rd} = \gamma_{P,fi} A_p k_{0,2\text{proof},0} f_y / \gamma_{M,fi}$$  
Section 7.1

**Section 7.4.3**

**Eq. 7.8**
\[ \chi = \frac{1}{\varphi_0 + \sqrt{\varphi_0^2 - \lambda^2}} \]  

but \( \leq 1,0 \)

\[ \varphi_0 = 0,5 \left( 1 + \alpha \left( \lambda_{0,\theta} - \lambda_0 \right) \right) \]

\[ \lambda_{Z,\theta} = \lambda_{z} \left[ \frac{k_{0,2,\text{proof},0}/k_{E,\theta}}{0,5} \right] = 1,492 \times (0,377/0,610)^{0,5} = 1,173 \]

For flexural buckling of a hollow section, \( \alpha = 0,49 \) and \( \lambda_0 = 0,4 \)  

\[ \varphi_{\theta,\theta} = 0,5 \left( 1 + 0,49 (1,173 - 0,4) + 1,173^2 \right) = 1,377 \]

\[ \chi_{z,\theta} = \frac{1}{\lambda_{z} + \sqrt{\lambda_{z}^2 - 1,173^2}} = 0,477 \]

\[ N_{b,\text{fl},\text{Rd}} = 0,477 \times 1500 \times 0,377 \times 220/1,0 = 59,3 \text{ kN} \]

\[ N_{\text{fl},\text{Ed}} = 13,0 \text{ kN} \], buckling resistance of member is OK

**Axial compression and bending moment**

The following expression for a class 1 cross section must be satisfied

\[ \frac{N_{\text{fl},\text{Ed}}}{A_g k_{0,2,\text{proof},\theta} f_y} + \frac{k_y M_{y,\text{fl},\text{Ed}}}{M_{y,\text{fl},0,\text{Rd}}} + \frac{k_z M_{z,\text{fl},\text{Ed}}}{M_{z,\text{fl},0,\text{Rd}}} \leq 1 \]

In which

\[ k_y = 1 - \frac{\mu_y N_{\text{fl},\text{Ed}}}{\chi_{y,\text{fl}} A_g k_{0,2,\text{proof},\theta} f_y} \leq 3 \]

\[ \mu_y = \left( (1,2,\beta_{M,y} - 3)\lambda_{y,0} + 0,44 \beta_{M,y} - 0,29 \right) \leq 0,8 \]

\[ \lambda_{y,0} = 0,866 \]

\[ \lambda_{y} = \lambda_{y} \left[ \frac{k_{0,2,\text{proof},0}/k_{E,\theta}}{0,5} \right] = 0,866 \times (0,377/0,610)^{0,5} = 0,681 \]

Assume the column is fixed at the base, a triangular bending moment distribution occurs and \( \beta_M = 1,8 \)

\[ \mu_y = (1,2 \times 1,8 - 3) \times 0,681 + 0,44 \times 1,8 - 0,29 \]

\[ = -0,070 \]

\[ \varphi_{\theta,\theta} = 0,5 \left( 1 + 0,49 (0,681 - 0,4) + 0,681^2 \right) = 0,801 \]

\[ \chi_{z,\theta} = \frac{1}{0,801 + \sqrt{0,801^2 - 0,681^2}} = 0,818 \]
\[ k_y = 1 - \frac{(-0.07) \times 13.0 \times 10^3}{0.818 \times 1500 \times 0.377 \times \frac{220}{1.00}} = 1.009 < 3.0 \]

Interaction expression:

\[ \frac{N_{f,i,Ed}}{\chi_{\min,fi}} = \frac{k_y M_{y,f,i,Ed}}{M_{y,f,i,Rd}} + \frac{k_y M_{y,f,i,Ed}}{M_{y,f,i,Rd}} \]

\[ M_{y,f,i,Rd} = k_{2,0} \left( \frac{\gamma_{M_0}}{\gamma_{M_{f,i}}} \right) M_{Rd} = 0.518 \times \left( \frac{1.1}{1.0} \right) \times 8.75 = 4.99 \text{ kNm} \]

\[ \frac{13.0 \times 10^3}{0.477 \times 1500 \times 0.377 \times \frac{220}{1.00}} + \frac{1.009 \times 1.82}{4.99} = 0.219 + 0.368 = 0.587 \]

\[ 0.587 < 1.00 \]

Thus section is OK in fire conditions for combined axial load and bending.
DESIGN EXAMPLE 11 – DESIGN OF A TWO-SPAN TRAPEZOIDAL ROOF SHEETING

This example deals with a two-span trapezoidal roof sheeting with a thickness of 0.6 mm from stainless steel grade 1.4401 CP500, i.e. cold worked to a yield strength of 500 N/mm². Comparisons will be made to a similar sheeting of grade 1.4401 in the annealed condition, i.e. $f_y = 240$ N/mm² (see also Design Example 3).

If the nominal yield strength in all directions of the sheet is not guaranteed by the producer it should be reduced to 80% of its value. In this example it is assumed that the strength was not guaranteed in order to demonstrate this.

The dimensions of the roof sheeting are shown below.

A detailed sketch of the roof sheeting is given in the figure below. The lower flange will be in compression over the mid support and therefore this case will be checked in this example.

Mid line dimensions:

- $h_0 = 70$ mm
- $w_0 = 212.5$ mm
- $b_{u0} = 57$ mm
- $b_r = 20$ mm
- $h_r = 6$ mm
- $b_{ro} = 8$ mm
- $b_{lo} = 65$ mm

radius, $r = 3$ mm

angle, $\varphi = 57.1^\circ$
CALCULATION SHEET

Data
Span length \( L = 3.5 \text{ m} \)
Load \( q = 1.4 \text{ kN/m}^2 \)
Self weight \( g = 0.07 \text{ kN/m}^2 \)
Sheeting thickness \( t = 0.6 \text{ mm} \)
Width of support \( s = 100 \text{ mm} \)
Yield strength \( f_y = 0.8 \times 500 = 400 \text{ N/mm}^2 \)
Modulus of elasticity \( E = 200000 \text{ N/mm}^2 \)

Partial factor \( \gamma_{M0} = 1.1 \)
Partial factor \( \gamma_{M1} = 1.1 \)
Load factor \( \gamma_G = 1.35 \) (permanent loads)
Load factor \( \gamma_Q = 1.5 \) (variable loads)

Effective section properties
Maximum width-to-thickness ratios
\[ \max \left( \frac{b_0}{t}, \frac{b_{w0}}{t} \right) = \frac{b_0}{t} = 108 < 400 \]
\[ h_0 / t = 117 < 400 \]

Location of the centroidal axis when the web is fully effective
Effective width of the compression flange
\[
\begin{align*}
    b_p &= \frac{b_{00} - b_t}{2} = 22.5 \text{ mm} \\
    \varepsilon &= \sqrt{\frac{235 \times E}{f_y \times 210000}} = 0.75 \\
    k_e &= 4 \\
    \bar{x}_p &= \frac{b_p / t}{28.4 \varepsilon \sqrt{k_e}} = 0.883 \\
    \rho &= \frac{0.772}{\bar{x}_p} - \frac{0.125}{\bar{x}_p^2} = 0.714 \\
    b_{eff,l} &= \rho b_p = 16.1 \text{ mm}
\end{align*}
\]

Reduced thickness of the flange stiffener:
The lower compressed flange is shown in detail below.
Effective thickness of the inclined part of the stiffener

\[ t_{\text{nl}} = \frac{\sqrt{\left(\frac{b_{\text{nl}} - b_{\text{nl0}}}{2}\right)^2 + h_{\text{t}}^2} \cdot t}{h_{\text{t}}} = 0,85 \text{ mm} \]

\[ A_s = (b_{\text{eff}} + b_{\text{nl}}) t + 2 h_{\text{t}} t_{\text{nl}} = 24,62 \text{ mm}^2 \]

\[ e_s = \frac{b_{\text{nl}} h_{\text{t}} + 2 h_{\text{t}} \frac{h_{\text{t}}}{2} t_{\text{nl}}}{A_s} = 2,41 \text{ mm} \]

The second moment of area for the stiffener is calculated with two strips of width 15t adjacent to the stiffener (smaller terms neglected)

\[ I_s = 2 \times 15 t^2 e_s^2 + b_{\text{nl}} (h_{\text{t}} - e_s)^2 + 2 h_{\text{t}} t_{\text{nl}} \left(\frac{h_{\text{t}}}{2} - e_s\right)^2 + 2 t_{\text{nl}} h_{\text{t}}^3 \frac{12}{12} = 159,1 \text{ mm}^4 \]

\[ b_s = 2 \sqrt{h_{\text{t}}^2 + \left(\frac{b_{\text{nl}} - b_{\text{nl0}}}{2}\right)^2} + b_{\text{nl0}} = 24,97 \text{ mm} \]

\[ l_b = 3,07 \sqrt{\frac{I_s h_{\text{t}} (2b_p + 3b_{\text{nl}})}{t^3}} = 251,0 \text{ mm} \]

\[ s_w = \sqrt{\left(\frac{w_0 - b_{\text{nl0}} - b_{\text{nl0}}}{2}\right)^2 + h_{\text{t}}^2} = 83,4 \text{ mm} \]

\[ b_d = 2b_p + b_s = 70,0 \text{ mm} \]

\[ k_{wo} = \frac{s_w + 2b_d}{s_w + 0,5b_d} = 1,37 \]

\[ l_b / s_w = 3,01 > 2 \rightarrow k_w = k_{wo} = 1,37 \]

\[ \sigma_{\text{cr,s}} = \frac{4,2 k_w E}{A_s} \sqrt{\frac{I_s t}{4 h_{\text{t}}^2 (2b_p + 3b_{\text{nl}})}} = 557,5 \text{ N/mm}^2 \]

\[ \chi_d = \sqrt{\frac{f_s}{\sigma_{\text{cr,s}}}} = 0,85 \rightarrow \chi_d = 1,47 - 0,723 \chi_d = 0,86 \]

\[ t_{\text{red}} = \chi_d t = 0,51 \text{ mm} \]

Optionally iterate to refine the value of the reduction factor for buckling of the stiffener.
Distance to the neutral axis from the compressed flange (fully effective web)

\[ A_{\text{tot}} = \sum A_i = 84,0 \text{ mm}^2 \]

\[ e_c = \sum \frac{A_i e_i}{A_{\text{tot}}} = 36,3 \text{ mm} \]

**Effective cross-section of the web**

\[ \psi = \frac{h_0}{e_c} = -0,929 \quad k_{\sigma} = 7,81 - 6,29\psi + 9,78\psi^2 = 22,1 \]

\[ b_{p,w} = s_w = 83,4 \text{ mm} \quad \bar{\lambda}_p = \frac{b_{p,w}}{t} = 1,391 \]

\[ \rho = \frac{0,772}{\bar{\lambda}_p} - \frac{0,125}{\bar{\lambda}_p^2} = 0,490 \quad b_{\text{eff},w} = \rho \frac{b_{p,w}}{1-\psi} = 21,2 \text{ mm} \]

\[ s_{\text{eff},1} = 0,4b_{\text{eff},w} = 8,47 \text{ mm} \quad s_{\text{eff},2} = 0,6b_{\text{eff},w} = 12,7 \text{ mm} \]

**Effective cross section properties per half corrugation**

\[ A_{\text{eff, tot}} = \sum A_{\text{eff,i}} = 70,8 \text{ mm}^2 \]

\[ e_{\text{eff,c}} = \sum \frac{A_{\text{eff,i}} e_{\text{eff,i}}}{A_{\text{eff,tot}}} = 40,0 \text{ mm} \]

\[ I_{\text{tot}} = \sum I_{\text{eff,i}} + \sum A_{\text{eff,i}} (e_c - e_{\text{eff,i}})^2 = 51710 \text{ mm}^4 \]

**Bending resistance per unit width (1m)**

\[ I = I_{\text{tot}} \frac{1000 \text{ mm}}{0,5w_0} = 486685 \text{ mm}^4 \]

\[ W_{\text{eff,i}} = \frac{I}{e_c} = 12165 \text{ mm}^3 \quad W_{\text{eff,u}} = \frac{I}{h_0 - e_c} = 16227 \text{ mm}^3 \]

\[ W_{\text{eff,i}} < W_{\text{eff,u}} \Rightarrow W_{\text{eff,min}} = W_{\text{eff,i}} \]

\[ M_{c,Rd} = W_{\text{eff,min}} f_y / \gamma_{M0} = 4,42 \text{ kNm} \]
Resistance to local transverse forces at intermediate support

Resistance to local transverse forces per unit width (1 m)

\[ \alpha = 0.15 \text{ (for sheeting profiles)} \quad \text{and} \quad l_a = s_s \]

\[ R_{w,Rd} = \alpha t^2 \sqrt{f_y E \left( 1 - \frac{1}{2} \sqrt{\frac{t}{r}} \right)} \left[ 0.5 + \sqrt{0.02 l_a / t} \right] (2.4 + (\varphi / 90)^2) \frac{1000 \text{ mm}}{0.5 w_0} \gamma_M \]

\[ R_{w,Rd} = 20.9 \text{ kN} \]

Interaction between bending moment and transverse force

The maximum bending moment will appear at the intermediate support where it will interact with the support reaction and therefore the following checks must be performed.

\[ \frac{M_{Ed}}{M_{c,Rd}} \leq 1 \quad \frac{F_{Ed}}{R_{w,Rd}} \leq 1 \quad \frac{M_{Ed}}{M_{c,Rd}} + \frac{F_{Ed}}{R_{w,Rd}} \leq 1.25 \]

Design load per unit width (1 m)

\[ q_d = \gamma_G q + \gamma_Q q = 2.20 \text{ kN/m} \]

The design load, \( q_d \), gives the following bending moment and support reaction at the intermediate support.

\[ M_{Ed} = \frac{qL^2}{8} = 3.37 \text{ kNm} \quad F_{Ed} = \frac{5}{4} qL = 9.63 \text{ kN} \]

\[ \frac{M_{Ed}}{M_{c,Rd}} = 0.76 \quad \frac{F_{Ed}}{R_{w,Rd}} = 0.46 \quad \frac{M_{Ed}}{M_{c,Rd}} + \frac{F_{Ed}}{R_{w,Rd}} = 1.22 \quad \text{OK} \]

Deflection at serviceability limit state

For verification in the serviceability limit state the effective width of compression elements should be based on the compressive stress in the element under serviceability limit state loading. The maximum compression stress is calculated as follows. A conservative approximation is made based on \( W_{\text{eff,min}} \) from ultimate limit state.

\[ M_{Ed,ser} = \frac{(q + g)L^2}{8} = 2.25 \text{ kNm} \]

\[ \sigma_{\text{com,Ed,ser}} = \frac{M_{Ed,ser}}{W_{\text{eff,min}}} = 186 \text{ N/mm}^2 \]

Now, the effective section properties are determined as before but with \( f_y \) replaced by \( \sigma_{\text{com,Ed,ser}} \). The calculations will not be shown here but the interesting results are:

\[ I = 573 \ 150 \text{ mm}^4 \]
\[ W_c = 15 \ 866 \text{ mm}^3 \]
\[ W_t = 16 \ 919 \text{ mm}^3 \]
Determination of the deflection:
Secant modulus corresponding to the stresses in the tension and compression flange respectively.
\[
\sigma_{1,\text{Ed,ser}} = \frac{M_{\text{Ed,ser}}}{W_u} = 142 \text{ N/mm}^2
\]
\[
\sigma_{2,\text{Ed,ser}} = \frac{M_{\text{Ed,ser}}}{W_1} = 133 \text{ N/mm}^2
\]
\[
E_{s,1} = \frac{E}{1 + 0,002 \frac{E}{f_y} \left( \frac{\sigma_{1,\text{Ed,ser}}}{f_y} \right)^n} = 199 \, 604 \text{ N/mm}^2 \quad n = 7,0
\]
\[
E_{s,2} = \frac{E}{1 + 0,002 \frac{E}{f_y} \left( \frac{\sigma_{2,\text{Ed,ser}}}{f_y} \right)^n} = 199 \, 730 \text{ N/mm}^2
\]
\[
E_s = \frac{E_{s,1} + E_{s,2}}{2} = 199 \, 667 \text{ N/mm}^2
\]

As a simplification, the variation of \( E_s \) along the length of the member may be neglected and the minimum value of \( E_s \) of that member may conservatively be used throughout its length, i.e.
\( E_s = E_{s,1} = 199 \, 603 \text{ N/mm}^2 \)

The permitted deflection is \( L/300 = 11,7 \text{ mm} \)
\[
x = \frac{1+\sqrt{33}}{16} L = 1,47 \text{ m} \quad \text{(location of maximum deflection)}
\]
\[
\delta = \frac{(g+q)L^4}{48E_{s,1}I} \left( \frac{x}{L} - 3 \frac{x^3}{L^3} + 2 \frac{x^4}{L^4} \right) = 10,4 \text{ mm} \quad \text{OK}
\]

Comparison with sheeting in grade 1.4401 in the annealed condition
The bending resistance per unit width of identical sheeting in grade 1.4401 in the annealed condition \( (f_y = 240 \text{ N/mm}^2) \) is:
\[
M_{c,Rd} = 3,22 \text{ kNm}
\]

and the resistance to local transverse forces is:
\[
R_{w,Rd} = 16,2 \text{ kN}
\]

With sheeting made from grade 1.4401 in the annealed condition, the span must be reduced to 2,9 m compared to 3,5 m for material in the cold worked strength condition. Hence, sheeting made from cold worked material enables the span to be increased, meaning that the number of secondary beams or purlins could be reduced, leading to cost reductions.
DESIGN EXAMPLE 12 – DESIGN OF A LIPPED CHANNEL IN AN EXPOSED FLOOR

Design a simply supported beam with a lipped channel in an exposed floor. The material is stainless steel grade 1.4401 CP500, i.e. cold worked to a yield strength of 500 N/mm². The beam is simply supported with a span, \( l \) of 4 m. The distance between adjacent beams is 1 m.

As the load is not applied through the shear centre of the channel, it is necessary to check the interaction between the torsional resistance of the cross-section and the lateral torsional buckling resistance of the member. However, this example only checks the lateral torsional buckling resistance of the member.

Factors
Partial factor \( \gamma_M = 1,1 \) and \( \gamma_{M1} = 1,1 \)  
Load factor \( \gamma_G = 1,35 \) (permanent loads) and \( \gamma_Q = 1,5 \) (variable loads)  

Table 2.1
Section 2.3.2

Actions
Permanent actions \( (G) \): 2 kN/m² 
Variable actions \( (Q) \): 3 kN/m² 

Load case to be considered in the ultimate limit state:
\[
q^* = \sum_j \gamma_{G,j} G_{k,j} + \gamma_{Q,j} Q_{k,j} = 7,2 \text{ kN/m}
\]

Structural Analysis
Reactions at support points (Design shear force)
\[
V_{Ed} = \frac{q^* \times 4}{2} = 14,4 \text{ kN}
\]

Design bending moment
\[
M_{Ed} = \frac{q^* \times 4^2}{8} = 14,4 \text{ kNm}
\]

Material Properties
Yield strength \( f_y = 500 \text{ N/mm}^2 \)  
Modulus of elasticity \( E = 200 \text{ 000 N/mm}^2 \)  
Shear modulus \( G = 76900 \text{ N/mm}^2 \)  

Table 3.5  
Section 3.2.4

Cross-section Properties
The influence of rounded corners on cross-section resistance may be neglected if the internal radius \( r \leq 5t \) and \( r \leq 0,10b_p \) and the cross section may be assumed to consist of plane elements with sharp corners. For cross-section stiffness properties the influence of rounded corners should always be taken into account.  

Section 4.6.2
**CALCULATION SHEET**

- **Job No.**
- **Sheet**
- **2 of 7**
- **Rev**
- **A**

**Job Title**
RFCS Stainless Steel Valorisation Project

**Subject**
Design Example 12 – Design of a lipped channel in a exposed floor

**Client**
RFCS

**Made by**
ER/EM

**Date**
Feb 2006

**Checked by**
HB

**Date**
March 2006

---

**Figure 4.5**

\[
\begin{align*}
&b_p = b - t - 2g_r = 115.6 \text{ mm} \\
g_r = r_m [\tan(\phi/2) - \sin(\phi/2)] = 2.2 \text{ mm} \\
r_m = r + t/2 = 7.5 \text{ mm} \\
r = 5 \text{ mm} \leq 5t = 25 \text{ mm} \\
r = 5 \text{ mm} \leq 0.10b_p = 11.56 \text{ mm}
\end{align*}
\]

The influence of rounded corners on section properties may be taken into account with sufficient accuracy by reducing the properties calculated for an otherwise similar cross-section with sharp corners, using the following approximations:

- **Notional flat width of the flange**, \( b_{p,f} = b - t - 2g_r = 115.61 \text{ mm} \)
- **Notional flat width of the web**, \( b_{p,w} = h - t - 2g_r = 150.61 \text{ mm} \)
- **Notional flat width of the lip**, \( b_{p,l} = c - t/2 - g_r = 25.30 \text{ mm} \)

- **\( A_g,sh = 2162 \text{ mm}^2 \)**
- **\( I_{yg,sh} = 9.069 \times 10^6 \text{ mm}^4 \)**
- **\( \delta = 0.43 \sum_{j=1}^m f_j \frac{\phi_j}{90^\circ} / \sum_{i=1}^m b_{p,i} = 0.02 \)**

\[
\begin{align*}
A_g &= A_{g,sh} (1 - \delta) = 2119 \text{ mm}^2 \\
I_g &= I_{yg,sh} (1 - 2\delta) = 8.708 \times 10^6 \text{ mm}^4
\end{align*}
\]

**Classification of the cross-section**

\[
\varepsilon = \left[ \frac{235}{210000} \right]^{0.5} = 0.669
\]

**Flange:** Internal compression parts. Part subjected to compression.

- **\( c = b_p = b - t - 2g_r = 115.6 \text{ mm} \)**
- **\( c/t = 23.12 > 30.7 \varepsilon \), therefore the flanges are Class 4**

**Web:** Internal compression parts. Part subjected to bending.
Calculation of the effective section properties

**Flange effective width:** Internal compression elements. Part subjected to compression.

\[ \bar{b} = b_p = b - t - 2g_r = 115.6 \text{ mm} \]

Assuming uniform stress distribution in the compression flange:

\[ \psi = \frac{\sigma_2}{\sigma_1} = 1 \quad \text{and the buckling factor} \quad k_\sigma = 4 \]

\[ \bar{x}_p = \frac{\bar{b}/t}{28.4 \sqrt{k_\sigma}} = 0.608 \]

Cold formed internal elements:

\[ \rho = \frac{0.772}{\bar{x}_p} - \frac{0.125}{\bar{x}_p^2} = 0.9311 < 1 \]

\[ b_{\text{eff}} = \rho \bar{b} = 107.64 \text{ mm}, \quad b_{\text{eff}} = 0.5b_{\text{eff}} = 53.82 \text{ mm}, \quad b_{\text{eff}} = 0.5b_{\text{eff}} = 53.82 \text{ mm} \]

**Effects of shear lag**

Shear lag in flanges may be neglected if \( b_0 < L_e/50 \), where \( b_0 \) is taken as the flange outstand or half the width of an internal element and \( L_e \) is the length between points of zero bending moment.

For internal elements: \( b_0 = (b-t)/2 = 60 \text{ mm} \)

The length between points of zero bending moment: \( L_e = 4000 \text{ mm}, \quad L_e/50 = 80 \text{ mm} \)

Therefore shear lag can be neglected.

**Flange curling**

\[ u = 2 \frac{\frac{\sigma^2}{2} b_s^4}{E z^2 t^2} = 2.55 \text{ mm} \]

\( b_s = 141 \text{ mm} \) is the distance between webs

\( t = 5 \text{ mm} \)

\( z = 77.5 \text{ mm} \) is the distance of the flange under consideration from neutral axis

\( \sigma_1 \) is mean stress in the flanges calculated with gross area (\( f_y = 500 \text{ N/mm}^2 \) is assumed)

Flange curling can be neglected if it is less than 5% of the depth of the profile cross-section:

\( u = 2.55 \text{ mm} < 0.05h = 8 \text{ mm} \), therefore flange curling can be neglected.
Stiffened elements. Edge stiffeners

Distortional buckling. Plane elements with edge stiffeners

**Step 1:** Initial effective cross-section for the stiffener

For flanges (as calculated before)

\[ b = 125 \text{ mm} \]
\[ b_p = 115.61 \text{ mm} \]
\[ b_{\text{eff}} = 107.65 \text{ mm} \]
\[ b_{\text{eff}} = 0.5b_{\text{eff}} = 53.82 \text{ mm} \]
\[ b_{\text{eff}} = 0.5b_{\text{eff}} = 53.82 \text{ mm} \]

For the lip, the effective width \( c_{\text{eff}} \) should be calculated using the corresponding buckling factor \( k_\sigma, \lambda_p \) and \( \rho \) expressions as follows:

\[ b_{p,c} = c - t / 2 - \rho \lambda_p = 25.30 \text{ mm} \]
\[ b_p = 115.6 \text{ mm} \]
\[ b_{p,c} / b_p = 0.22 < 0.35 \quad \text{then} \quad k_\sigma = 0.5 \]

\[ \lambda_p = \frac{b_t}{28.4 k_\sigma \sqrt{\rho}} = 0.45 \quad (\bar{b} = 30 \text{ mm}) \]

Cold formed outstand elements:

\[ \rho = \frac{1}{\lambda_p} - \frac{0.231}{\lambda_p^2} = 1.08 > 1 \quad \text{then} \quad \rho = 1 \]

\[ c_{\text{eff}} = \rho b_{p,c} = 25.30 \text{ mm} \]

**Step 2:** Reduction factor for distortional buckling

Calculation of geometric properties of effective edge stiffener section

\[ b_{\text{eff}} = 53.82 \text{ mm} \]
\[ c_{\text{eff}} = 25.30 \text{ mm} \]
\[ A_s = (b_{\text{eff}} + c_{\text{eff}})t = 395.64 \text{ mm}^2 \]
**Job Title**: RFCS Stainless Steel Valorisation Project

**Subject**: Design Example 12 – Design of a lipped channel in an exposed floor

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**Job No.** | **Sheet** | **5 of 7** | **Rev** | **A**
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**Client** | Made by | ER/EM | Date | Feb 2006
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**Checked by** | HB | Date | March 2006
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**y_a = 4,01 mm**  
**y_b = 18,27 mm**  

**I_s = 21211,8 mm^4**

**Calculation of linear spring stiffness**

\[
K_1 = \frac{E t^3}{4(1 - \nu^2) b_1^2 h_w + b_1^3 + 0,5 b_2 h_2 h_f k_f} = 2,487 \text{ N/mm}^2
\]

**b_1 = b - y_b - t/2 = 104,23 mm** (the distance from the web-to-flange junction to the gravity center of the effective area of the edge stiffener, including the efficient part of the flange b_2)

**k_f = 0** (flange 2 is in tension)

**h_w = 150 mm** is the web depth

Elastic critical buckling stress for the effective stiffener section

\[
\sigma_{cr,s} = \frac{2\sqrt{KEI_s}}{A_s} = 519,195 \text{ N/mm}^2
\]

**Reduction factor \(\chi_d\) for distortional buckling**

\[
\bar{\lambda}_d = \sqrt{\frac{f_{yb}}{\sigma_{cr,s}}} = 0,98
\]

\[
0,65 < \bar{\lambda}_d < 1,38 \quad \text{then} \quad \chi_d = 1,47 - 0,723\bar{\lambda}_d = 0,76
\]

**Reduced area and thickness of effective stiffener section**

\[
A_{s,red} = \chi_d A_s \frac{f_{yb}}{\sigma_{com,fd}} = 300,88 \text{ mm}^2
\]

**t_{red} = t A_{s,red}/A_s = 3,8 mm**

**Calculation of effective section properties with distortional buckling effect**

**A_{eff,sh} = 2028 mm^2**

\[
\delta = 0,43 \sum_{j=1}^{n} \frac{\phi_j}{90^\circ} / \sum_{i=1}^{m} b_{p,i} = 0,02
\]

**A_{eff} = A_{eff,sh} (1 - \delta) = 1987 mm^2**
CALCULATION SHEET

zG = 68.98 mm (distance from the bottom fibre to the neutral axis)

\[ I_{y,\text{eff},sh} = 8.274 \times 10^6 \text{ mm}^4 \]
\[ I_{y,\text{eff}} = I_{y,\text{eff},sh} (1 - 2\delta) = 7.943 \times 10^6 \text{ mm}^4 \]
\[ W_{y,\text{eff},\text{sup}} = 92.34 \times 10^3 \text{ mm}^3 \]
\[ W_{y,\text{eff},\text{inf}} = 115.2 \times 10^3 \text{ mm}^3 \]

**Resistance of cross-section**

**Cross-section subject to bending moment**

\[ M_{c,Rd} = W_{y,\text{eff},\text{min}} f_y / \gamma_M = 41.97 \text{ kNm} \text{ for Class 4 cross-section} \]

Design bending moment \( M_{Ed} = 14.4 \text{ kNm} \)

Cross-section moment resistance is Ok

**Cross-section subject to shear**

\[ V_{pl,Rd} = A_v (f_y / \sqrt{3}) / \gamma_M = 209.95 \text{ kN} \]

\( A_v = 800 \text{ mm}^2 \) is the shear area

Design shear force \( V_{Ed} = 14.4 \text{ kN} \)

Cross-section shear resistance is Ok

**Cross-section subjected to combination of loads**

\( V_{Ed} = 14.4 \text{ kN} > 0.5 V_{pl,Rd} = 104.97 \text{ kN} \)

There is no interaction between bending moment and shear force

**Flexural members**

**Lateral-torsional buckling**

\[ M_{b,Rd} = \chi_{LT} W_{y,\text{eff},\text{sup}} f_y / \gamma_M \text{ for Class 4 cross-section} \]

\[ \chi_{LT} = \frac{1}{\varphi_{LT} + \left[ \varphi_{LT}^2 - \bar{\lambda}_{LT}^2 \right]^{0.5}} \leq 1 \]

\[ \varphi_{LT} = 0.5 \left( 1 + \alpha_{LT} \left( \bar{\lambda}_{LT} - 0.4 \right) + \bar{\lambda}_{LT}^2 \right) \]

\[ \bar{\lambda}_{LT} = \left( \frac{W_{y,\text{eff}} f_y}{M_{cr}} \right) \]

\( \alpha_{LT} = 0.34 \) for cold formed sections

Determination of the elastic critical moment for lateral-torsional buckling

\[ M_{cr} = C \left[ \frac{\pi^2 EI_y}{(k_z L)^2} \right]^{1/2} \left( \frac{I_w}{k_w} \right) \left( \frac{k_z L}{k_w} \right)^3 G I_z \left( C_2 z_2 - C_3 z_3 \right)^2 \left( C_2 z_2 - C_3 z_3 \right)^2 \]
For simply supported beams with uniform distributed load: $C_1 = 1.12$, $C_2 = 0.45$ and $C_3 = 0.525$.

Assuming normal conditions of restraint at each end: $k_z = k_w = 1$.

$z_e = z_a - z_s = h/2 = 80$ mm

$z_a$ is the co-ordinate of point load application

$z_s$ is the co-ordinate of the shear centre

$y_G = 45.34$ mm (distance from the central axis of the web to the gravity centre)

$I_{z,sh} = 4.274 \times 10^6$ mm$^4$

$I_{w,sh} = 23.19 \times 10^9$ mm$^6$

$I_e = I_{z,sh} (1 - 2\delta) = 4.103 \times 10^6$ mm$^4$

$I_w = I_{w,sh} (1 - 4\delta) = 21.33 \times 10^9$ mm$^6$

Note: The expression used to determine the warping torsion is obtained from Wei-Wen You, “Cold-Formed Steel Design”, Appendix B-Torsion

Then, $M_{cr} = C_1 \frac{\pi^2 EI_z}{(k_z L)^2} \left[ \frac{k_z}{k_w} \left( \frac{I_w}{I_z} + \frac{(k_z L)^2}{\pi^2 EI_z} + C_2 z_g^2 \right) \right]^{1/2} - (C_2 z_g^2) = 33.74$ kNm

$\bar{\lambda}_{LT} = \sqrt{\frac{W_{y,eff, sup} f_y}{M_{cr}}} = 1.17$ ($W_{y,eff, sup} = 92.39 \times 10^3$ mm$^3$, compression flange)

$\varphi_{LT} = 0.5 \left( 1 + \alpha_{LT} \left( \bar{\lambda}_{LT} - 0.4 \right) + \bar{\lambda}_{LT}^2 \right) = 1.315$

$\chi_{LT} = \frac{1}{\varphi_{LT} + \left( \varphi_{LT}^2 - \bar{\lambda}_{LT}^2 \right)^{0.5}} = 0.522$

$M_{b,Rd} = \chi_{LT} W_{y,eff, sup} f_y / \gamma_{M1} = 21.91$ kNm

Design moment $M_{Ed} = 14.4$ kNm, therefore lateral torsional buckling resistance $Ok$

Note: As the load is not applied through the shear centre of the channel, it is also necessary to check the interaction between the torsional resistance of the cross-section and the lateral torsional buckling resistance of the member.

Shear buckling resistance

The shear buckling resistance only requires checking when $h_w/t \geq 52\varepsilon/\eta$ for an unstiffened web.

The recommended value for $\eta = 1.20$

$h_w/t = 28$, $52\varepsilon/\eta = 28.99$, therefore no further check required.
DESIGN EXAMPLE 13 - HOLLOW SECTION LATTICE GIRDER

The lattice girder supports roof glazing and is made of square and rectangular hollow sections of grade 1.4301 stainless steel; a comparison is made between material in two strength levels - the annealed condition ($f_y = 220 \text{ N/mm}^2$) and in the cold worked condition (strength level CP460, $f_y = 460 \text{ N/mm}^2$). Calculations are performed at the ultimate limit state and then at the fire limit state for a fire duration of 30 minutes. For the CP460 material the reduction factors for the mechanical properties at elevated temperatures are conservatively taken as those for grade 1.4318 C850 (Table 7.1).

The structural analysis was carried out using the FE-program WINRAMI marketed by Finnish Constructional Steelwork Association (FCSA) (www.terasrakenneyhdistys.fi). The WINRAMI design environment includes square, rectangular and circular hollow sections for stainless steel structural analysis. WINRAMI solves the member forces, deflections and member resistances for room temperature and structural fire design and also joint resistance at room temperature (it also checks all the geometrical restraints of truss girder joints). In the example, the chord members are modelled as continuous beams and the diagonal members as hinge jointed. According to EN 1993-1-1, the buckling lengths for the chord and diagonal members could be taken as 0.9 times and 0.75 times the distance between nodal points respectively, but in this example conservatively the distance between nodal points has been used as the buckling length. The member forces were calculated by using WINRAMI with profile sizes based on the annealed strength condition. These member forces were used for both the annealed and CP460 girders.

This example focuses on checking 3 members: mainly axial tension loaded lower chord (member 0), axial compression loaded diagonal (member 31) and combination of axial compression and bending loaded upper chord member (member 5). The weight of the girders is also compared.

The welded joints should be designed according to the Section 6.3, which is not included in this example.

Annealed: lower chord 100x60x4, upper chord 80x80x5, corner vertical 60x60x5 diagonals from left to middle: 50x50x3, 50x50x3, 40x40x3, 40x40x3, 40x40x3, 40x40x3, 40x40x3.

CP460: lower chord 60x40x4, upper chord 70x70x4, corner vertical 60x60x5, all diagonals 40x40x3.

Span length 15m, height in the middle 3.13 m, height at the corner 0.5 m.

Weight of girders: Annealed: 407 kg, CP460 307 kg. The weight is not fully optimized.
Actions

Assuming the girder carries equally distributed snow load, glazing and its support structures and weight of girder:

Permanent actions ($G$): Load of glazing and supports 1 kN/m²

Dead load of girder (WINRAMI calculates the weight)

Variable actions ($Q$): Snow load 2 kN/m²

Load case 1 to be considered (ultimate limit state): $\sum_j \gamma_{G,j} G_{k,j} + \gamma_{Q,1} Q_{k,1}$

Load case 2 to be considered (fire situation): $\sum_j \gamma_{G_A,j} G_{k,j} + \gamma_{\psi,1} Q_{k,1}$

Ultimate limit state (room temperature design) Fire design

$\gamma_{G,j} = 1.35$ (unfavourable effects) $\gamma_{G_A,j} = 1.0$

$\gamma_{Q,1} = 1.5$ $\gamma_{\psi,1} = 0.2$

(Recommended partial safety factors for actions shall be used in this example)

Factored actions for ultimate limit state:

Permanent action: Load on nodal points: $1.35 \times 4.1$ kN

Self weight of girder (is included by WINRAMI)

Variable action Load from snow: $1.5 \times 8.1$ kN

Forces at critical member are:

Forces are determined by the model using profiles in the annealed strength condition

Lower chord member, member 0

Annealed: 100x60x4 mm, CP460: 60x40x4 mm

$N_{c,Ed} = 142.2$ kN, $N_{c,Ed} = 46.9$ kN

$M_{max,Ed} = 0.672$ kNm, $M_{max,Ed} = 0.245$ kNm

Upper chord member, member 5

Annealed: 80x80x5 mm, CP460: 70x70x4 mm

$N_{c,Ed} = -149.1$ kN, $N_{c,Ed} = -49.2$ kN

$M_{max,Ed} = 2.149$ kNm, $M_{max,Ed} = 0.731$ kNm

Diagonal member, member 31

Annealed: 50x50x3 mm, CP460: 40x40x3 mm

$N_{c,Ed} = -65.9$ kN, $N_{c,Ed} = -21.7$ kN
CALCULATION SHEET

Material properties
Use material grade 1.4301
Annealed:  $f_y = 220 \text{ N/mm}^2$  $f_u = 550 \text{ N/mm}^2$  $E = 200 000 \text{ N/mm}^2$
CP460:  $f_y = 460 \text{ N/mm}^2$  $f_u = 650 \text{ N/mm}^2$  $E = 200 000 \text{ N/mm}^2$

Partial safety factors
The following partial safety factors are used throughout the design example:
$\gamma_M = 1.1$,  $\gamma_M = 1.1$,  $\gamma_M = 1.1$

Cross section properties
Annealed
Member 0:  $A= 1175 \text{ mm}^2$  $W_{pl,y}= 37,93 \cdot 10^3 \text{ mm}^3$
Member 5:  $A= 1436 \text{ mm}^2$  $I_y=131,44 \cdot 10^4 \text{ mm}^4$  $i_y=30,3 \text{ mm}$  $W_{pl,y} = 39,74 \cdot 10^3 \text{ mm}^3$
Member 31:  $A= 541 \text{ mm}^2$  $I_y=19,47 \cdot 10^4 \text{ mm}^4$  $i_y=19 \text{ mm}$  $W_{pl,y} = 9,39 \cdot 10^3 \text{ mm}^3$

CP460
Member 0:  $A= 695 \text{ mm}^2$  $W_{pl,y} = 13,16 \cdot 10^3 \text{ mm}^3$
Member 5:  $A=1015 \text{ mm}^2$  $I_y=72,12 \cdot 10^4 \text{ mm}^4$  $i_y=26,7 \text{ mm}$  $W_{pl,y} = 24,76 \cdot 10^3 \text{ mm}^3$

Classification of the cross-section of member 5 and member 31
Annealed:  $\varepsilon=1,01$  CP460:  $\varepsilon =0,698$
Assume conservatively that $c = h - 2t$
Annealed 80x80x5 : $c = 80 - 10 = 70 \text{ mm}$  CP460 70x70x4 : $c = 70 - 8 = 62 \text{ mm}$
Annealed 50x50x3 : $c = 50 - 6 = 44 \text{ mm}$  CP460 40x40x3 : $c = 40 - 6 = 34 \text{ mm}$
Flange/web subject to compression:
Annealed 80x80x5 : $c/t = 14$  CP460 70x70x4 : $c/t = 15,5$
Annealed 50x50x3 : $c/t = 14,6$  CP460 40x40x3 : $c/t = 11,3$
For Class 1,  $\frac{c}{t} \leq 25,7 \varepsilon$, therefore both profiles are classified as Class 1
Member 31:  $A=421 \text{ mm}^2$  $I_y=9,32 \cdot 10^4 \text{ mm}^4$  $i_y=14,9 \text{ mm}$  $W_{pl,y} = 5,72 \cdot 10^3 \text{ mm}^3$

LOWERING CHORD MEMBER, DESIGN IN ROOM AND FIRE TEMPERATURE
A) Room temperature design
Tension resistance of cross section
$$N_{pl,Rd} = A_g f_y / \gamma_M$$
Annealed:  $N_{pl,Rd} = 1175 \text{ mm}^2 \times 220 \text{ N/mm}^2 / 1,1 = 235 \text{ kN} > 142,2 \text{ kN OK.}$
CP460:  $N_{pl,Rd} = 695 \text{ mm}^2 \times 460 \text{ N/mm}^2 / 1,1 = 290 \text{ kN} > 142,2 \text{ kN OK.}$
### Moment resistance of cross-section

\[ M_{c,Rd} = \frac{W_p f_y}{\gamma_M} \]

**Annealed:**  \[ M_{c,Rd} = \frac{37.93 \times 10^3 \times 220}{1.1 \times 10^6} = 7.58 \text{ kNm} > 0.672 \text{ kNm OK.} \]

**CP460:**  \[ M_{c,Rd} = \frac{13.16 \times 10^3 \times 460}{1.1 \times 10^6} = 5.50 \text{ kNm} > 0.672 \text{ kNm OK.} \]

### Axial tension and bending moment interaction

\[ \frac{N_{Ed}}{N_{Rd}} + \frac{M_{y,Ed}}{M_{y,Rd}} \leq 1 \]

**Annealed:**  \[
\frac{142.2 \text{ kN}}{235 \text{ kN}} + \frac{0.672 \text{ kNm}}{7.58 \text{ kNm}} = 0.69 \leq 1 \quad \text{OK.}
\]

**CP460:**  \[
\frac{142.2 \text{ kN}}{290 \text{ kN}} + \frac{0.672 \text{ kNm}}{5.50 \text{ kNm}} = 0.61 \leq 1 \quad \text{OK.}
\]

### B) Fire temperature design

**\( \varepsilon_{res} = 0.2 \)**

Steel temperature after 30 min fire \( \Theta = 823 \degree C \)

**\( f_{2,0} = f_{0.2\text{proof},0} + g_{2,0} (f_{u,0} - f_{0.2\text{proof},0}) \)**

**Annealed:**

- \( k_{0.2\text{proof},0} = 0.27 - 23/100 \times (0.27 - 0.14) = 0.240 \)
- \( f_{0.2\text{proof},0} = 0.240 \times 220 \text{ N/mm}^2 = 52.8 \text{ N/mm}^2 \)
- \( g_{2,0} = (0.27 - 23/100 \times (0.27 - 0.38) = 0.357 \)
- \( f_{u,0} = (0.27 - 23/100 \times (0.27 - 0.15)) \times 550 \text{ N/mm}^2 = 133.3 \text{ N/mm}^2 \)
- \( f_{2,0} = 52.8 \text{ N/mm}^2 + 0.357 \times (133.3 - 52.8) \text{ N/mm}^2 = 81.5 \text{ N/mm}^2 \)
- \( k_{2,0} = 81.5 / 220 = 0.37 \)

**CP460:**

- \( k_{0.2\text{proof},0} = 0.23 - 23/100 \times (0.23 - 0.11) = 0.202 \)
- \( f_{0.2\text{proof},0} = 0.202 \times 460 \text{ N/mm}^2 = 93.1 \text{ N/mm}^2 \)
- \( g_{2,0} = 0.25 \)
- \( f_{u,0} = (0.24 - 23/100 \times (0.24 - 0.10)) \times 650 \text{ N/mm}^2 = 135.1 \text{ N/mm}^2 \)
- \( f_{2,0} = 93.1 \text{ N/mm}^2 + 0.25 \times (135.1 - 93.1) \text{ N/mm}^2 = 103.6 \text{ N/mm}^2 \)
- \( k_{2,0} = 103.6 / 460 = 0.225 \)

### Tension resistance of cross section

\[ N_{fi,Rd} = k_{2,0} N_{Rd} [\gamma_{M0} / \gamma_{M,fi}] \]

**Annealed:**  \[ N_{fi,Rd} = 0.370 \times 235 \text{ kN} \times 1.1 / 1.0 = 95.6 \text{ kN} > 46.9 \text{ kN OK.} \]

**CP460:**  \[ N_{fi,Rd} = 0.225 \times 290 \text{ kN} \times 1.1 / 1.0 = 59.3 \text{ kN} > 46.9 \text{ kN OK.} \]
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CALCULATION SHEET

Moment resistance of cross-section

$$M_{f,0,Rd} = k_{2,0} M_{Rd} \left[ \frac{f_{y} M_{0}}{\gamma_{M_{0}}} \right] \gamma_{M_{B}}$$

Annealed: $$M_{f,0,Rd} = 0.370 \times 7.58 \text{kNm} \times 1.1 / 1.0 = 3.08 \text{kNm} > 0.245 \text{kNm} \text{OK.}$$

CP460: $$M_{f,0,Rd} = 0.225 \times 5.50 \text{kNm} \times 1.1 / 1.0 = 1.36 \text{kNm} > 0.245 \text{kNm} \text{OK.}$$

Axial tension and bending moment interaction

$$\frac{N_{Ed}}{N_{Rd}} + \frac{M_{y,Ed}}{M_{y,Rd}} \leq 1$$

Annealed: $$\frac{46,9 \text{kN}}{95,6 \text{kN}} + \frac{0,245 \text{kNm}}{3,08 \text{kNm}} = 0,57 \leq 1 \text{ OK.}$$

CP460: $$\frac{46,9 \text{kN}}{59,3 \text{kN}} + \frac{0,245 \text{kNm}}{1,36 \text{kNm}} = 0,97 \leq 1 \text{ OK.}$$

DIAGONAL MEMBER DESIGN IN ROOM AND FIRE TEMPERATURE

Buckling length = 1253 mm

A) Room temperature design

$$N_{b,Rd} = \frac{\chi f_{y}}{\gamma_{M_{1}}}$$

Annealed:

$$\lambda = \frac{L_{cr}}{i} \frac{1}{\pi} \sqrt{\left( \frac{f_{y}}{E} \right)} = \frac{1253}{19} \frac{1}{\pi} \sqrt{\left( \frac{220}{200000} \right)} = 0.696$$

$$\varphi = 0.5(1 + \alpha(\lambda - \lambda_{0}) + \lambda^{2}) = 0.5(1+0.49(0.696-0.4)+0.696^{2}) = 0.815$$

$$\chi = \frac{1}{\varphi + \sqrt{(\varphi^{2} - \lambda^{2})}} = \frac{1}{0.815 + \sqrt{(0.815^{2} - 0.696^{2})}} = 0.807$$

$$N_{b,Rd} = 0.807 \times 541 \text{mm}^{2} \times 220 \text{N/mm}^{2} / 1.1 = 87.3 \text{kN} > 65.9 \text{kN} \text{ OK.}$$

CP460:

$$\lambda = \frac{L_{cr}}{i} \frac{1}{\pi} \sqrt{\left( \frac{f_{y}}{E} \right)} = \frac{1253}{14.9} \frac{1}{\pi} \sqrt{\left( \frac{460}{200000} \right)} = 1.283$$

$$\varphi = 0.5(1 + \alpha(\lambda - \lambda_{0}) + \lambda^{2}) = 0.5(1+0.49(1.283-0.4)+1.283^{2}) = 1.540$$

$$\chi = \frac{1}{\varphi + \sqrt{(\varphi^{2} - \lambda^{2})}} = \frac{1}{1.540 + \sqrt{(1.540^{2} - 1.283^{2})}} = 0.418$$

$$N_{b,Rd} = 0.418 \times 421 \text{mm}^{2} \times 460 \text{N/mm}^{2} / 1.1 = 73.6 \text{kN} > 65.9 \text{kN} \text{ OK.}$$
B) Fire temperature design

\[ \varepsilon_{res} = 0,2 \]
Steel temperature after 30 min fire \( \Theta = 832 \, ^\circ C \)

**Annealed:**

\[ k_{0,2proof,0} = 0,27-32/100 \times (0,27-0,14) = 0,228 \]
\[ k_{E,0} = 0,63-32/100 \times (0,63-0,45) = 0,572 \]

**CP460:**

\[ k_{0,2proof,0} = 0,23-32/100 \times (0,23-0,11) = 0,191 \]
\[ k_{E,0} = 0,52-32/100 \times (0,52-0,35) = 0,465 \]

\[ N_{b,fi,t,Rd} = \chi_{\beta} A k_{0,2proof, \beta} f_y / \gamma_{M, \beta} \]

**Annealed:**

\[ \lambda_\beta = \lambda_\beta \left( k_{0,2proof, \beta} / k_{E, \beta} \right) = 0,696 \sqrt{0,228/0,572} = 0,439 \]
\[ \varphi_\beta = 0,5(1 + \alpha(\lambda_\beta - \lambda_0) + 0,439^2) = 0,5(1+0,49(0,439-0,4)+0,439^2) = 0,606 \]
\[ \chi_{\beta} = \frac{1}{\varphi_0 + \sqrt{\varphi_0^2 - \lambda_\beta^2}} \]
\[ = \frac{1}{0,606 + \sqrt{0,606^2 - 0,439^2}} = 0,977 \]
\[ N_{b,fi,t,Rd} = 0,977 \times 541 \, mm^2 \times 0,228 \times 220 \, N/mm^2 /1,0 = 26,5 \, kN > 21,7 \, kN \, OK. \]

**CP460:**

\[ \lambda_\sigma = \lambda_\sigma \left( k_{0,2proof, \sigma} / k_{E, \sigma} \right) = 1,283 \sqrt{0,191/0,465} = 0,822 \]
\[ \varphi_\sigma = 0,5(1 + \alpha(\lambda_\sigma - \lambda_0) + 0,439^2) = 0,5(1+0,49(0,822-0,4)+0,822^2) = 0,941 \]
\[ \chi_\sigma = \frac{1}{\varphi_0 + \sqrt{\varphi_0^2 - \lambda_\sigma^2}} \]
\[ = \frac{1}{0,941 + \sqrt{0,941^2 - 0,822^2}} = 0,714 \]
\[ N_{b,fi,t,Rd} = 0,714 \times 421 \, mm^2 \times 0,191 \times 460 \, N/mm^2 /1,0 = 26,4 \, kN > 21,7 \, kN \, OK. \]

**UPPER CHORD MEMBER DESIGN IN ROOM AND FIRE TEMPERATURE**

Buckling length = 1536 mm

**A) Room temperature design**

\[ \frac{N_{Ed}}{(N_{b,Rd})_{min}} + k_y \left( \frac{M_{y,Ed} + N_{Ed} e_{N_y}}{\beta_{W,y} W_{pl,y} f_y / \gamma_{M1}} \right) \leq 1,0 \]

**Annealed:**

\[ \beta_{W,y} = 1,0 \, \text{class 1 cross section} \]
\[ k_y = 1,0 + 2(\lambda_0 - 0,5) N_{Ed} / N_{b,Rd,y} \, \text{but} \, 1,2 \leq k_y \leq 1,2 + 2 N_{Ed} / N_{b,Rd,y} \]
\[ \overline{\lambda} = \frac{L_{cr} \, 1}{\pi \sqrt{f_y / E}} = \frac{1536 \, 1}{30,3 \, \pi \sqrt{220/200000}} = 0,535 \]

**Section 7.4.7**

**Table 1.1**

**Eq. 7.8**

**Eq. 7.12**

**Eq. 7.11**

**Eq. 7.10**

**Eq. 5.40**

**Sec. 5.5.2**

**Eq. 5.5a**
Job No. | VALCOSS | Sheet 7 of 9 | Rev A
---|---|---|---
Job Title | RFCS Stainless Steel Valorisation Project
Subject | Design Example 13 – Stainless steel lattice girder made of hollow sections
Client | Made by PTY/AAT | Date Jan 2006
Checked by | MAP | Date Feb 2006

**CALCULATION SHEET**

\[
\varphi = 0.5(1 + \alpha(\bar{\lambda} - \bar{\lambda}_0) + \bar{\lambda}^2) = 0.5(1 + 0.49(0.535 - 0.4) + 0.535^2) = 0.676
\]
\[
\chi = \frac{1}{\varphi + \sqrt{(\varphi^2 - \lambda^2)}} = \frac{1}{0.676 + \sqrt{(0.676^2 - 0.535^2)}} = 0.917
\]
\[
N_{b,Rd,y} = 0.917 \times 1436 \text{ mm}^2 \times 220 \text{ N/mm}^2 / 1.1 = 263.3 \text{ kN} > 149.1 \text{ kN}
\]
\[
k_y = 1.0 + 2(0.535 - 0.5) \times 149.1 / 263.3 = 1.039 \quad \text{because calculated value is less than 1.2, the value of } k_y = 1.2.
\]
\[
\frac{149.1}{263.3} + 1.2 \left( \frac{2.149 \times 10^2}{1.0 \times 39.74 \times 10^3 \times 220 / 1.1} \right) = 0.890 < 1.0 \quad \text{OK}
\]

**CP460**

\[
\beta_{W,y} = 1.0 \quad \text{class 1 cross section}
\]
\[
\bar{\lambda} = \frac{L_y}{i} \frac{1}{\pi} \sqrt{f_y / E} = \frac{1536.1}{267} \frac{1}{\pi} \sqrt{460 / 200000} = 0.878
\]
\[
\varphi = 0.5(1 + \alpha(\bar{\lambda} - \bar{\lambda}_0) + \bar{\lambda}^2) = 0.5(1 + 0.49(0.878 - 0.4) + 0.878^2) = 1.002
\]
\[
\chi = \frac{1}{\varphi + \sqrt{(\varphi^2 - \lambda^2)}} = \frac{1}{1.002 + \sqrt{(1.002^2 - 0.878^2)}} = 0.673
\]
\[
N_{b,Rd,y} = 0.673 \times 1015 \text{ mm}^2 \times 460 \text{ N/mm}^2 / 1.1 = 285.6 \text{ kN} > 149.1 \text{ kN}
\]
\[
k_y = 1.0 + 2(0.878 - 0.5) \times 149.1 / 285.6 = 1.394, \text{ but } 1.2 \leq k_y \leq 1.2 + 2(149.1 / 285.6) = 2.244, \text{ thus } k_y = 1.394
\]
\[
\frac{149.1}{285.6} + 1.394 \left( \frac{2.149 \times 10^2}{1.0 \times 24.76 \times 10^3 \times 460 / 1.1} \right) = 0.81 < 1.0 \quad \text{OK}
\]

**B) Fire temperature design**

\( r_{ecu} = 0.2 \)

Steel temperature 80x80x5 mm \( \Theta = 810 \) °C
Steel temperature 70x70x4 mm \( \Theta = 823 \) °C

**Annealed:**

\[
k_{0,2\text{proof},0} = 0.27 - 10 / 100 \times (0.27 - 0.14) = 0.257
\]
\[
f_{0,2\text{proof},0} = 0.257 \times 220 \text{ N/mm}^2 = 56.5 \text{ N/mm}^2
\]
\[
g_{2,0} = (0.35 - 10 / 100 \times 0.35 - 0.38) = 0.353
\]
\[
f_{u,0} = (0.27 - 10 / 100 \times (0.27 - 0.15)) \times 550 \text{ N/mm}^2 = 141.9 \text{ N/mm}^2
\]
\[
f_{2,0} = 56.5 \text{ N/mm}^2 + 0.353 \times (141.9 - 56.5) \text{ N/mm}^2 = 86.6 \text{ N/mm}^2
\]
\[
k_{2,0} = 86.6 / 220 = 0.394
\]
\[
k_{E,0} = 0.63 - 10 / 100 \times (0.63 - 0.45) = 0.612
\]

Section 7.2
Table 7.1
Eq. 7.1
### Design Example 13 – Stainless steel lattice girder made of hollow sections

**Client:** RFCS  
**Made by:** PTY/AAT  
**Date:** Jan 2006  
**Checked by:** MAP  
**Date:** Feb 2006

#### Calculation Sheet

**CP460:**

\[
\lambda_{0} = \lambda \sqrt{\left(k_{0,2}^{\text{proof},\theta} / k_{E,\theta}\right)} = 0,535 \sqrt{(0,257 / 0,612)} = 0,347
\]

\[
\varphi_{0} = 0,5(1 + \alpha(\varphi_{0} - \lambda_{0}) + \lambda_{0}^{2}) = 0,5(1+0,49(0,347-0,4)+0,347^{2}) = 0,547
\]

\[
\chi_{fi} = \frac{1}{\varphi_{0} + \sqrt{(\varphi_{0}^{2} - \lambda_{0}^{2})}} = 1,03 = 1,0
\]

\[
k_{y} = 1 - \frac{\mu_{y}N_{fi,Ed}}{\chi_{y,\beta}k_{0,2}^{\text{proof},\theta}f_{y} / \gamma_{M,\beta}} \leq 3
\]

\[
\mu_{y} = (1,2\beta_{M,y} - 3)\lambda_{y,\theta} + 0,44\beta_{M,y} - 0,29 \leq 0,8
\]

\[
\chi_{min,\beta}k_{0,2}^{\text{proof},\theta}f_{y} / \gamma_{M,\beta} = 1,0 \times 1436 \text{ mm}^{2} \times 0,257 \times 220 \text{ N/mm}^{2} / 1,0 = 81,2 \text{ kN}
\]

\[
M_{y,\beta,\theta,\text{rd}} = k_{2,\beta}(\gamma_{M_{0}} \gamma_{M_{f}})M_{\text{rd}} = 0,394 \times 1,1/1,0 \times 39,74 \times 10^{3} \times 220 / 1000 = 3,79 \text{ kN mm}
\]

\[
\psi = -0,487 \text{ kNm} / 0,731 \text{ kNm} = -0,666
\]

\[
\beta_{M,y} = 1,8-0,7\times\psi = 2,466
\]

\[
\mu_{y} = (1,2 \times 2,466-3)0,347 + 0,44 \times 2,466 - 0,29 = 0,78
\]

\[
k_{y} = 1 - 0,80 \times 49,2 \text{ kN} / 81,2 \text{ kN} = 0,515
\]

\[
49,2 / 81,2 = 0,515 \times 0,731 / 3,79 = 0,70 < 1,0 \text{ OK.}
\]

**Annealed:**

\[
\bar{\lambda}_{0} = \bar{\lambda} \sqrt{\left(k_{0,2}^{\text{proof},\theta} / k_{E,\theta}\right)} = 0,878 \sqrt{(0,202 / 0,481)} = 0,569
\]

\[
\varphi_{0} = 0,5(1 + \alpha(\varphi_{0} - \lambda_{0}) + \lambda_{0}^{2}) = 0,5(1+0,49(0,569-0,4)+0,569^{2}) = 0,703
\]

\[
\chi_{fi} = \frac{1}{\varphi_{0} + \sqrt{(\varphi_{0}^{2} - \lambda_{0}^{2})}} = \frac{1}{0,703 + \sqrt{(0,703^{2} - 0,569^{2})}} = 0,896
\]
**CALCULATION SHEET**

\[ \chi_{\text{min,f}} A_e k_{0,2,\text{proof},f} / \gamma M_{\text{f,f}} = 0.896 \times 1015 \text{ mm}^2 \times 0.202 \times 460 \text{ N/mm}^2 / 1.0 = 84.5 \text{ kN} \]

\[ > 49.2 \text{ kN OK.} \]

\[ M_{y,\text{f,f,Rd}} = k_2,0[\gamma M_0 / \gamma M_{\text{f,f}}] M_{\text{Rd}} = 0.225 \times 1.1 / 1.0 \times 24.76 \times 10^3 \times 460 / 1000^2 = 2.81 \text{ kNm} \]

\[ > 0.731 \text{ kNm OK.} \]

\[ \psi = -0.487 \text{ kNm/0.731 kNm} = -0.666 \]

\[ \beta_{M,y} = 1.8 - 0.7 \times \psi = 2.466 \]

\[ \mu_y = (1.2 \times 2.466 - 3)0.569 + 0.44 \times 2.466 - 0.29 = 0.771, \]

because calculated value is less than 0.8, the value of \( \mu_y = 0.8 \)

\[ k_y = 1 - 0.80 \times 49.2 \text{ kN/84.5 kN} = 0.534 \]

\[ \frac{49.2}{84.5} + 0.534 \times \frac{0.731}{2.81} = 0.72 < 1.0 \text{ OK.} \]